



# Dusty Plasma

**Waleed Moslem**  
Professor of Theoretical Plasma Physics

# Outline

- Types of plasma
- Occurance of dusty plasma
- Properties of dusty plasma
- Two milestones in dusty plasma
- Mach cones
- Wakefield

# Outline

- **Types of plasma**
- Occurance of dusty plasma
- Properties of dusty plasma
- Two milestones in dusty plasma
- Mach cones
- Wakefield

# Types of plasma

- (I) Classical plasma (electron-ion plasma)  
+ve ions / electrons / -ve ions / positrons
- (II) Dusty (complex) plasma  
+ve dust / -ve dust / +ve ions / electrons / -ve ions
- (III) Quantum plasma  
Electrons / positrons / holes / +ve ions

# Types of plasma, cont.



**Irving Langmuir**  
**1927**



**Padma Kant Shukla**  
**1990**



**Giovanni Manfredi**  
**2000**

# Types of plasma, cont.

## Classical plasma

- Mainly → +ve ions & electrons
- Sometimes → -ve ions & positrons
- 1927 → now
- Applications / observations / Experiment → laboratory, space plasma, astrophysical plasma

# Outline

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# Occurance of dusty plasma

- What is dusty plasma? A four component system, consisting of electrons, ions, neutral atoms and micron size solid dust grains
- A few nanometers to tens of micrometers
- A four component system, consisting of electrons, ions, neutral atoms and micron size solid dust grains
- Observations → Comet tails, Planetary rings, Solar and planetary nebulae, Lower ionosphere (mesosphere), Atmospheric lightning, Industrial plasma processing devices, Magnetic fusion devices ,...etc.

# Occurance of dusty plasma



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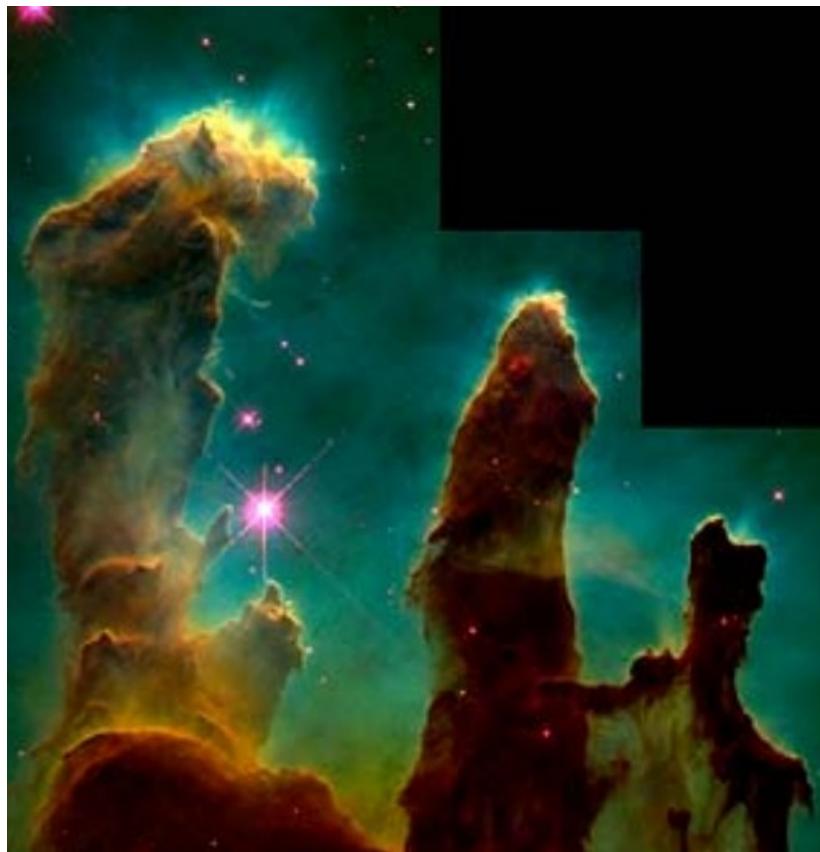
Hyakutake



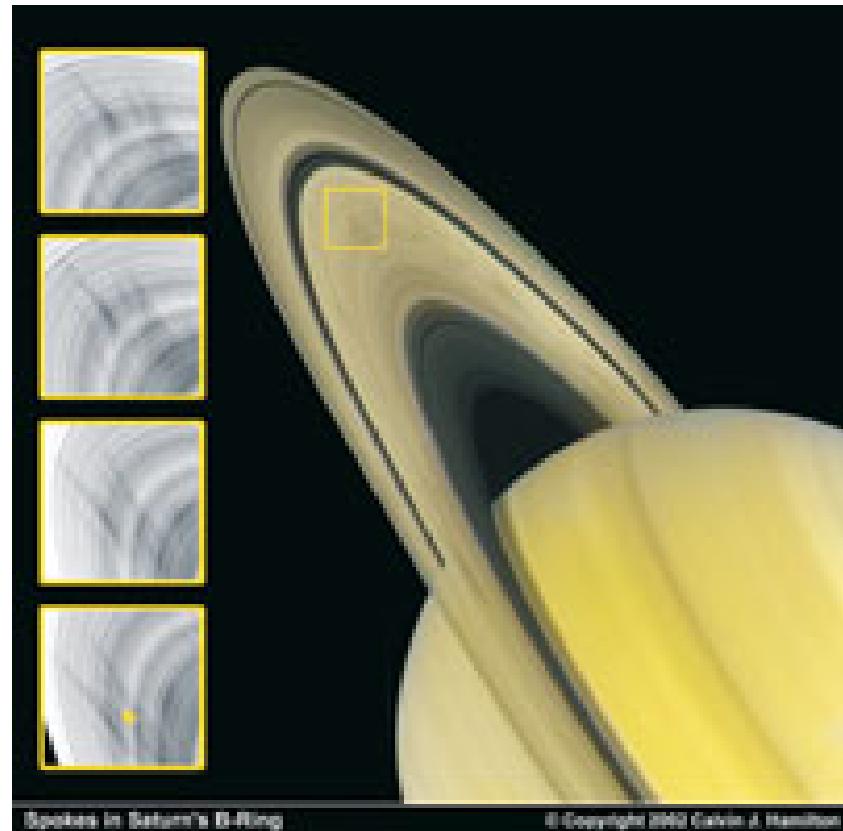
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Hale-Bopp

# Occurance of dusty plasma

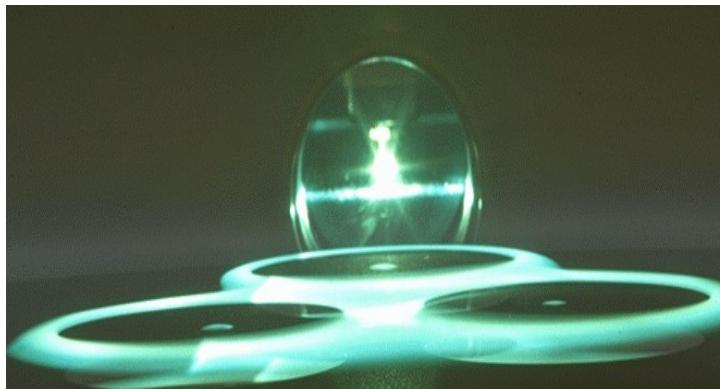


Eagle Nebula

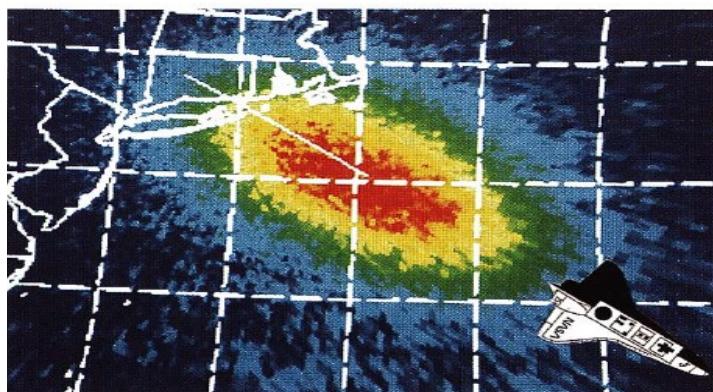


Saturn Rings

# Occurance of dusty plasma



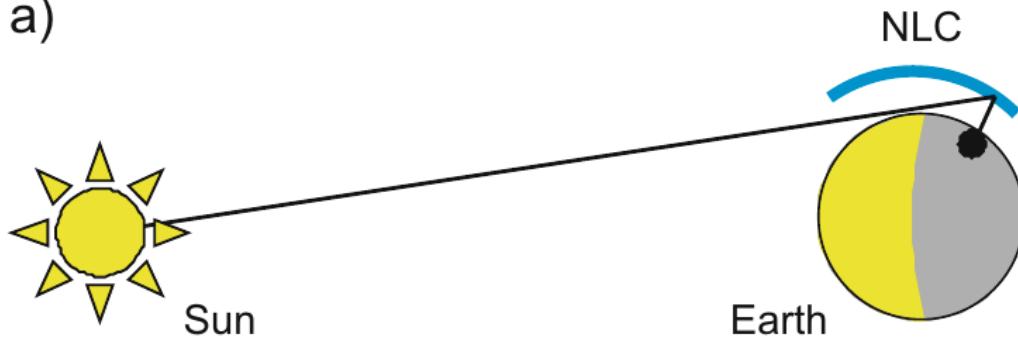
**Charged dust clouds** around silicon wafers, formed in a plasma processing device; a serious contamination issue



**Dusty plasma of charged ice** caused by the Space Shuttle engine exhaust

# Occurance of dusty plasma

a)

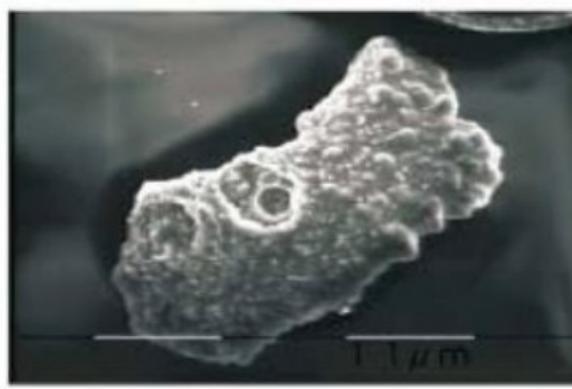


**Noctilucent clouds** formed in the summer mesosphere at 75-80 km altitude range; 100 nm water ice, charged

# Occurance of dusty plasma



0.1 mm

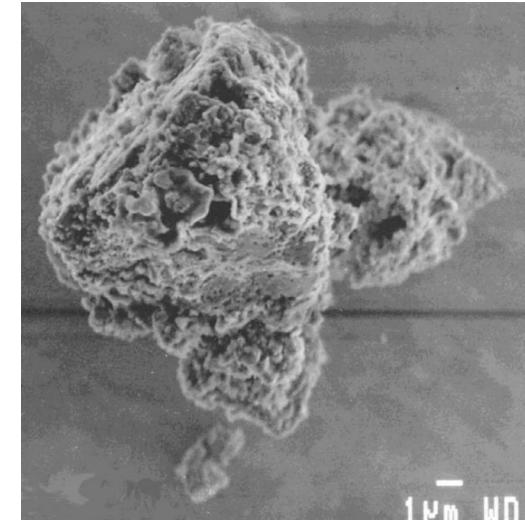
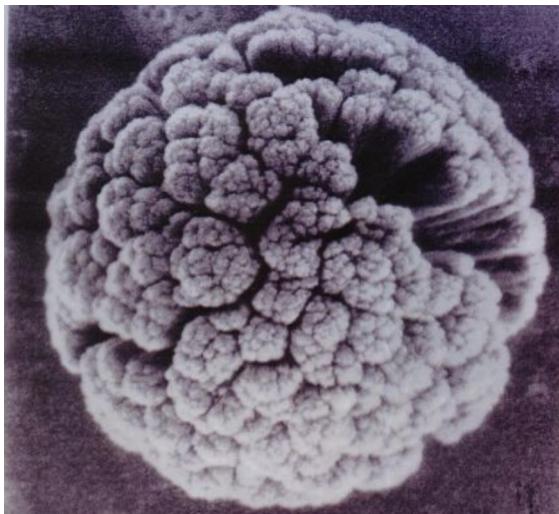


1 μm



200 nm

Significant amount of dust particles is observed in the chambers of fusion devices



# Occurance of dusty plasma

- The “dust” is a result of the strong interaction between the material walls and energetic plasma, which causes flaking, blistering, arching and erosion of the carbon limiters or beryllium surfaces.
- Studies indicate that dust can be transported deep into the plasma, causing a serious contamination problem.
- Movies 1 & 2 & 3 & 4

# Occurance of dusty plasma

- Flaking of redeposited material,

تقشر المواد المعاد ترسبيها

- Agglomeration from supersaturated vapour,

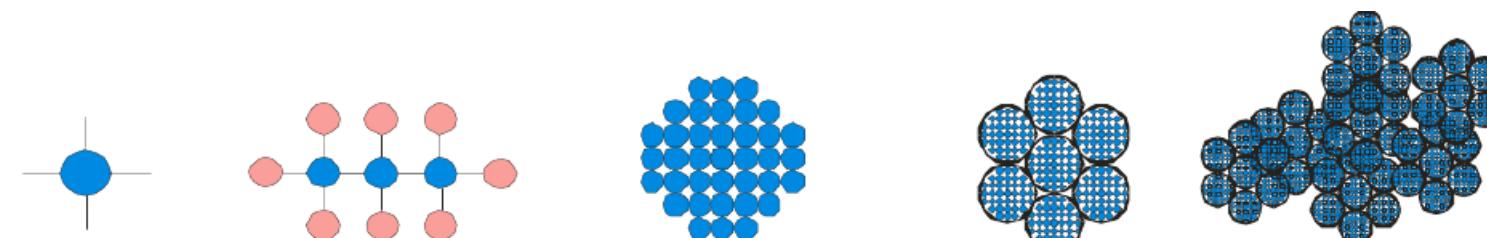
تكتل من بخار مفرط التسبيع

- Particulate ejection due to thermal transients,

طرد الجسيمات بسبب العبور الحراري

- Growth from hydrocarbon.

النمو من مركبات الهيدروكربونات



Molecule

Macro-molecule

Nanoparticle

Agglomerate

Powder

0.1 nm

1 nm

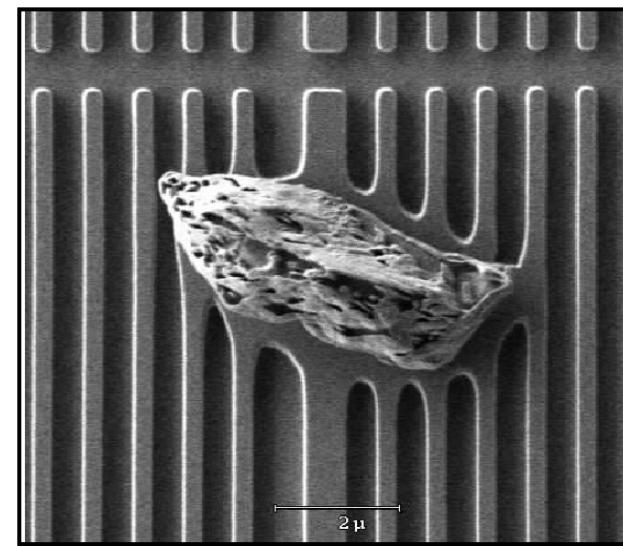
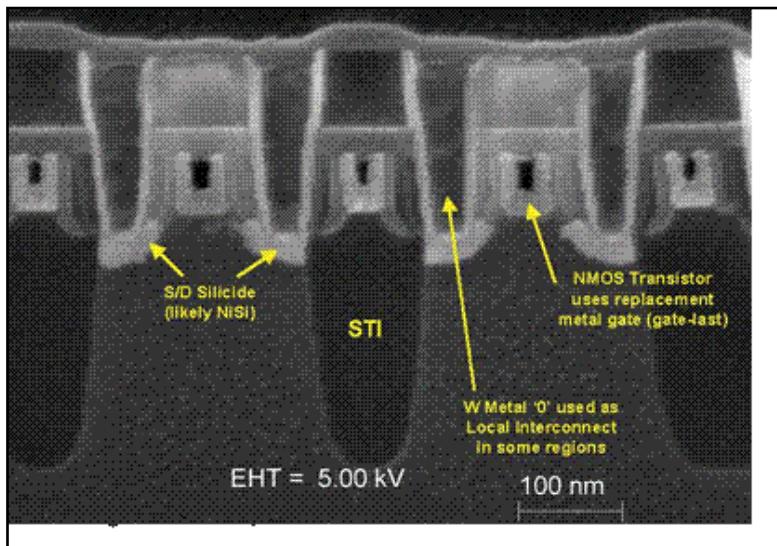
10 nm

100 nm

1 μm

# Occurance of dusty plasma

- Semiconductor industry
- Plasma chemistry and nanotechnology → coagulation of macroparticles

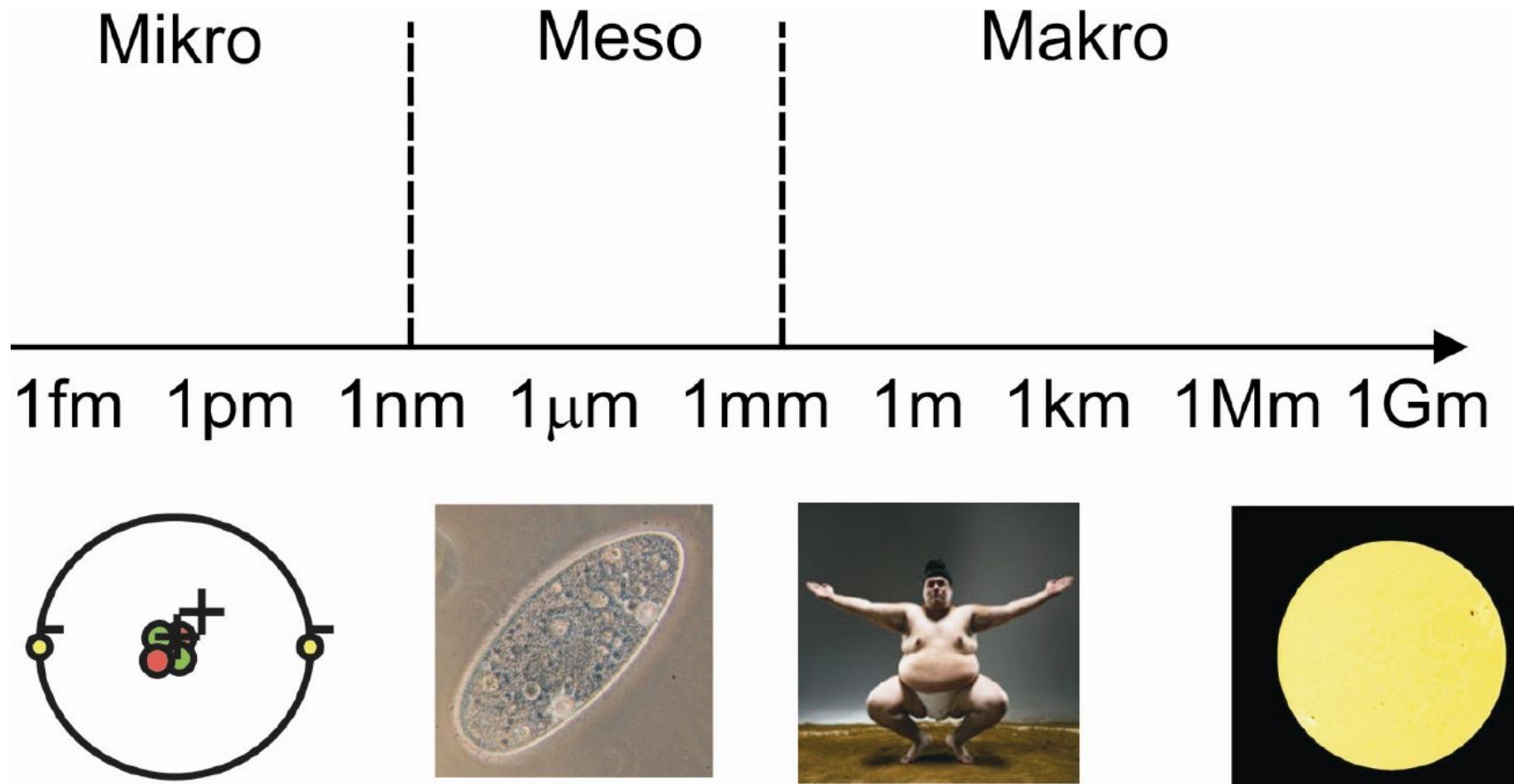


# Outline

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- Occurance of dusty plasma
- Properties of dusty plasma
- Two milestones in dusty plasma
- Mach cones
- Wakefield

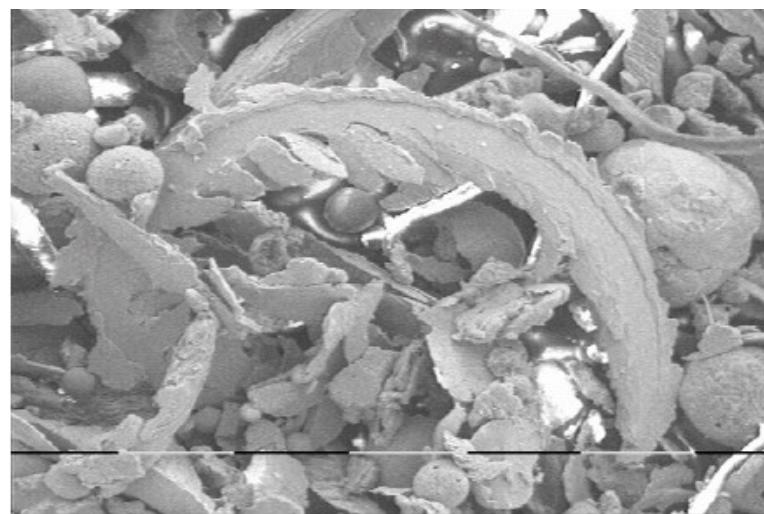
# Properties of dusty plasma

- Dusty plasmas are multi-component plasmas
- They contain electrons, ions, neutral atoms/molecules, and micro-particles/charged dust grains

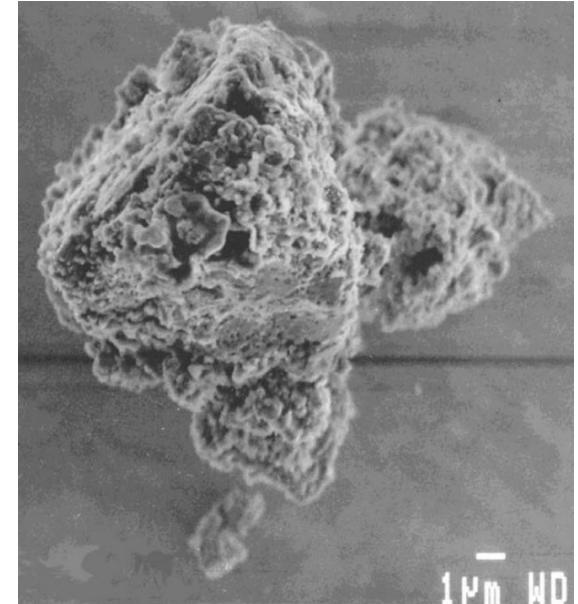


# Properties of dusty plasma

- They are significantly different from the usual electron-ion plasmas: dust size distributions
- New time scales associated with dust particle motion
- Dust charging as a dynamical variable



----- 0.1 mm



# Properties of dusty plasma

## Basic dust-plasma interaction

Charging

Capture of electrons

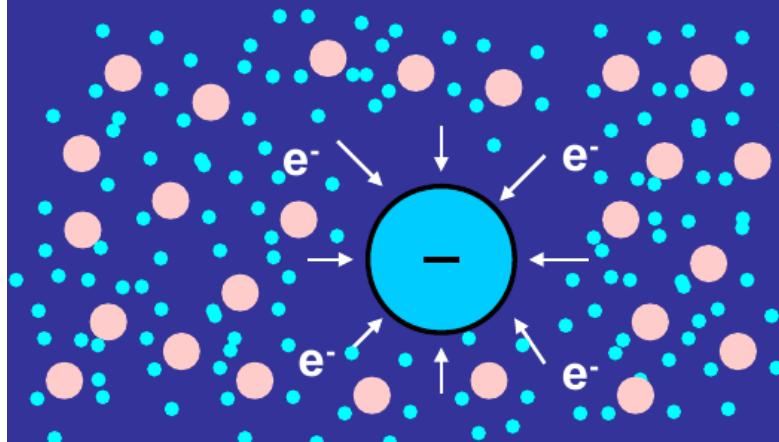
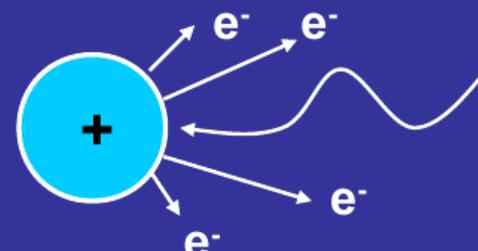
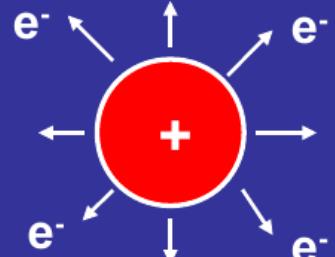


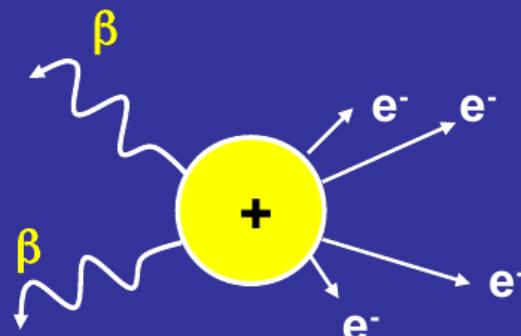
Photo-electron emission



Thermal-electron emission

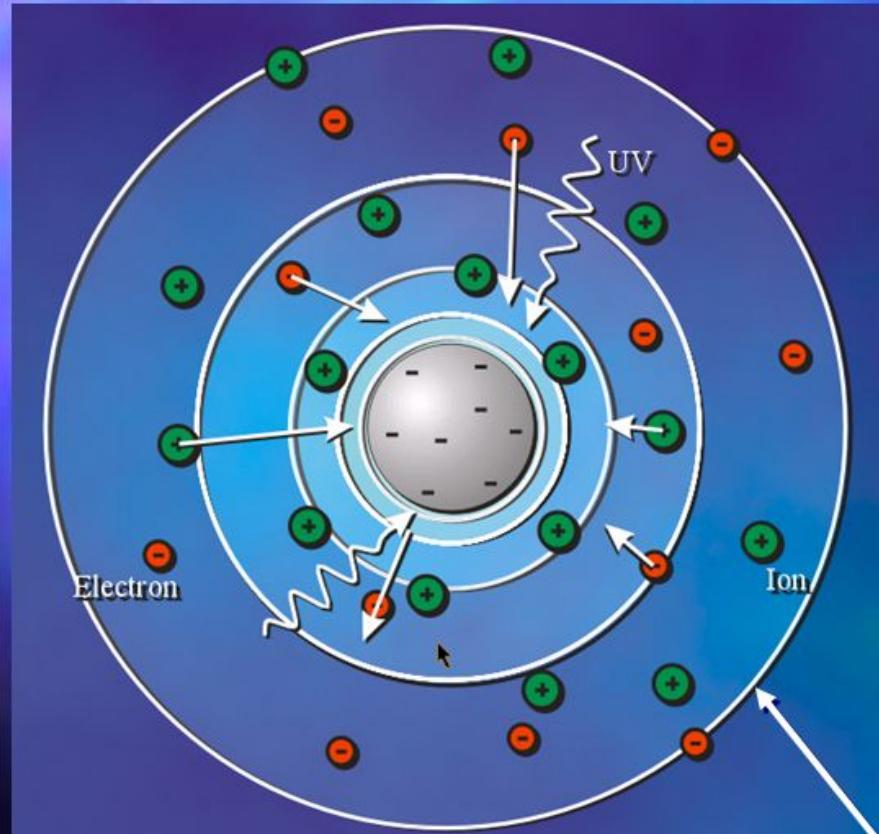


Radioactive decay



# Properties of dusty plasma

## Charging of a single particle in a plasma



### Collection of charges

particle is negatively charged due to higher mobility of electrons

positive charge cloud around particle  $\Rightarrow$  Debye screening

### Temporal charge variation

$$\frac{dQ}{dt} = I_{\text{electrons}} + I_{\text{ions}} + I_{\dots}$$

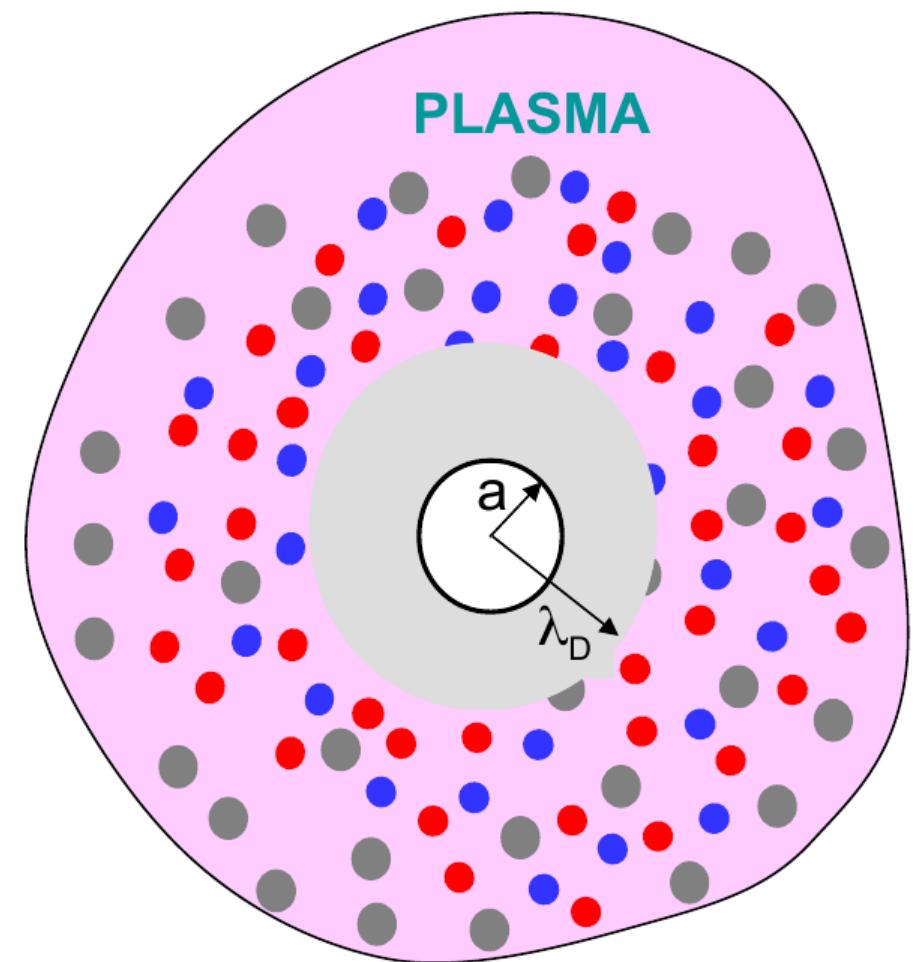
$$\text{Steady state: } \frac{dQ}{dt} = 0$$

For a particle of 1 $\mu\text{m}$  diameter:  $Q = -1500e$

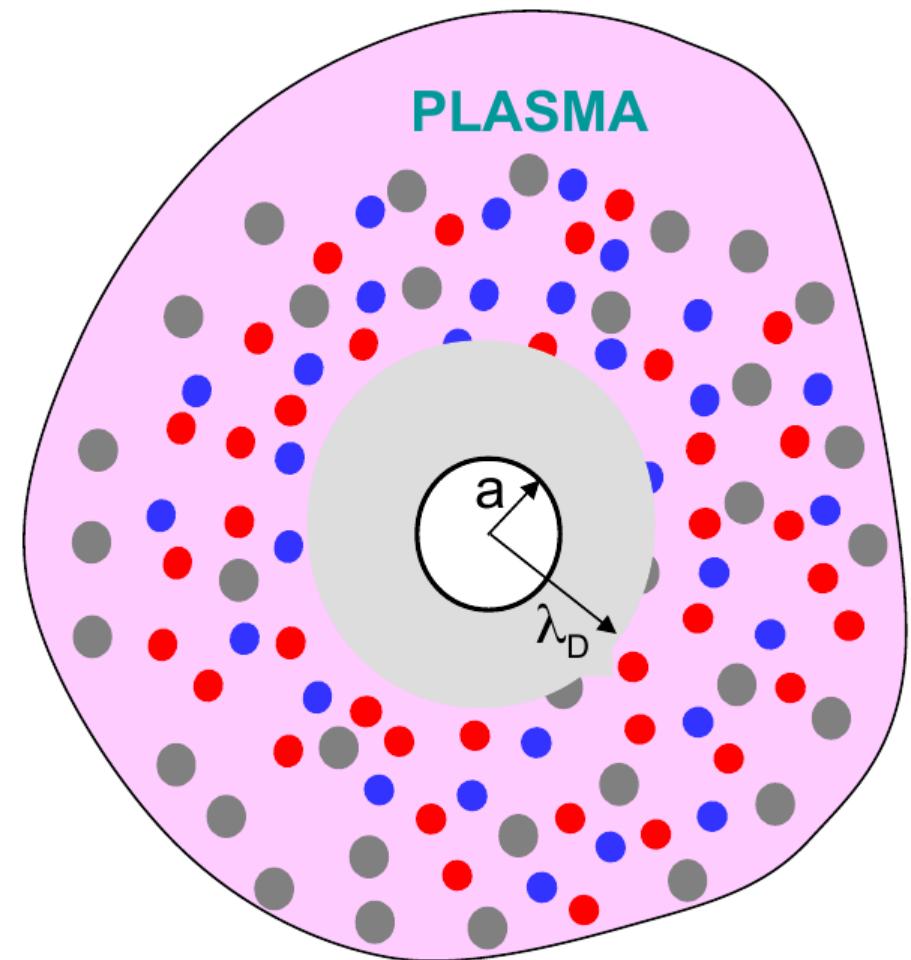
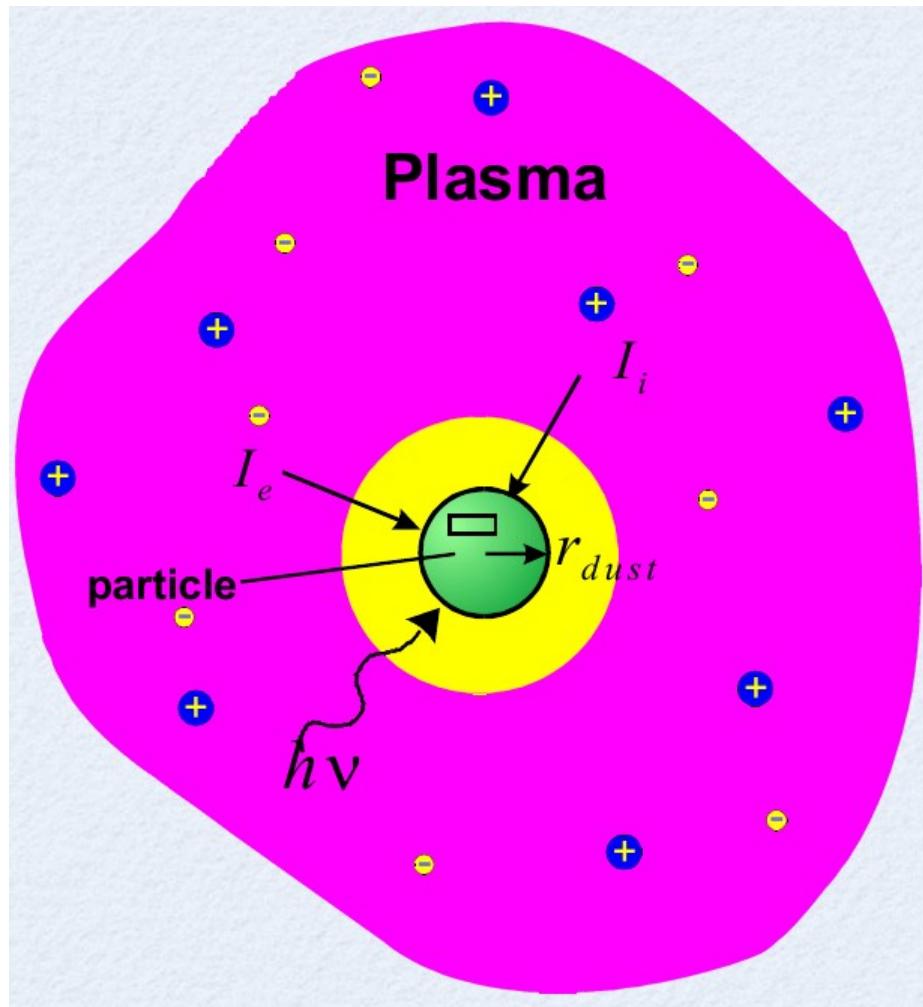
$$\text{Debye length: } \lambda_D = \sqrt{\frac{kT}{4\pi e^2 n}}$$

Potential contour lines

# Properties of dusty plasma



# Properties of dusty plasma



# Properties of dusty plasma

Electron-ion plasma	Dusty plasma
$n_{e0} = \sum_i Z_i n_{i0}$	$Q_d n_{d0} + e n_{e0} = e \sum_i Z_i n_{i0}$
$Q_i = Z_i e$	$Q_d = Z_d e \gg Q_i$
$Z_i = \text{const.}$	$dQ_d/dt = I_e + I_i + I_s + \dots$
$m_i$	$m_d \sim 10^{12} m_i$
$\lambda_{De}$	$\lambda_D \sim \lambda_{Di}$
Uniform particle sizes	Size distributions
IAW, EIC, $f \sim 1$ kHz	DAW, DLW, $f \sim 10$ Hz,

# Properties of dusty plasma

- Debye shielding

$$\lambda_D = \frac{\lambda_{De}\lambda_{Di}}{\sqrt{\lambda_{De}^2 + \lambda_{Di}^2}}$$

$$\lambda_{De} = (k_B T_e / 4\pi n_{e0} e^2)^{1/2} \text{ and } \lambda_{Di} = (k_B T_i / 4\pi n_{i0} e^2)^{1/2}$$

- -ve dust → what happen?
- +ve dust → what happen?
- Dust plasma frequency

$$\omega_{pd} = (4\pi n_{d0} Z_d^2 e^2 / m_d)^{1/2}$$

# Properties of dusty plasma

- Dust-in-plasma & Dusty plasma → G.W.
- Intergrain distance & Debye length
- Intergrain distance > Debye length → ??
- Intergrain distance < Debye length → ??

# Properties of dusty plasma

- Dust-in-plasma & Dusty plasma → G.W.
- Intergrain distance & Debye length
- Intergrain distance > Debye length → Dust-in-plasma
- Intergrain distance < Debye length → Dusty plasma

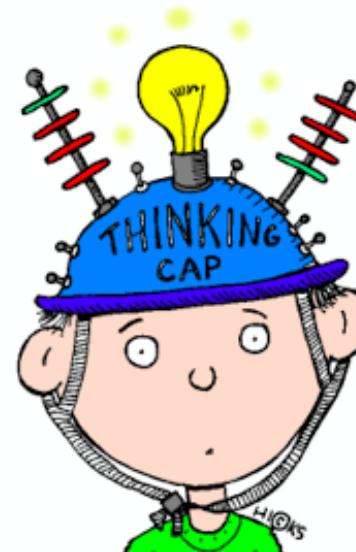
# Properties of dusty plasma

$Z_d \approx 10^3$ ,  $m_d \approx 2 \times 10^{-12}$  g,  $n_{d0} \approx 10^{-9}$  cm $^{-3}$

$T_e \approx 5 - 22$  eV,  $T_i \approx 60 - 120$  eV,  $n_{e0} \approx 1 - 23 \times 10^3$  cm $^{-3}$

## Calculate

- Debye length
- Dust frequency
- Intergrain distance
- Type of plasma (dust-in-plasma or dusty plasma)



# Outline

- Types of plasma
- Occurance of dusty plasma
- Properties of dusty plasma
- Two milestones in dusty plasma
- Mach cones
- Wakefield

# Two milestones in dusty plasma

- **Dust Coulomb crystal (IKEZI 1986)**

First prediction by H. Ikezi, Phys. Fluids 29, 1764 (1986);  
Observations: Chu & Lin I, PRL 72, 4009 (1994); Physica A, 205, 183 (1994); Thomas et al, PRL 73, 653 (1994).

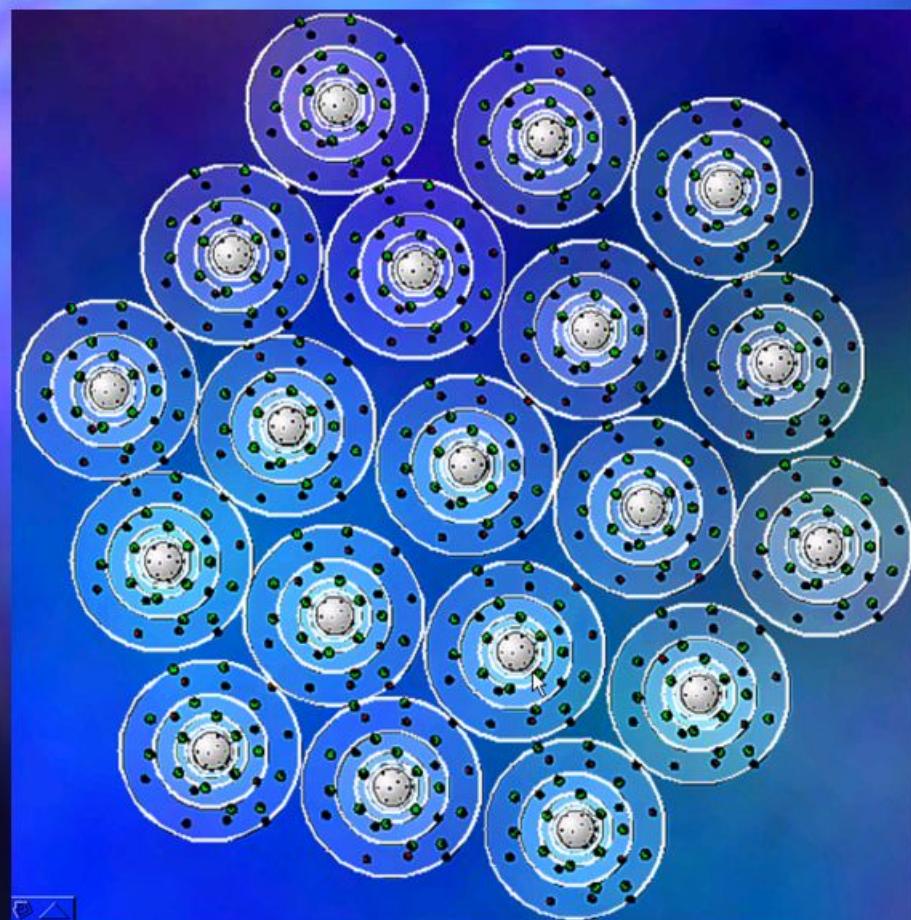
- **Dust-acoustic waves (SHUKLA 1989; RAO, SHUKLA & YU 1990)**

First prediction: P. K. Shukla, Proc. 1st Capri Workshop on Dusty Plasmas, pp. 38–39, 28 May – 2 June 1989. N. N. Rao, P. K. Shukla, and M. Y. Yu, Planet. Space. Sci 38, 543 (1990).  
Observation: J. Chu, J.-B. Du, Lin I, J. Phys. A: Appl. Phys. 27, 296 (1994); A. Barkan, R. L. Merlino, and N. D’Angelo, Phys. Plasmas 2 3563 (1995).

# Two milestones in dusty plasma

## Dust Coulomb crystal

**Plasma crystallisation**



$\lambda_i \approx 50 \mu m \ll \lambda_e \approx \Delta$

**Phase diagram depends on:**

- a) Coulomb coupling parameter for interacting particles:  
 $\Gamma = Q^2 / 4\pi\epsilon_0 \Delta k_B T$   
Coulomb energy/Thermal energy  
 $\Gamma < 1$ : system is weakly coupled (common)  
 $\Gamma > 1$ : system is strongly coupled (uncommon)
- b) Lattice parameter:  
 $\kappa \leq \Delta/\lambda_D$   
( $\Delta$ : particle distance,  $\lambda_D$ : Debye length)

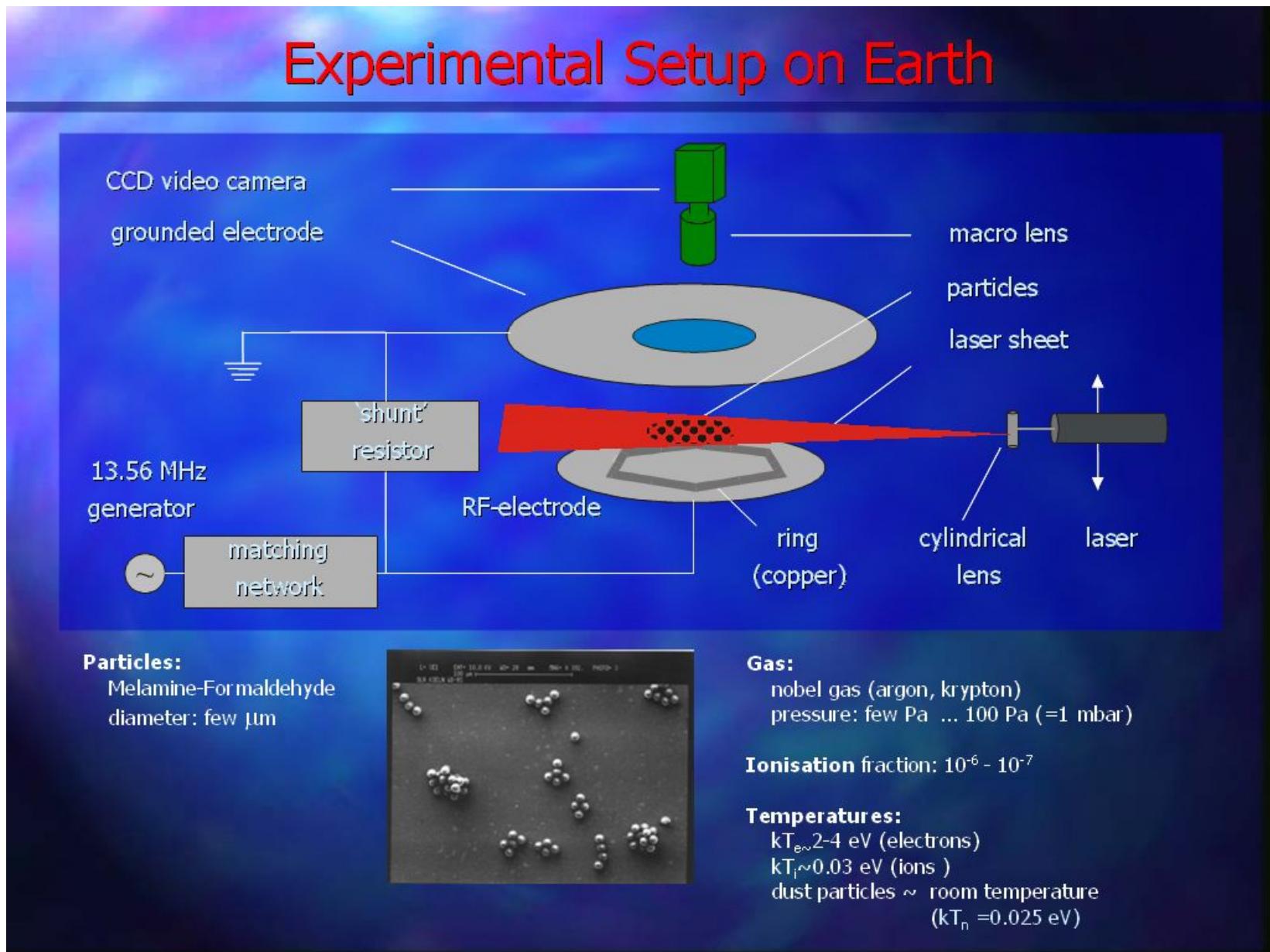
$\Gamma \gg 1$  and  $\kappa \sim 1$

⇒ plasma crystal

$\Gamma = 172$  for one component,  
pure Coulomb interaction

# Two milestones in dusty plasma

## Dust Coulomb crystal



# Two milestones in dusty plasma

## Dust Coulomb crystal

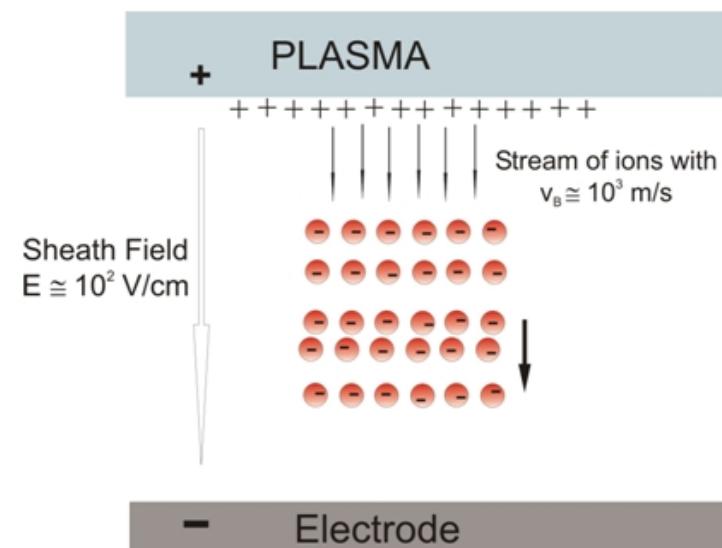
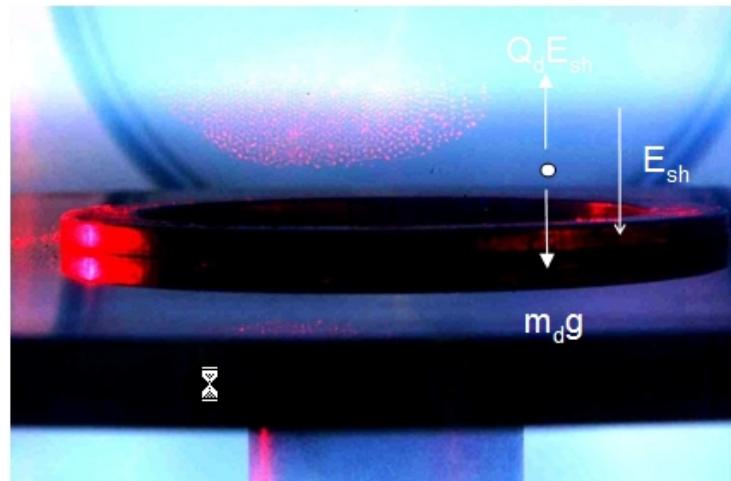
### Crystals in RF plasma sheath

- RF frequency  $f=13.56$  MHz

$$V_{\text{electrode}} = V_{\text{dc}} + V_{\text{rf}} \sin(2\pi f t)$$

(self-bias  $\approx -10 \dots -100$  V)      (p-p  $\sim 50-200$  V)

- Dust has inertia  $\rightarrow$  in equilibrium  $Q_d E_{\text{sh}} = m_d g$  ( $E_{\text{sh}}$  is time averaged sheath field)



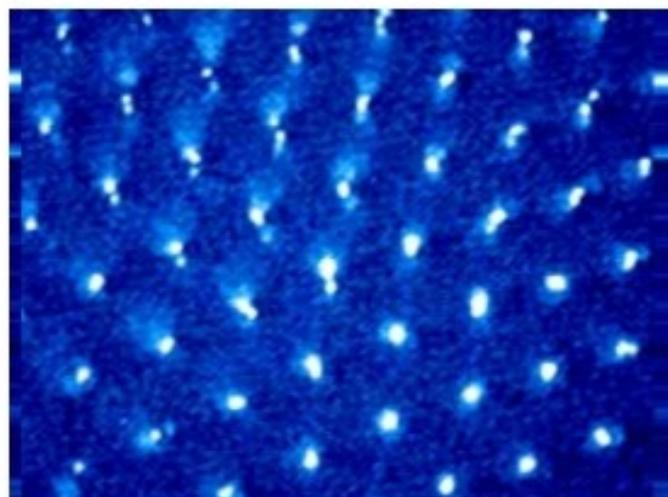
# Two milestones in dusty plasma

## Dust Coulomb crystal

### 微粒電漿晶格

微粒的大量負電荷造成強大靜電交互作用力  
自動排列成晶格或液體結構，懸浮於背景電漿中

1993  
春季



首度實驗室觀測/ 博士班學  
生朱仁宏的研究成果

J.H.Chu and Lin I, PRL(1994) Lin I  
et al, Science (1996)

數百微米微粒間距，提供一可以透過數位光學顯微技術直接觀  
測與追蹤粒子軌跡的平台

# Two milestones in dusty plasma

## Dust Coulomb crystal

- Two particles
- Three particles
- Disorder phase
- Flow phase
- Crystalline phase

# Two milestones in dusty plasma

## Dust Coulomb crystal

Solid State Crystals	Dust Crystals
$Z_i > 1$	$Z_d \sim 10^3\text{--}10^5$
$\mathcal{E}_{\text{interaction}}$ a few eV	$\mathcal{E}_{\text{interaction}} \geq 900 \text{ eV}$
Lattice Spacing $L \sim 0.1 \text{ nm}$	$L \sim 1 \text{ mm}$

# Two milestones in dusty plasma

## Dust acoustic waves

- Padma K. Shukla and his collaborators predicted the existence of dust acoustic waves, dust ion acoustic waves and shocks....etc.
- His interest:
  - (1) Physics of low- and high-temperature plasma
  - (2) Nonlinear quantum plasma physics
  - (3) Nonlinear space and astroplasmas
  - (4) Nonlinear processes in geophysical flows
  - (5) Collective interactions in dusty plasmas
  - (6) Laser-plasma interactions
  - (7) Plasma high-energy charged particle accel.
  - (8) Nonlinear photonics/optics



**Padma Kant Shukla**  
1950 – 2013 (India-Germany)  
Member of The Royal Swedish  
Academy of Science

# Two milestones in dusty plasma

## Dust acoustic waves

	<b>Restoring Forces</b>	<b>Inertia</b>	<b>Phase Speed</b>
<b>SW</b>	Neutral Gas Pressure	Mass of Neutral Atoms	$(T_n/m_n)^{1/2}$
<b>IAW</b>	Electron Pressure	Ion Mass	$C_s = (T_e/m_i)^{1/2}$
<b>DIAW</b>	Electron Pressure	Ion Mass	$(n_{i0}/n_{e0})^{1/2}C_s$
<b>DAW</b>	Ion Pressure Electron Pressure	Dust Mass Dust Mass	$Z_d(n_{d0}T_i/n_{i0}m_d)^{1/2}$ $Z_d(n_{d0}T_e/n_{e0}m_d)^{1/2}$
<b>AW</b>	Magnetic Tension	Ion Mass	$(B_0^2/8\pi n_{i0}m_i)^{1/2}$
<b>DALW</b>	Magnetic Tension	Dust Mass	$(B_0^2/8\pi n_{i0}m_d)^{1/2}$

# Two milestones in dusty plasma

## Dust acoustic waves

*Planet. Space Sci.*, Vol. 38, No. 4, pp. 543–546, 1990

Printed in Great Britain.

## DUST-ACOUSTIC WAVES IN DUSTY PLASMAS

**N. N. RAO,\* P. K. SHUKLA and M. Y. YU**

*Physica Scripta*. Vol. 45, 508, 1992.

## Dust Ion-Acoustic Wave

**P. K. Shukla\* and V. P. Silin†**

# Two milestones in dusty plasma

## Dust acoustic waves

- Xu et al. 1992 → modify the Q-machine to allow the dispersal of dust grains over a portion of the cylindrical plasma column
- Chu et al. 1994 → for the first time a dusty plasma has been confined in a cylindrical symmetric rf plasma system

# Coulomb solids and low-frequency fluctuations in RF dusty plasmas

J H Chu, Ji-Bin Du and Lin I

Department of Physics, National Central University, Chungli, Taiwan 32054,  
Republic of China

Received 23 April 1993, in final form 4 August 1993

**Phys. Plasmas 2 (10), October 1995**

**Laboratory observation of the dust-acoustic wave mode**

A. Barkan, R. L. Merlino, and N. D'Angelo

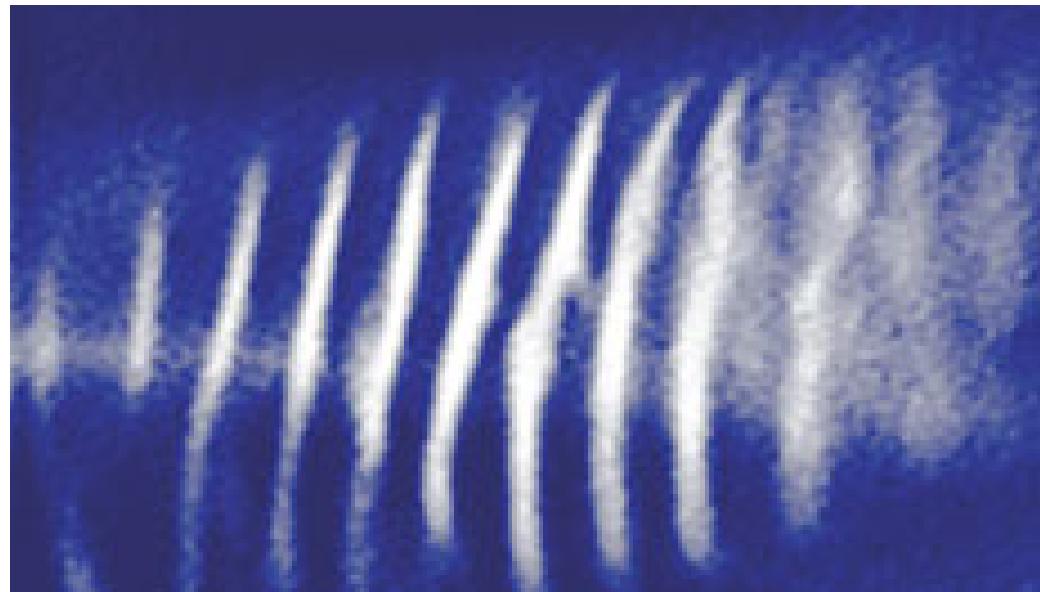
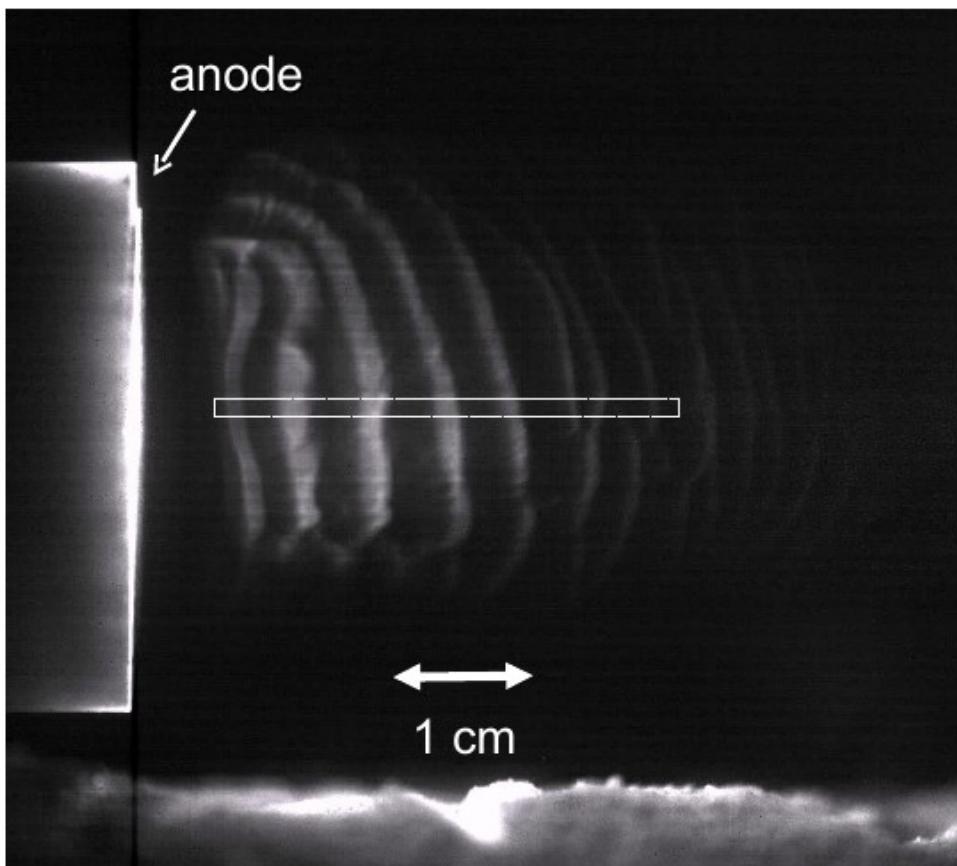
*Planet. Space Sci.*, Vol. 44, No. 3, pp. 239–242, 1996

**Experiments on ion-acoustic waves in dusty plasmas**

A. Barkan, N. D'Angelo and R. L. Merlino

# Two milestones in dusty plasma

## Dust acoustic waves



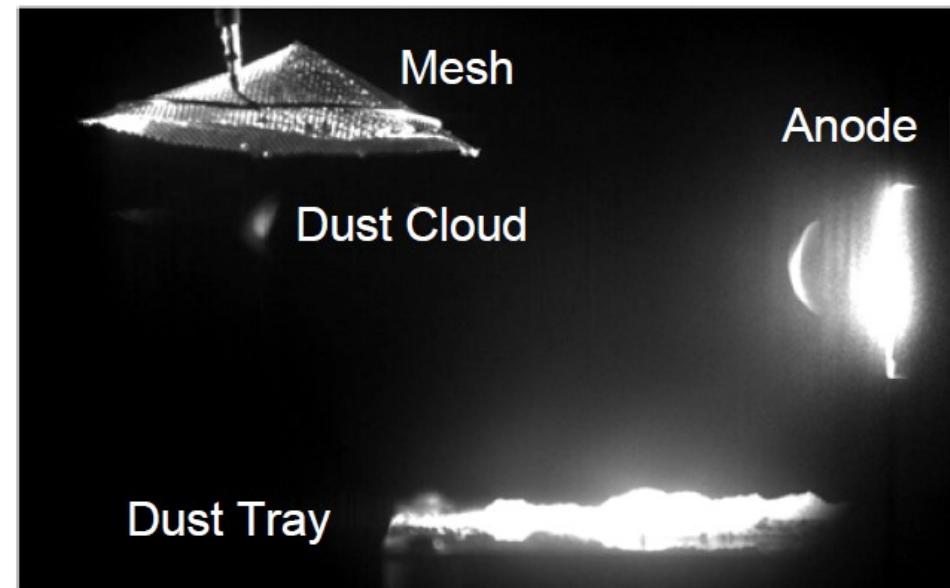
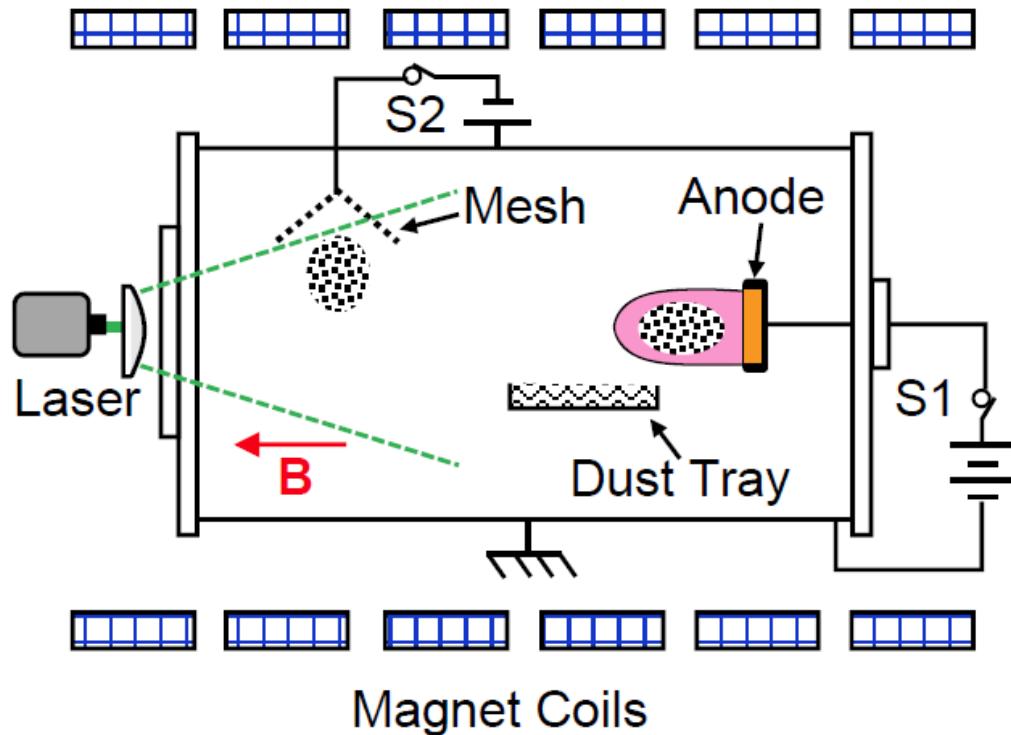
Movies 1 & 2 & 3

# Two milestones in dusty plasma

## Dust acoustic waves

Theory	Observation
$v_{ph} = Z_d \left( \frac{T_i n_d}{m_d n_i} \right)^{1/2} = 8 \text{ cm/s}$ $(\lambda = 0.5 \text{ cm}, f = 15 \text{ Hz})$	$v_{ph} = 9 \text{ cm/s}$ $(\lambda = 0.6 \text{ cm}, f = 15 \text{ Hz})$

# Two milestones in dusty plasma



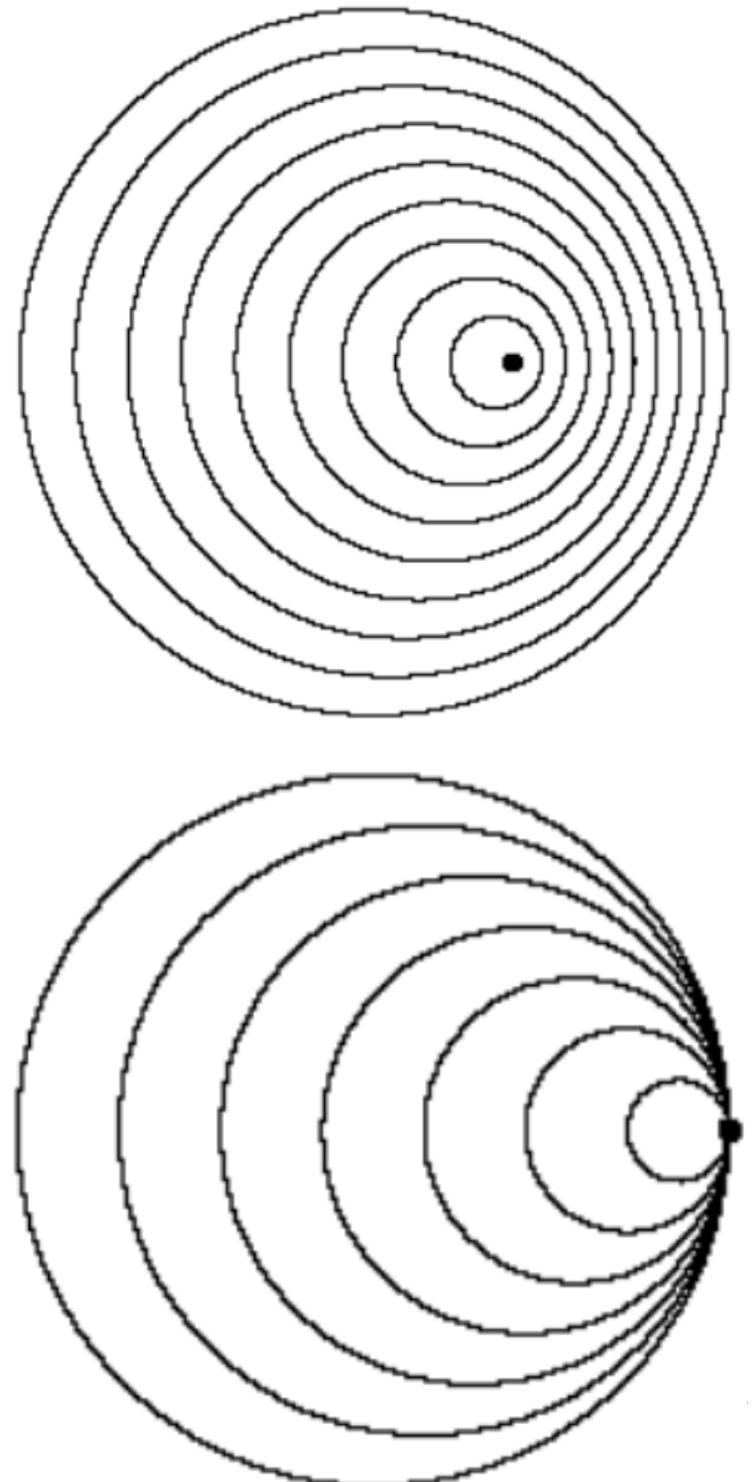
- DC glow discharge in argon at  $p \sim 0.1 - 0.2$  Torr
- 1 micron diameter spherical silica particles
- Conical mesh used to trap a secondary dust cloud

# Outline

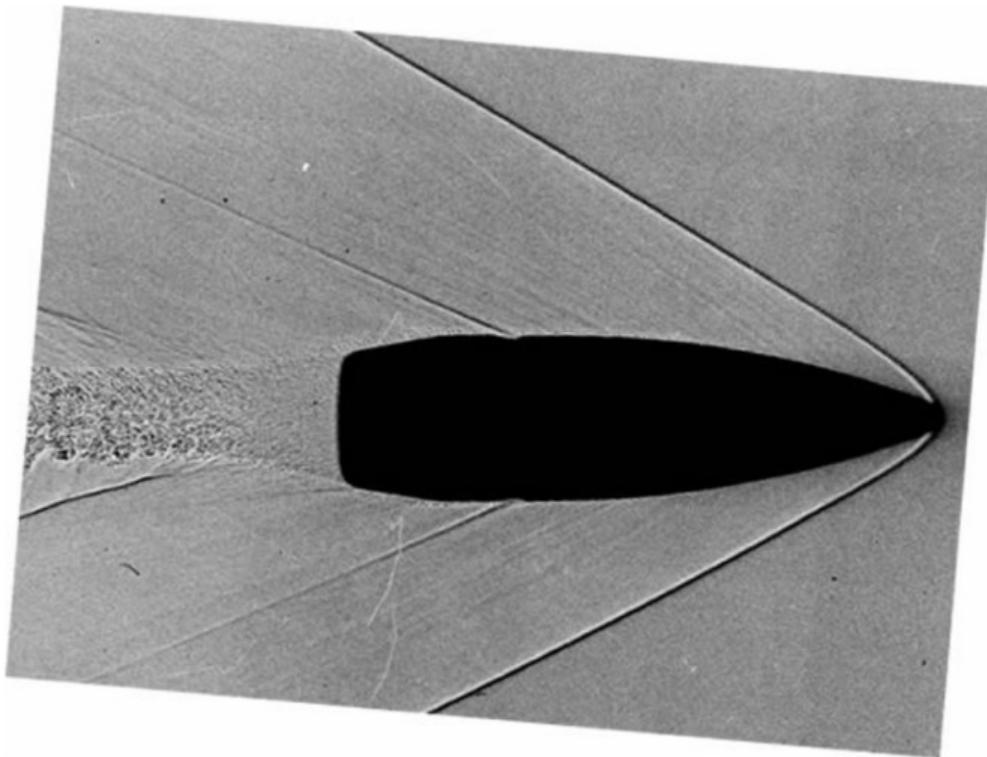
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- **Mach cones**
- Wakefield

# Mach Cones

- When an object moves through the air it pushes the air in front of it away, creating a pressure wave.
- This pressure wave travels away from the object at the speed of sound.
- If the object itself is travelling at the speed of sound then these pressure waves build up on top of each other to create a shock wave



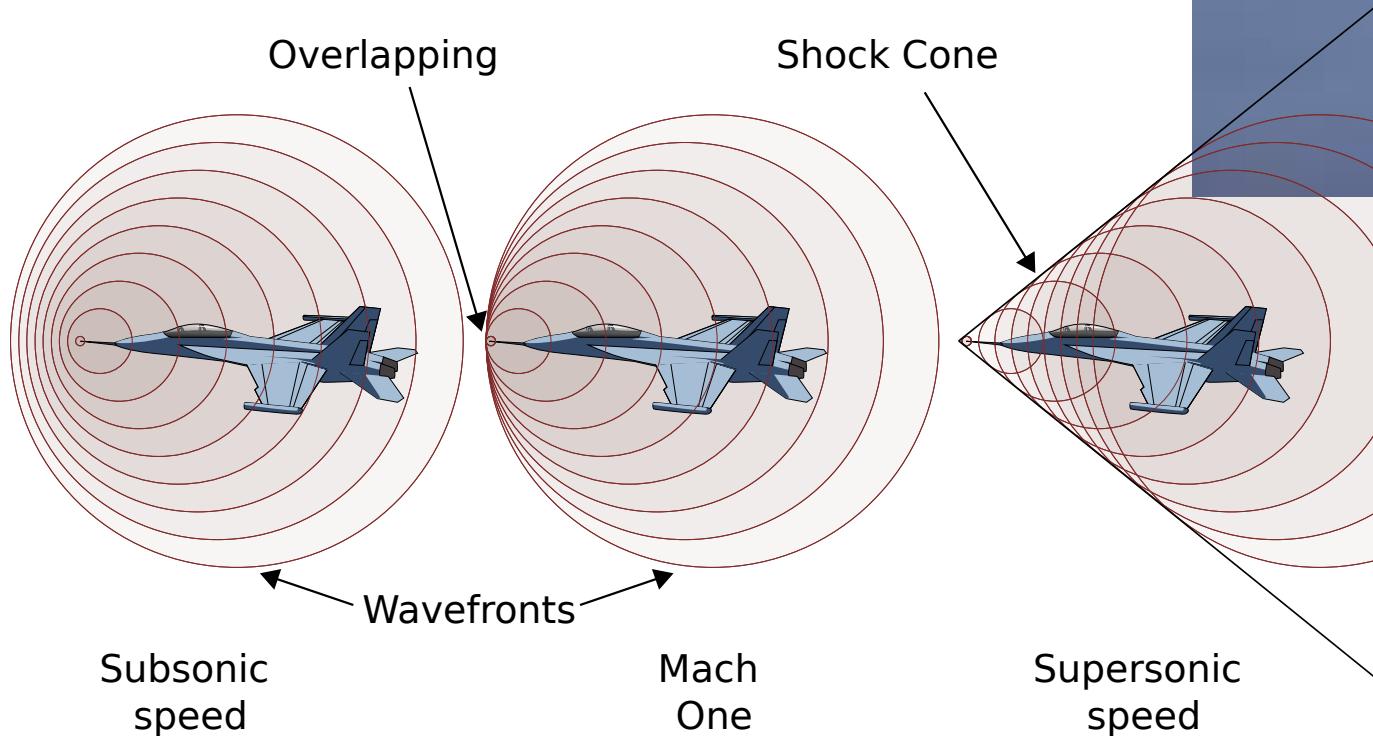
# Mach Cones, cont.



In the photograph above the Mach cone angle is  $28^\circ$  and therefore the bullet must have been travelling at Mach 2.1 or 720 metres per second (assuming the speed of sound is 340 m/s).

# Mach Cones, cont.

Movie 1



# Mach Cones, cont.

- Havnes et al (1995, 1996) theoretically predicted the existence of super DA Mach cones in dusty plasmas that are relevant to planetary rings and interstellar space.

# Mach Cones, cont.

VOLUME 83, NUMBER 18

PHYSICAL REVIEW LETTERS

1 NOVEMBER 1999

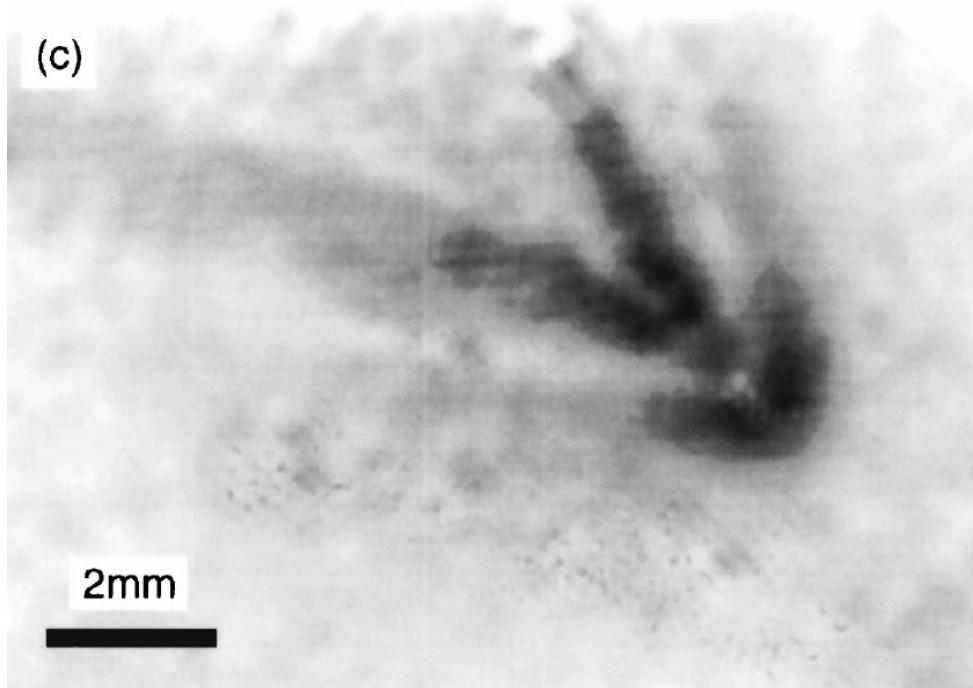
## Mach Cones in a Coulomb Lattice and a Dusty Plasma

D. Samsonov, J. Goree,\* Z. W. Ma, and A. Bhattacharjee

*Department of Physics and Astronomy, The University of Iowa, Iowa City, Iowa 52242*

H. M. Thomas and G. E. Morfill

*Max Planck Institut für extraterrestrische Physik, 85740 Garching, Germany*



# Mach Cones, cont.

PHYSICAL REVIEW E

VOLUME 61, NUMBER 5

MAY 2000

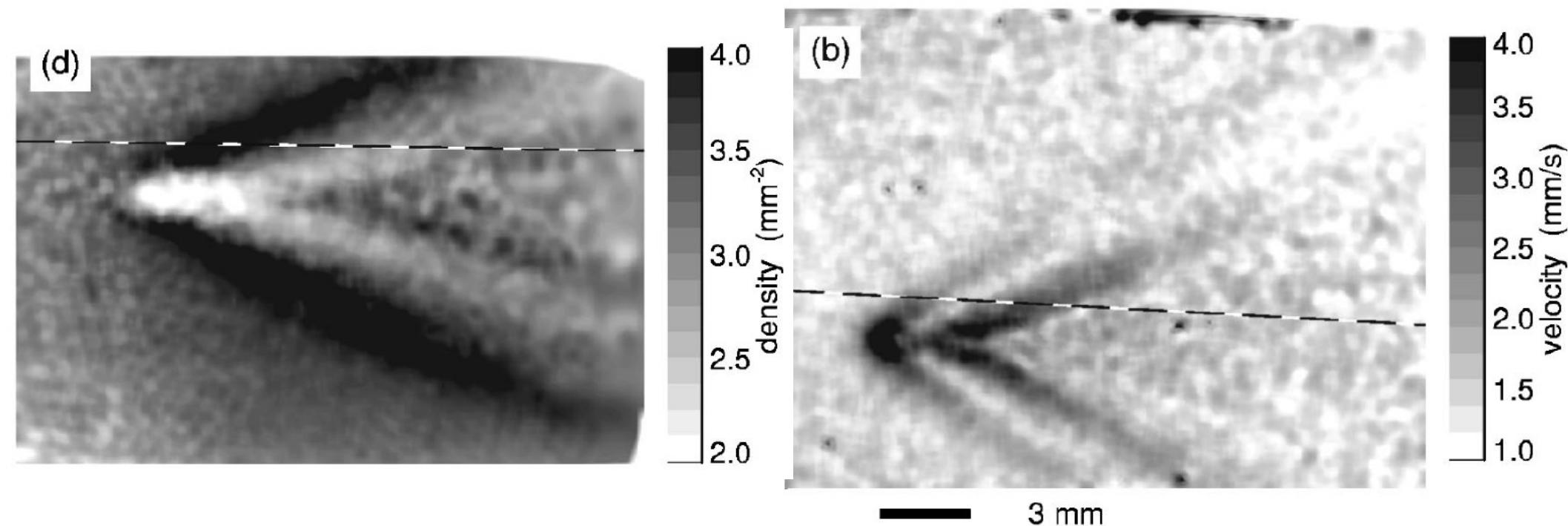
## Mach cone shocks in a two-dimensional Yukawa solid using a complex plasma

D. Samsonov\* and J. Goree<sup>†</sup>

*Department of Physics and Astronomy, The University of Iowa, Iowa City, Iowa 52242*

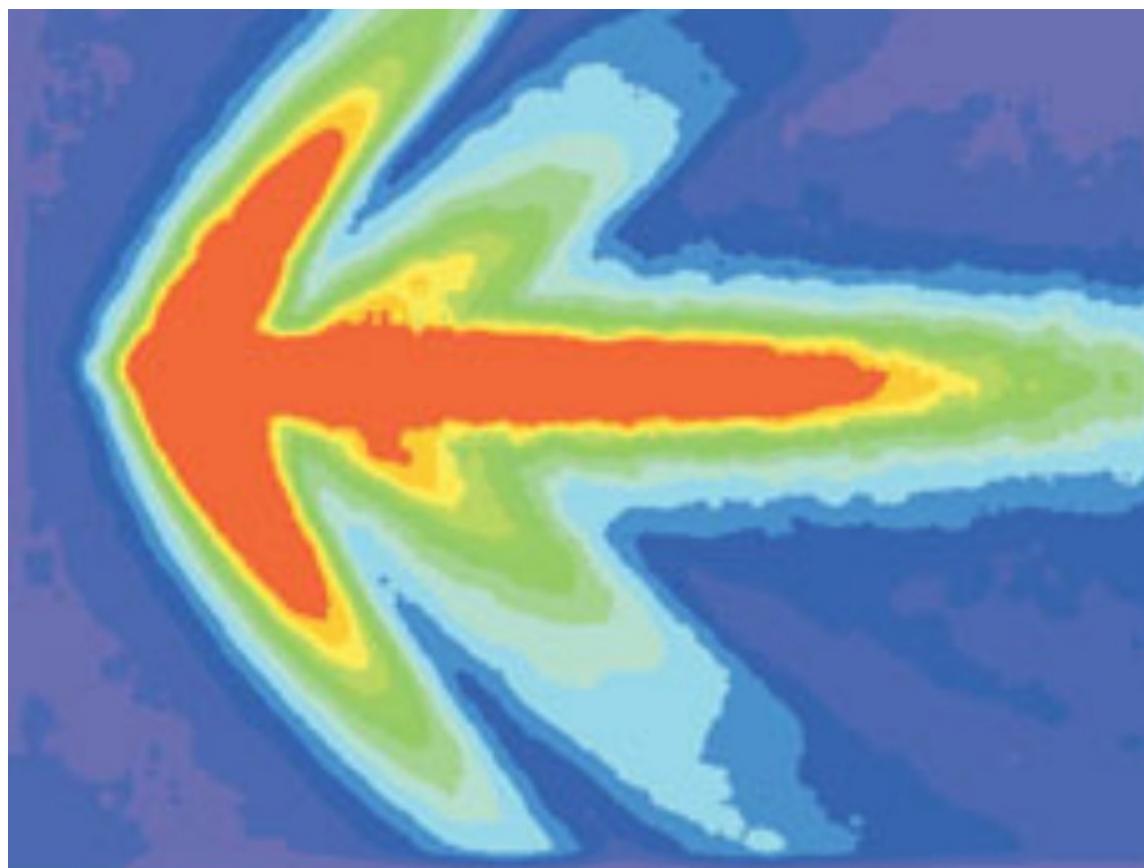
H. M. Thomas and G. E. Morfill

*Max-Planck-Institut für Extraterrestrische Physik, Giessenbachstrasse, 85740 Garching, Germany*



# Mach Cones, cont.

- Mach cones in dusty crystal
- Movie [1](#)

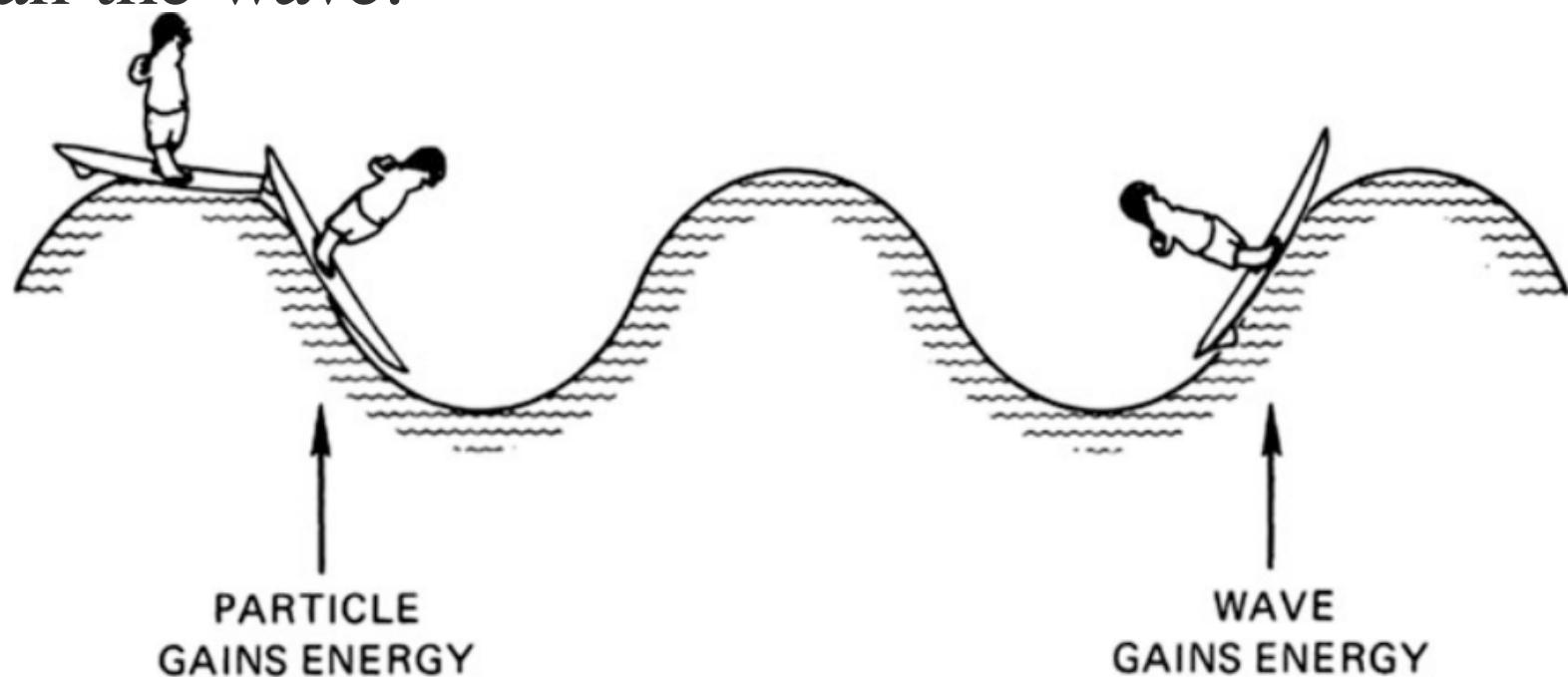


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# Wakefield

- In 1979 John Dawson, in a paper with T. Tajima, proposed that Landau damping effect could be used to accelerate particles
- In plasma, there are electrons both faster and slower than the wave.

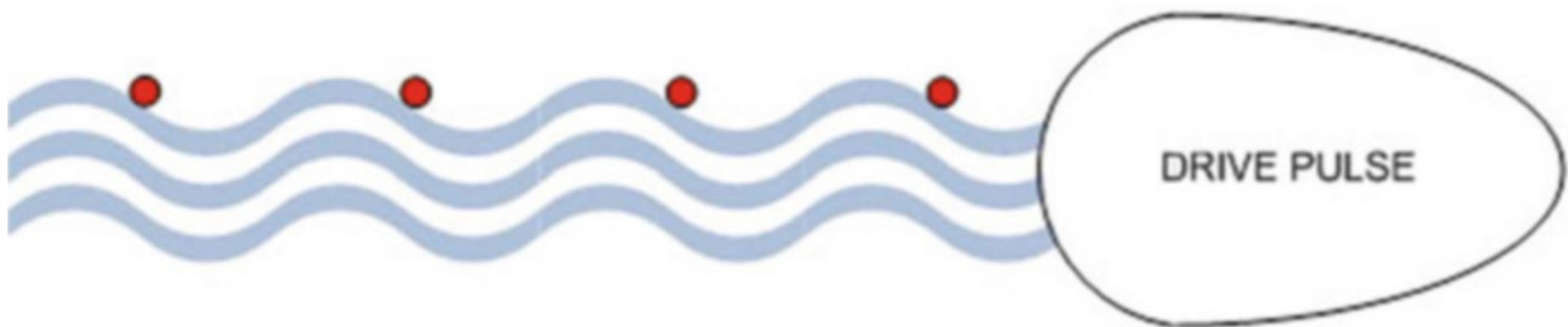


# Wakefield, cont.



# Wakefield, cont.

- There were two early ideas on plasma accelerators: *beatwave* and *wakefield*.



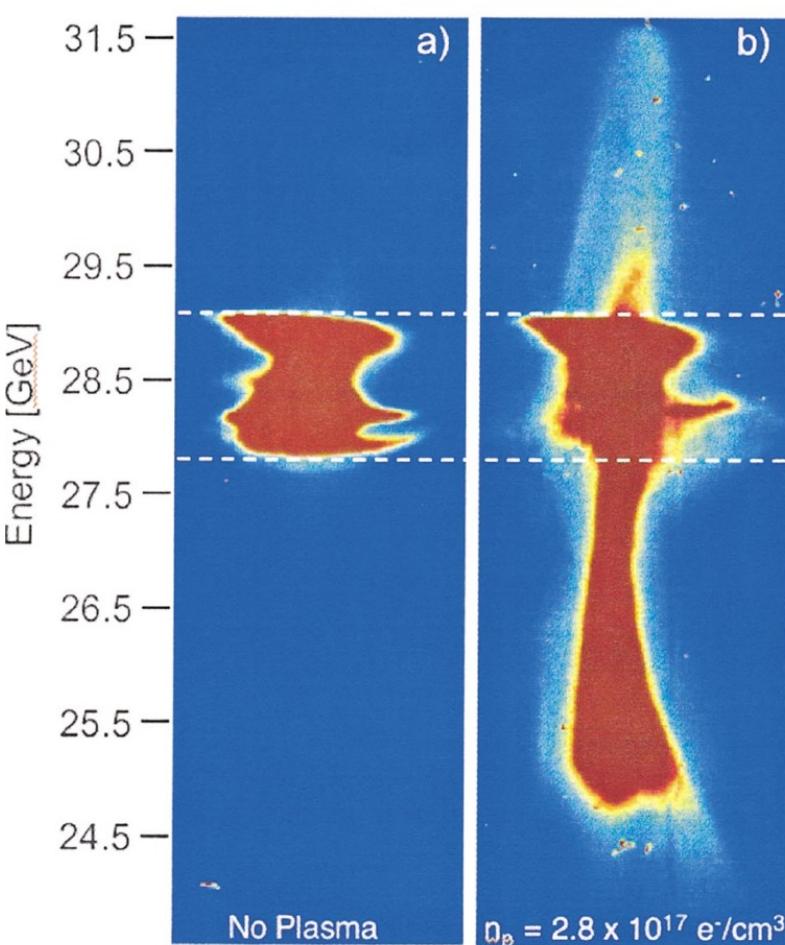
# Wakefield, cont.

PRL 95, 054802 (2005)

PHYSICAL REVIEW LETTERS

week ending  
29 JULY 2005

## Multi-GeV Energy Gain in a Plasma-Wakefield Accelerator



J. Decker,<sup>1</sup> S. Deng,<sup>3</sup> P. Emma,<sup>1</sup> C. Huang,<sup>2</sup> R. H. Iverson,<sup>1</sup> D. K. Johnson,<sup>2</sup> Lu,<sup>2</sup> K. A. Marsh,<sup>2</sup> W. B. Mori,<sup>2</sup> P. Muggli,<sup>3</sup> C. L. O'Connell,<sup>1</sup> E. Oz,<sup>3</sup> R. H. Siemann,<sup>1</sup> and D. Walz<sup>1</sup>

a) No Plasma → Only electron beam with 1 GeV energy.

b) 10 cm long lithium plasma → the core of the electron bunch has lost energy driving the plasma wake while particles in the back of the bunch have been accelerated to 2.7 GeV

# Wakefield, cont.



# Wakefield, cont.

Phys. Fluids, Vol. 28, No. 7, July 1985

## Attractive potential between resonant electrons

M. Nambu and H. Akama

*College of General Education, Kyushu University, Ropponmatsu, Fukuoka 810, Japan*

Physics Letters A 203 (1995) 40–42

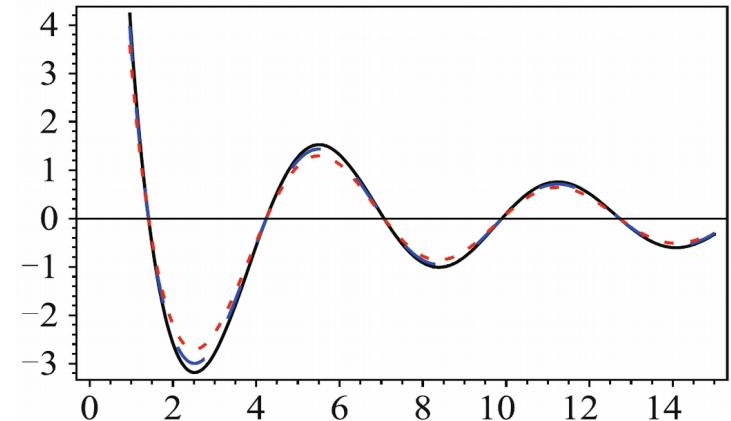
Attractive forces between charged particulates in plasmas

Mitsuhiko Nambu, Sergey V. Vladimirov <sup>1</sup>, Padma K. Shukla <sup>2</sup>

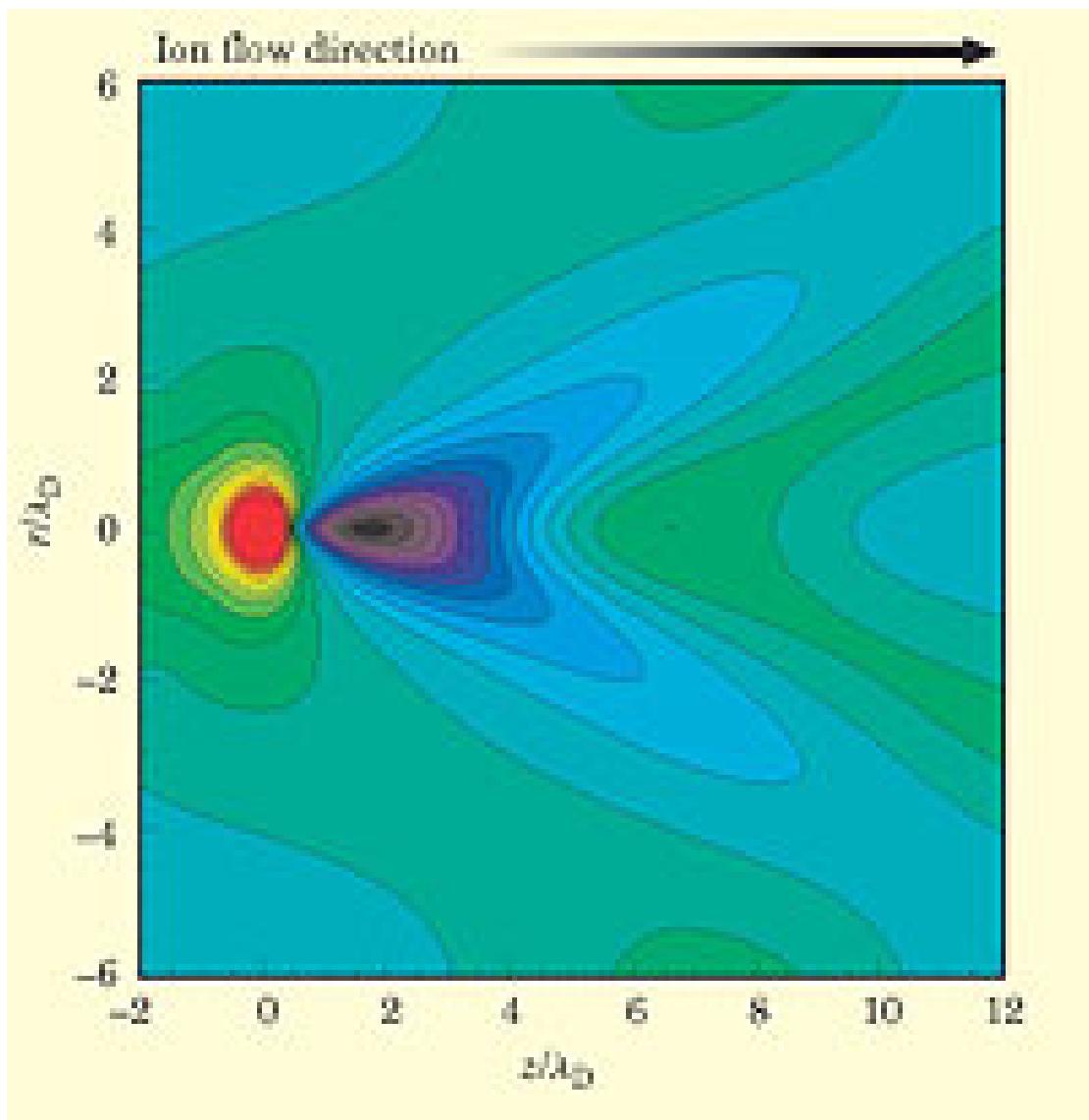
The charged particles having the same polarity can  
attract each other...!!

# Wakefield, cont.

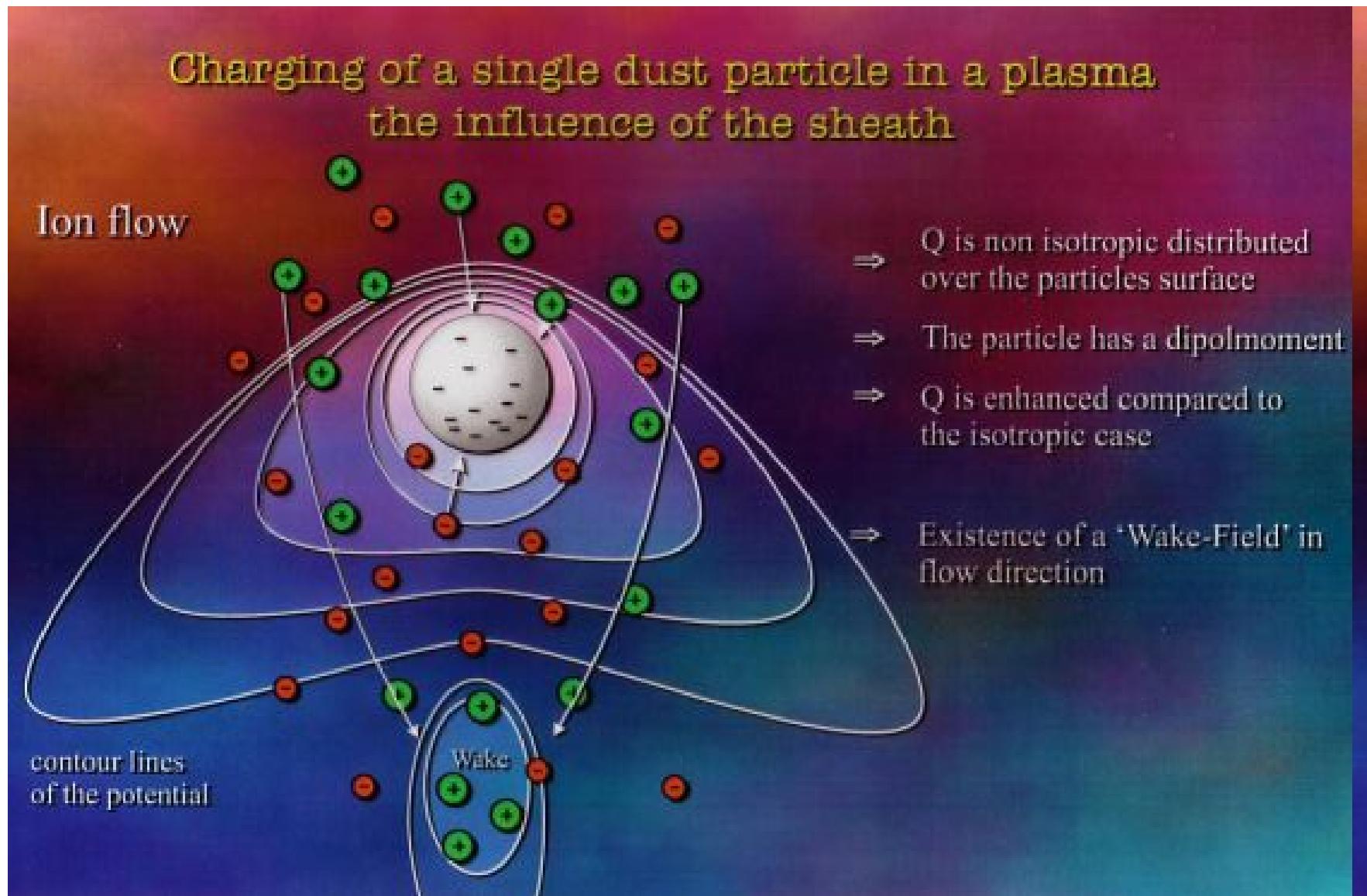
- $V_{ph} \sim C_s$
- Appearing long-range **oscillatory wakefield**
- The background **positive ions are trapped/focused** in the negative part of the oscillatory wake potential.
- The **negative charges are attracted** to each other as they are **glued by positive ions** in a linear chain
- Dust crystals



# Wakefield, cont.



# Wakefield, cont.



# سؤال هام

طائر يبلغ طوله سبعة عشر سنتيمتراً ويتميز  
بشكله المستدير، وجناحيه الطويلين مما يجعله  
قادراً على الطيران لمسافات طويلة وهو مكون  
من لونين الأبيض والبني.....

طائر يبلغ طوله سبعة عشر سنتيمتراً، ويتميز  
بشكله المستدير، وجناحيه الطويلين مما يجعله  
قادراً على الطيران لمسافات طويلة وهو مكون  
من لونين الأبيض والبني..... نامسلا





# Finally .....!!!!!!

