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# Technical Plasma

Prof. Dr. Mohammed Shihab

Plasma Technology



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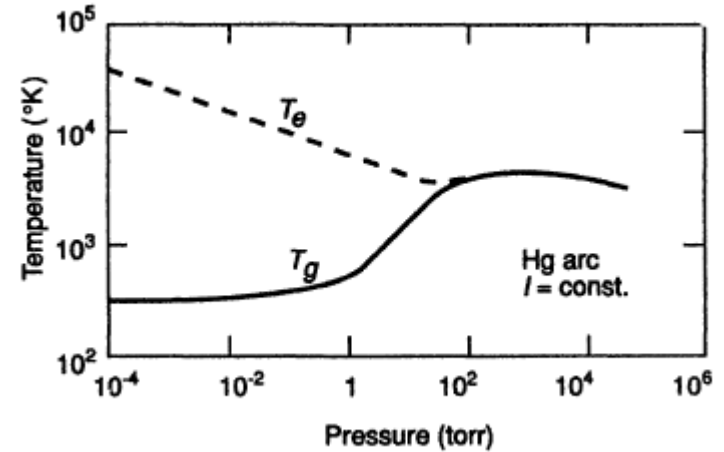
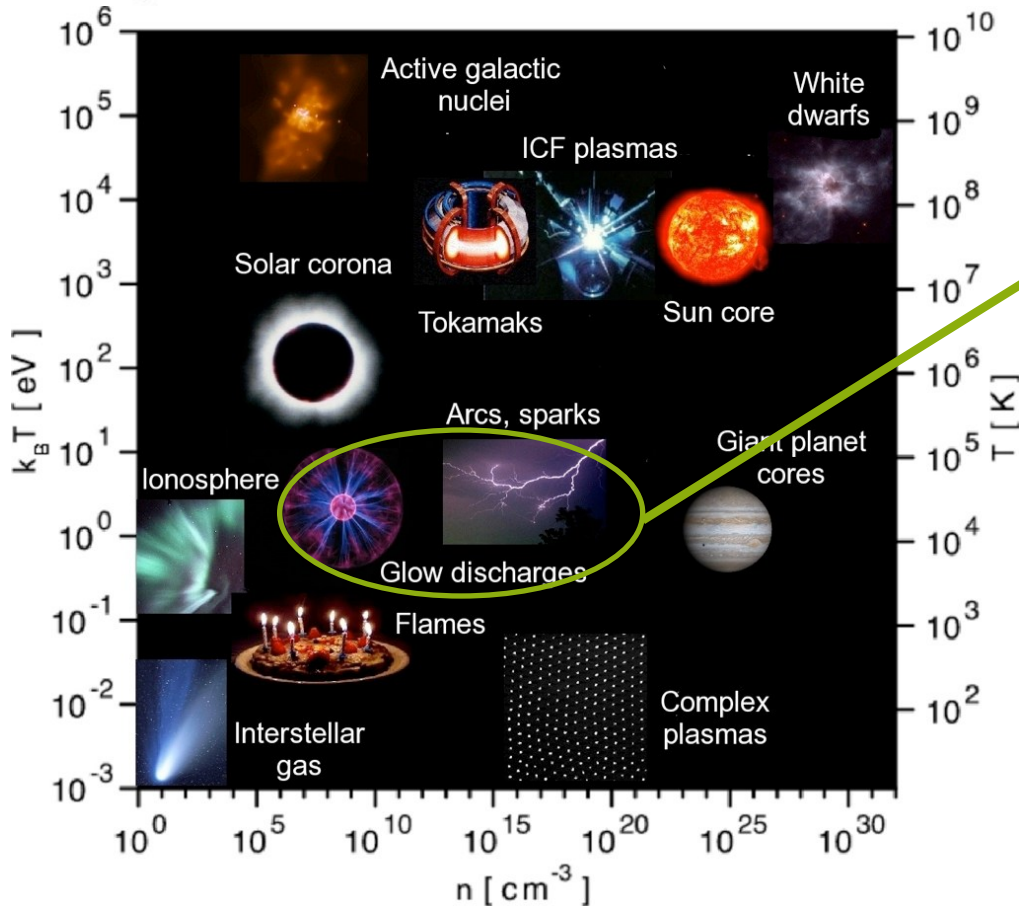


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# Low Temperature Plasma

- Low degree of ionization
- Neutral background  $10^6$  the ion and electron density
- Collisions with the background gas is dominant compared to electron ion collisions



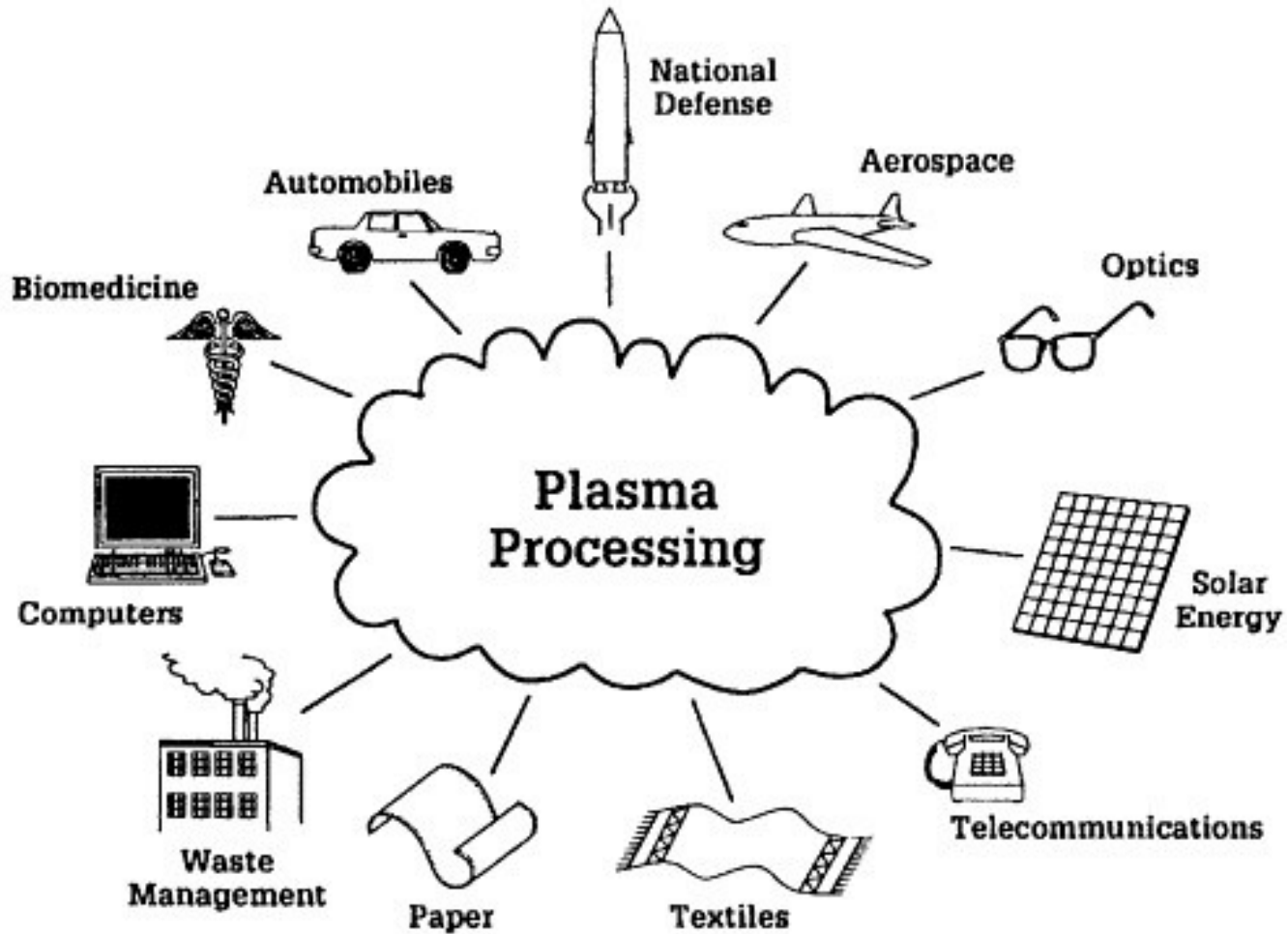
- Non-equilibrium plasmas at low pressures

$$T_e = 11000 - 60000K$$

$$T_e = 1 - 5eV \quad T_i = 300K$$

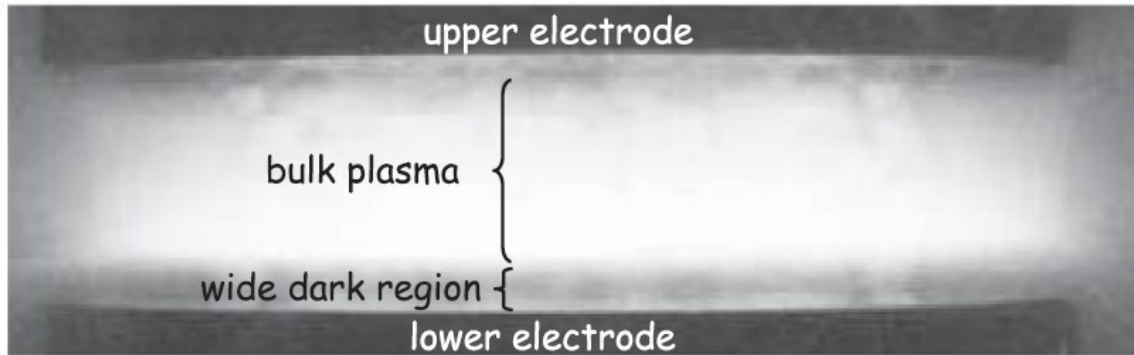
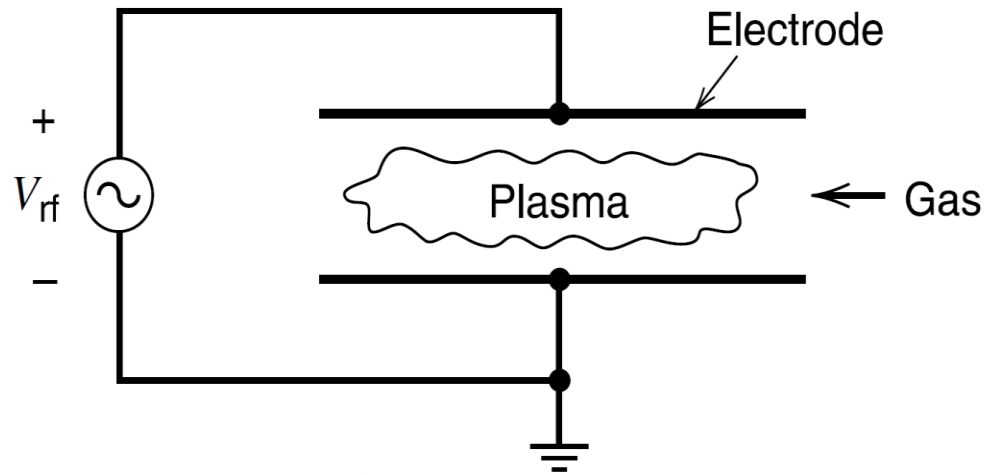


# Various applications





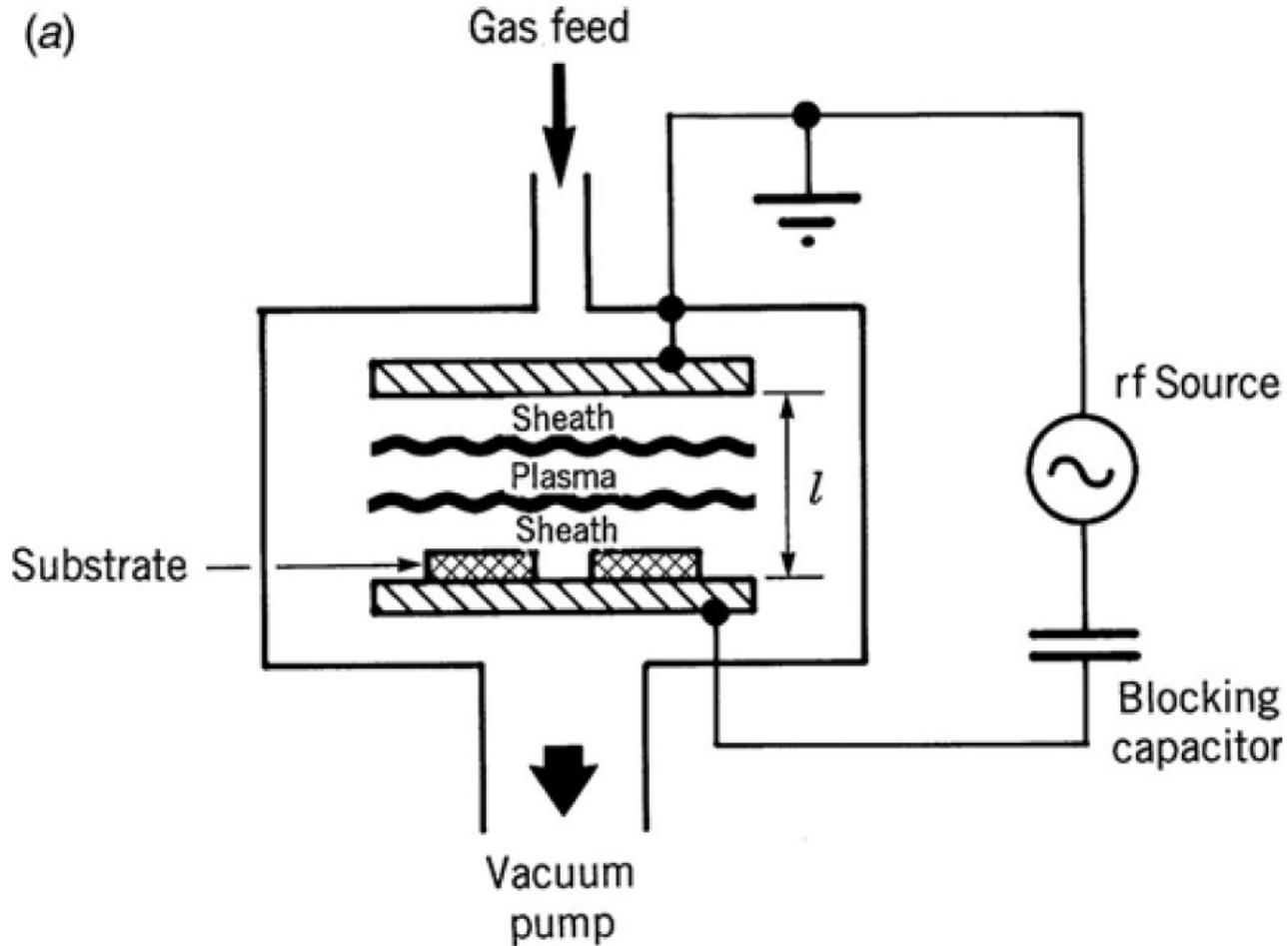
# Symmetric CCP discharge



- The ion flux and the ion energies increase (decreases) by increasing (decreasing) the driving frequency.



# CCPs & blocking a Capacitor





# Geometrically Asymmetric

- The RF current is constant.
- But the ground electrode Area is greater then the powered electrode area.

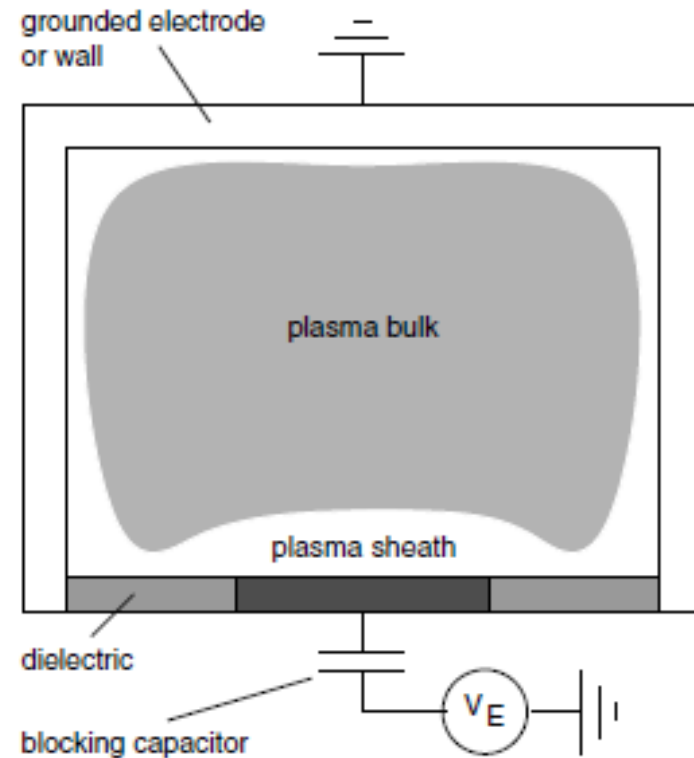
$$J_g = I_{rf} / A_g$$

$$J_p = I_{rf} / A_p$$

$$J_p \gg J_g$$

- The blocking capacitor blocks DC currents:

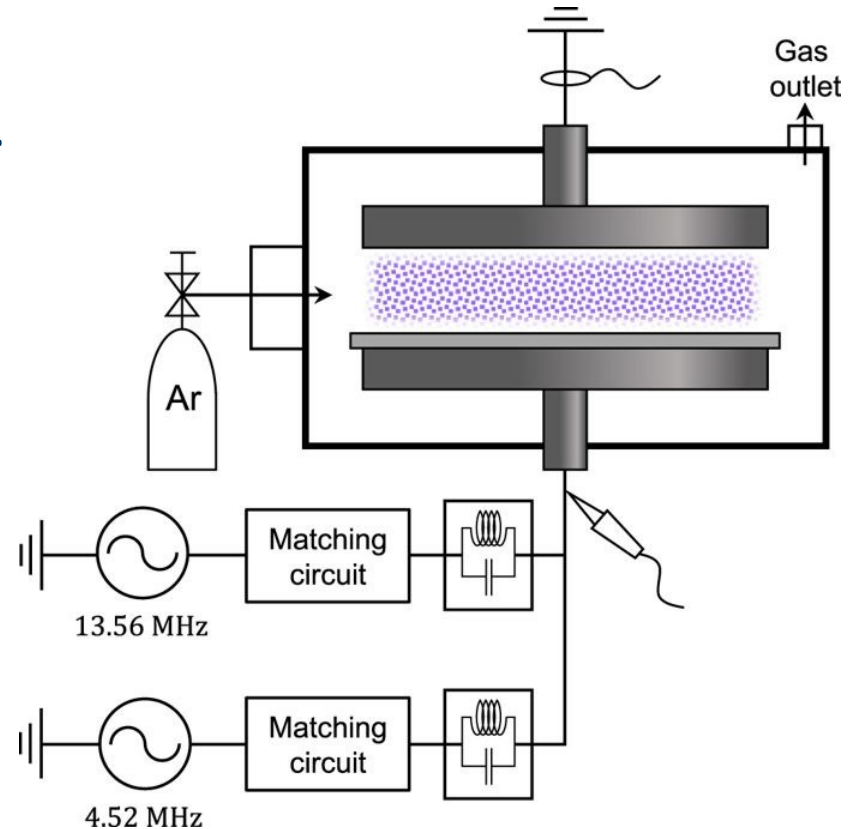
$$\frac{V_p}{V_g} = \left( \frac{A_g}{A_p} \right)^4$$





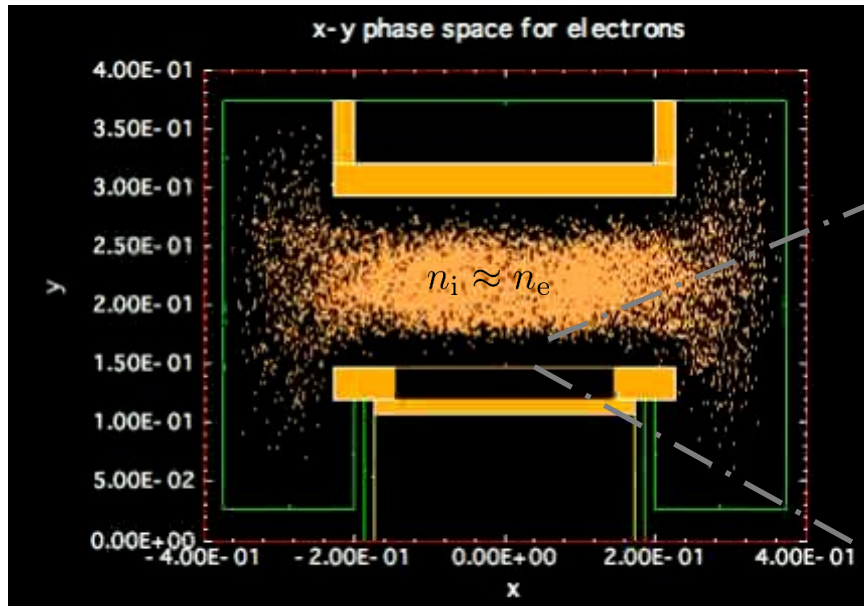
# Electrically Asymmetric

- The high frequency controls the ion plasma bulk (ion flux).
- The lower frequency controls the plasma sheath.
- The phase shift between the two sources controls also the sheath potential.
- The independent control is not always perfect.

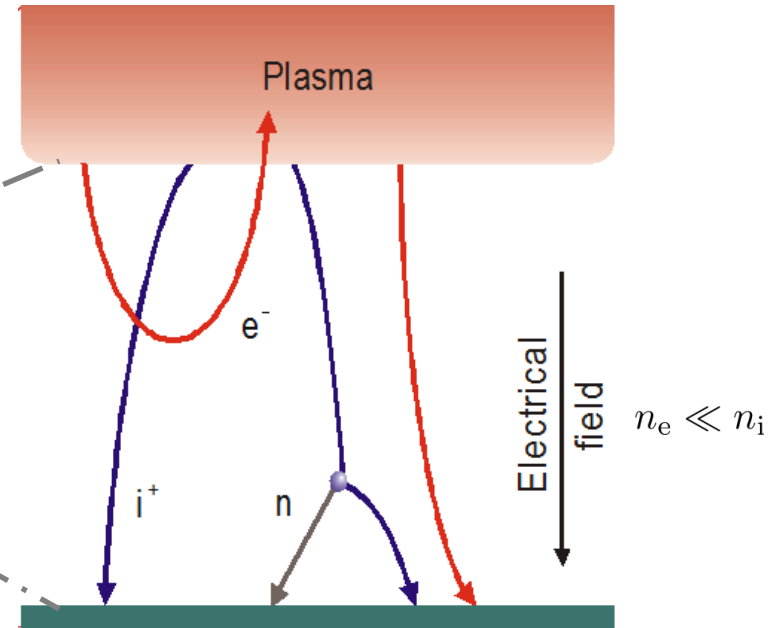




# Plasma Sheaths



TET



- RF sheaths:

- High frequency regime
- Intermediate frequency regime
- Low frequency regime

$$\omega_{RF} \gg \omega_{pi}$$

$$n_i(x) \Leftrightarrow \bar{E}(x)$$

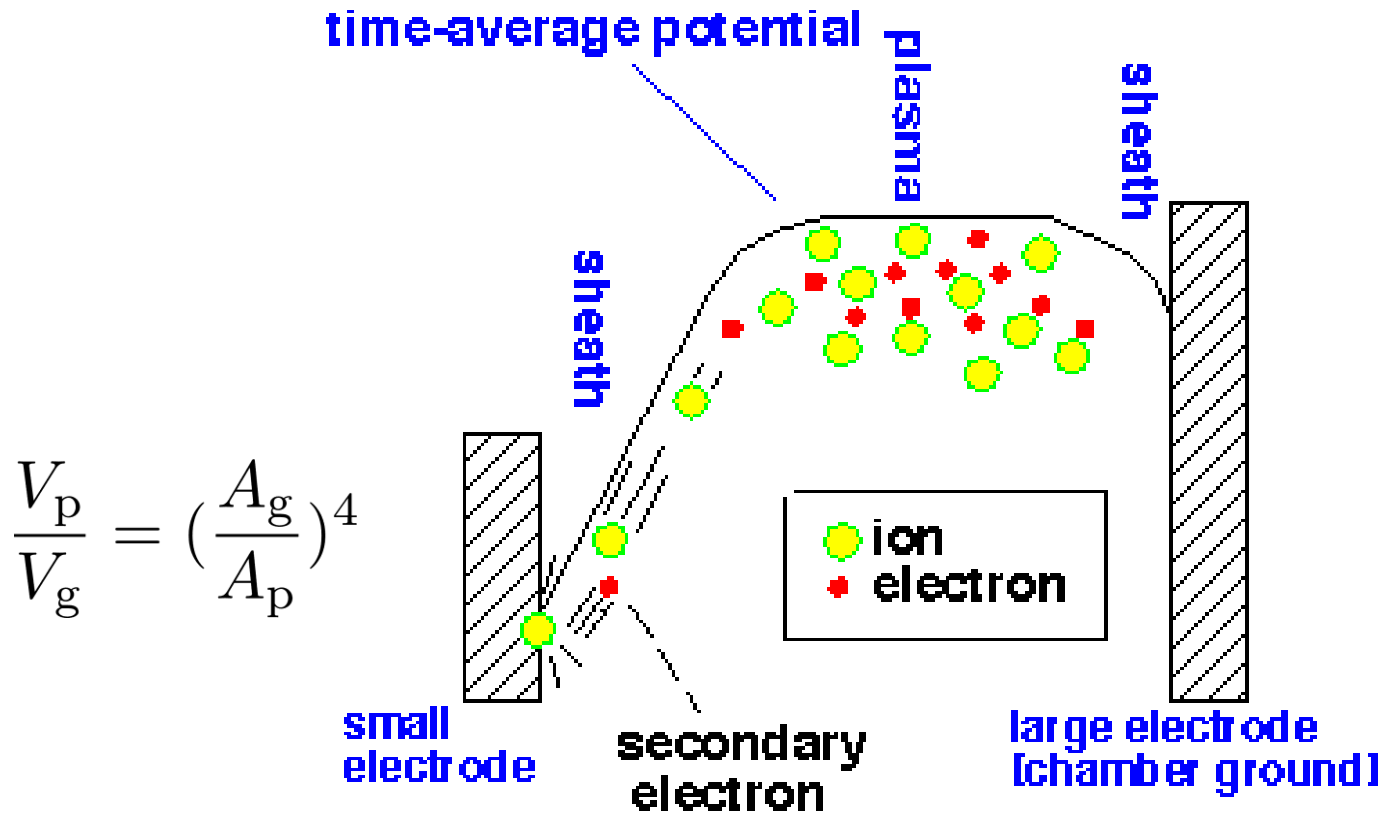
$$\omega_{RF} \approx \omega_{pi}$$

$$\omega_{RF} \ll \omega_{pi}$$

$$n_i(x, t) \Leftrightarrow E(x, t)$$

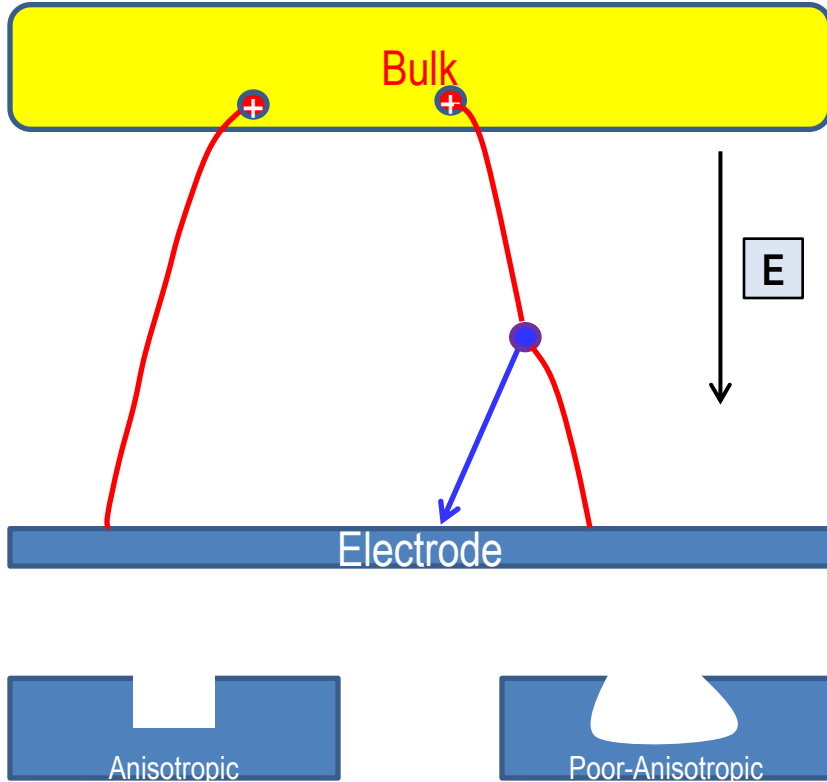


# Particle and Potential distribution





# Plasma Processing

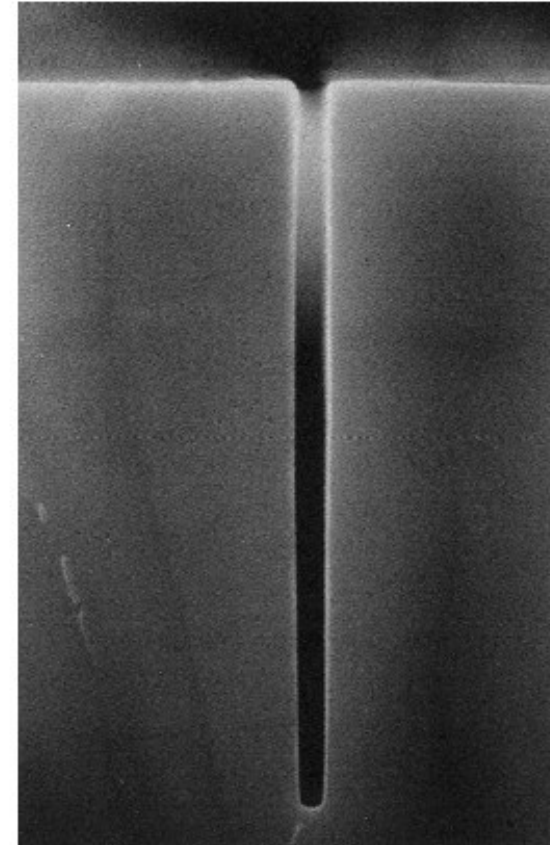


Intel



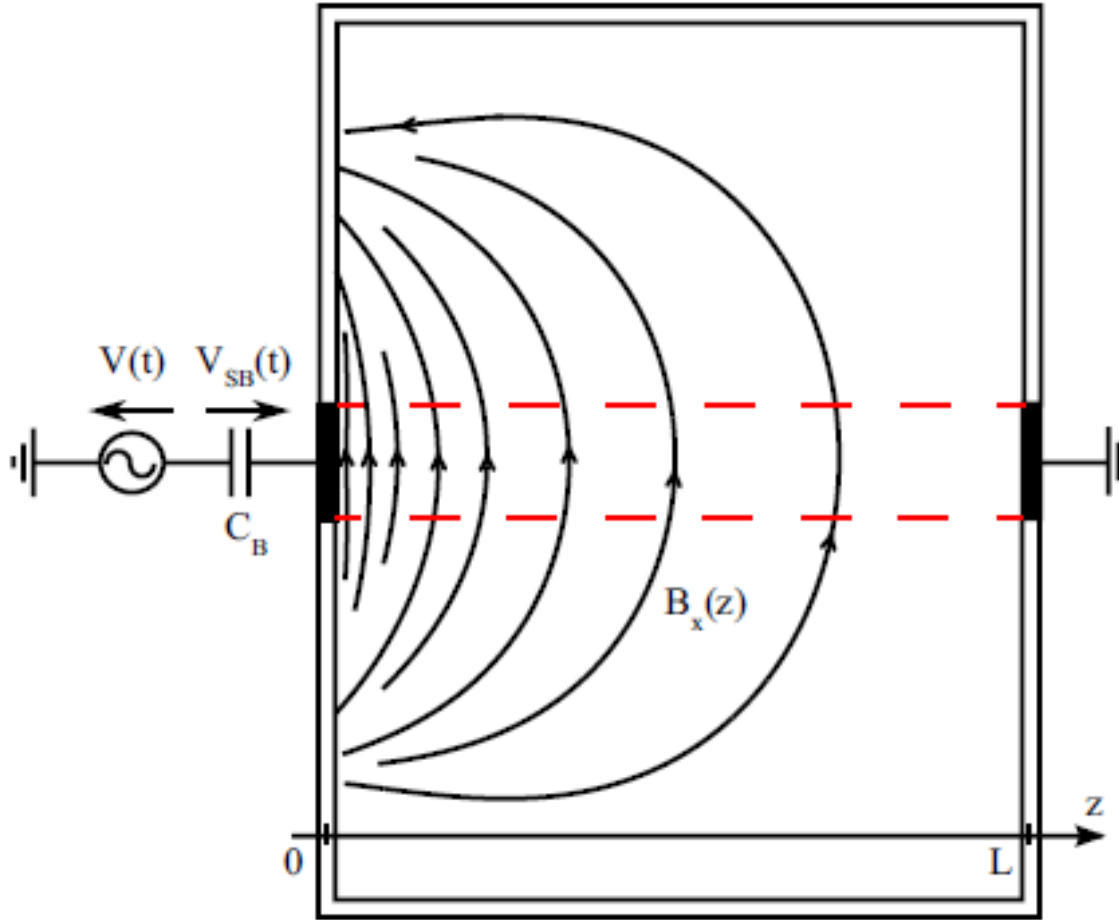
# Plasma Etching

- An etched profile with
  - 0.5 micrometer (500 Nanometer) wide
  - 4 micrometer (4000 nanometer)
- Such profiles are used for device isolation and charge storage capacitors.
- Human hair is 50-100 micrometer in diameter.

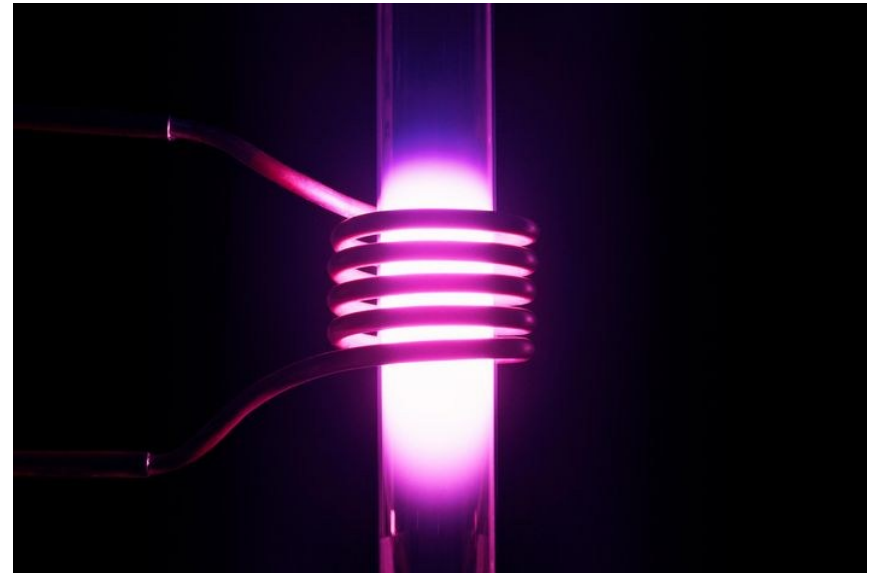
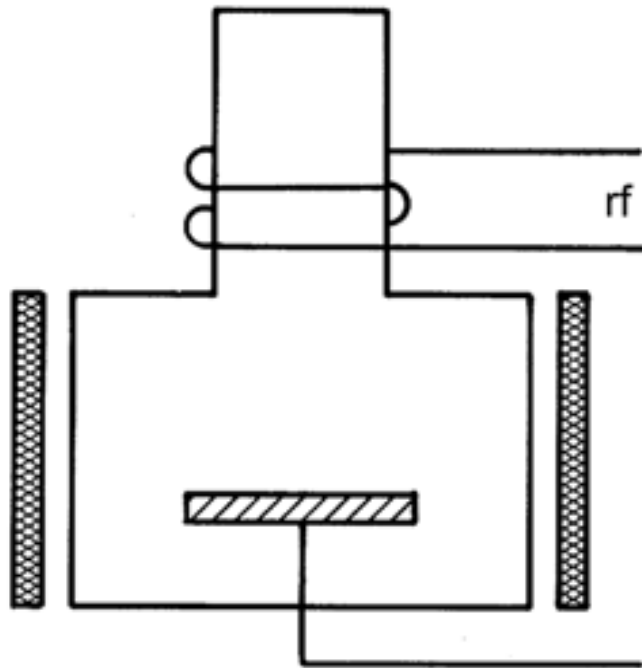




# Magnetron

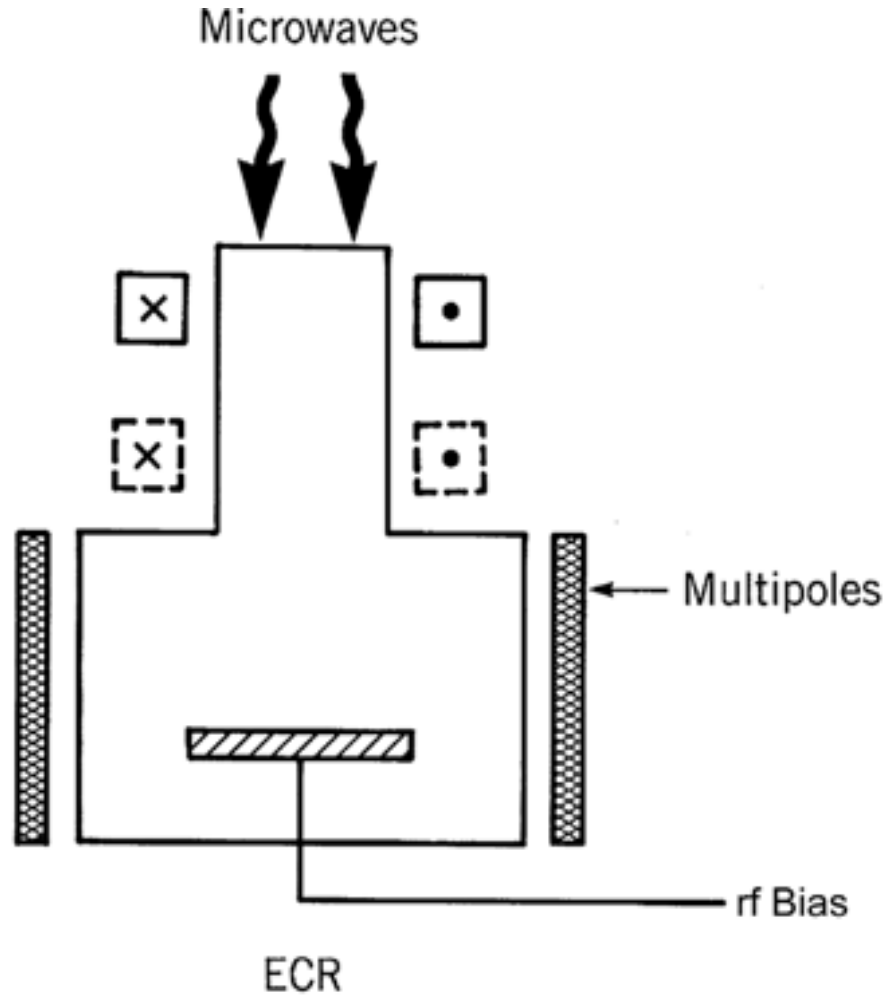


# High density sources (ICP)



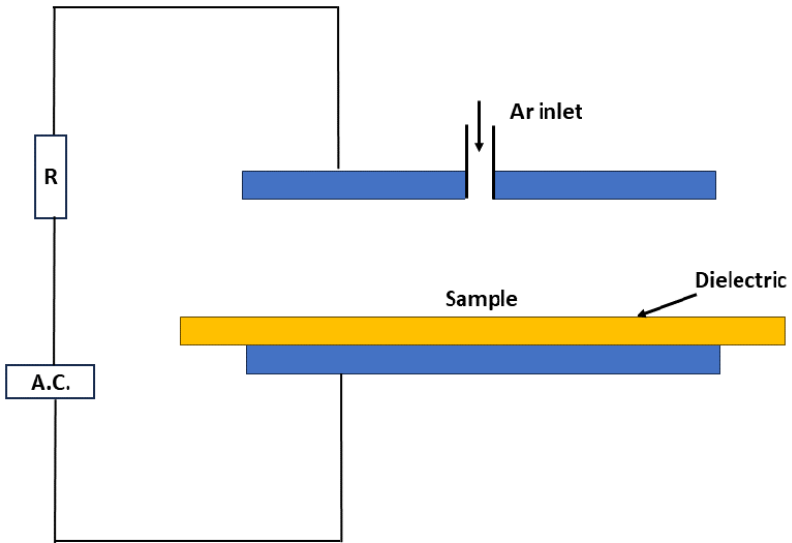


# High density sources (ECR)

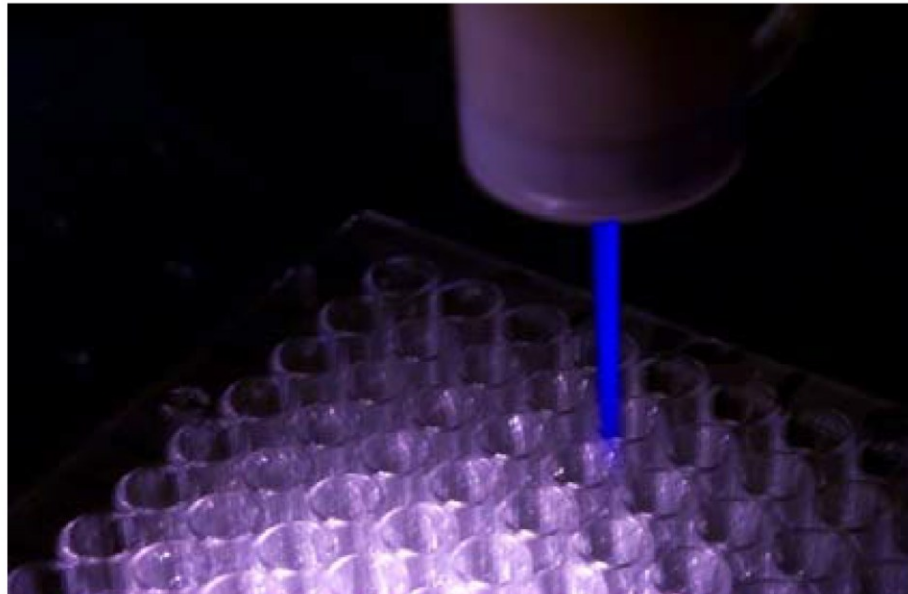
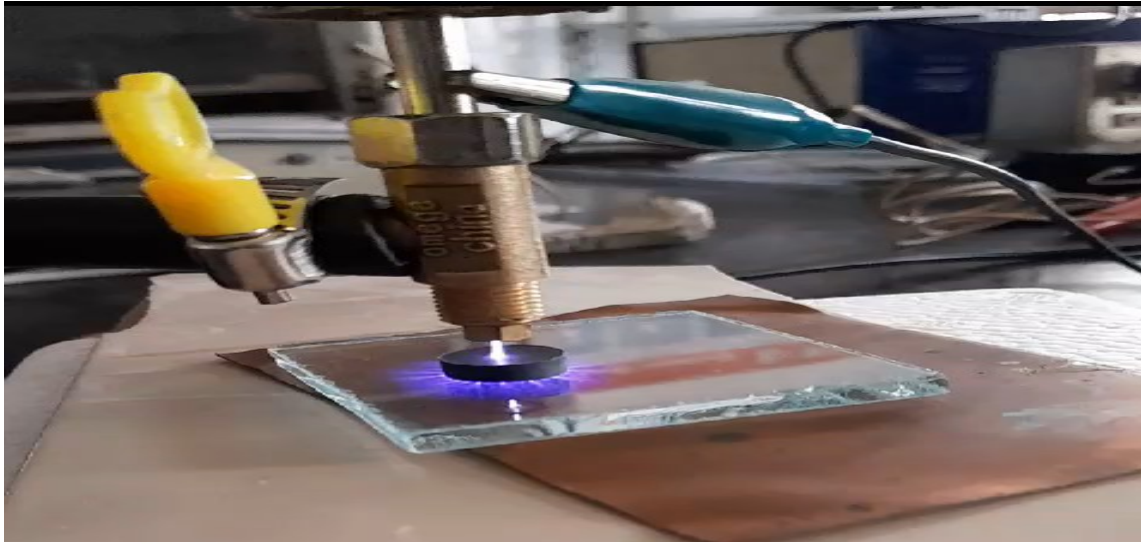


# Home-made Devices

## DBD-JET



# Atmospheric Plasma Jet



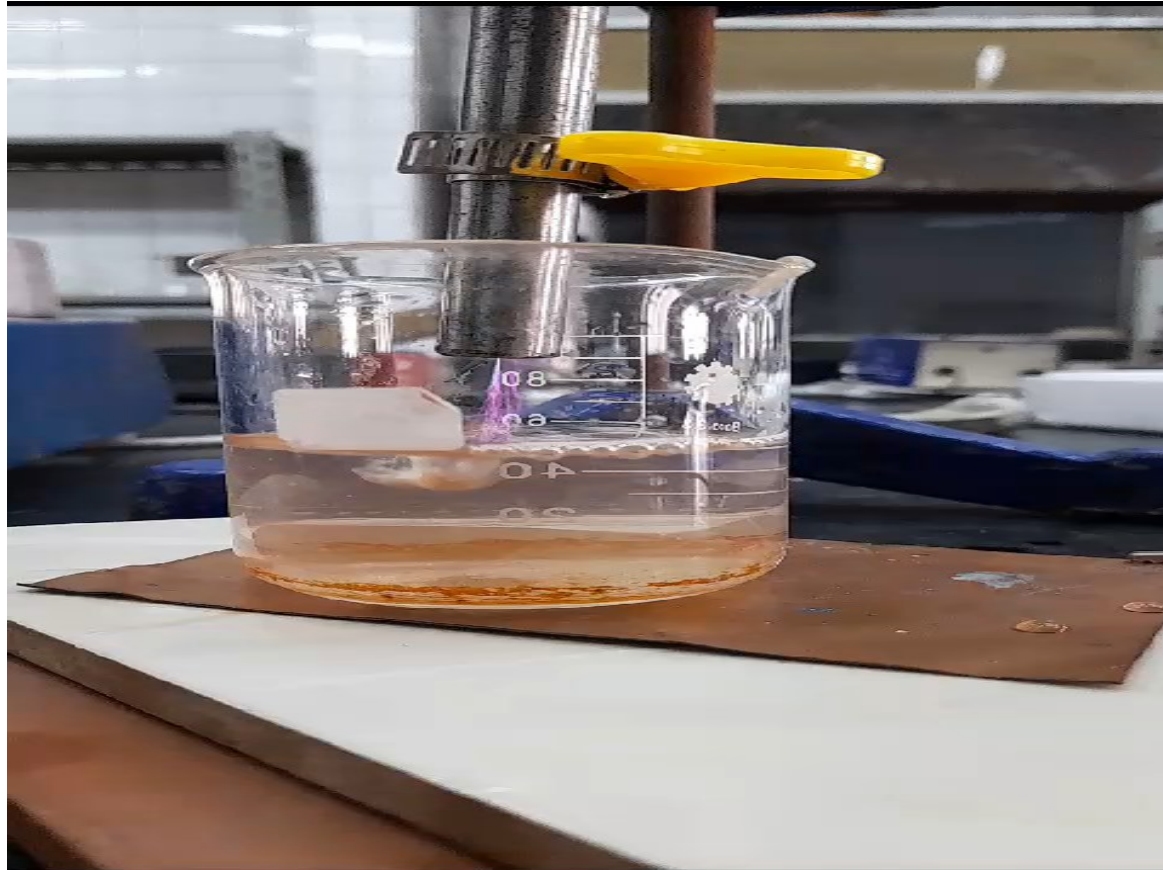
(a)



(b)

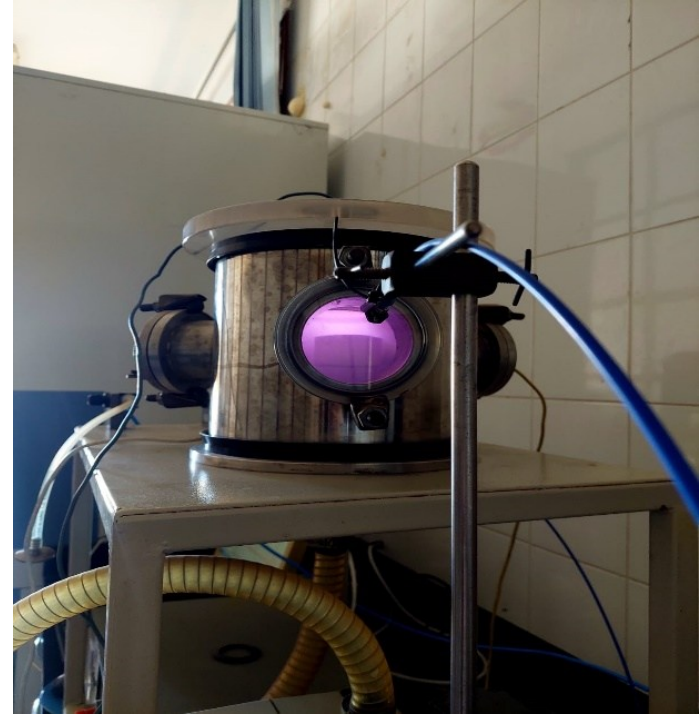
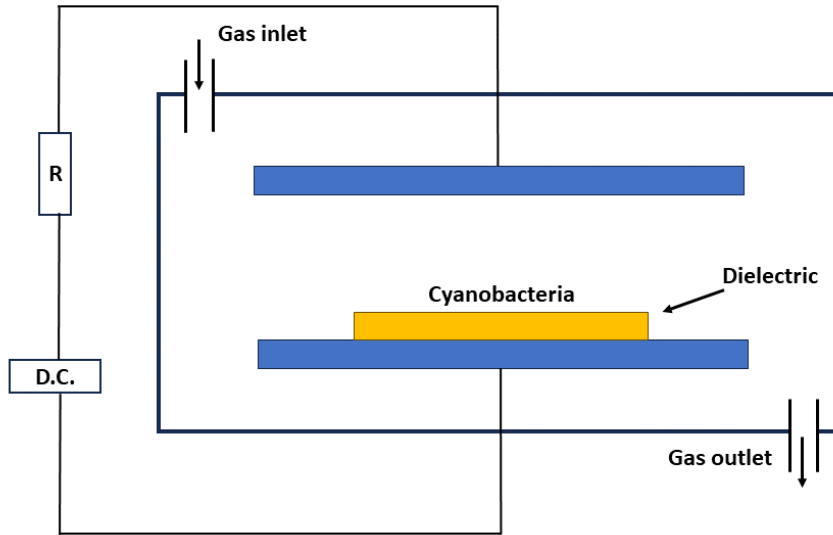


# Devices





# Capacitive Coupled Plasma





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# Theoretical Side

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# Challenges of plasma simulation

- The most accurate method is to solve the equation of motion of each particle in the plasma.

$$m \frac{d\vec{v}_k}{dt} = e\vec{E}_k + e\vec{v}_k \times \vec{B}_k$$

- No. of particles is very very large  $n = 10^9 - 10^{13} \text{cm}^{-3}$

- Maxwell equations

$$\vec{\nabla} \cdot \vec{D} = \rho_v$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\vec{\nabla} \cdot \vec{B} = 0$$

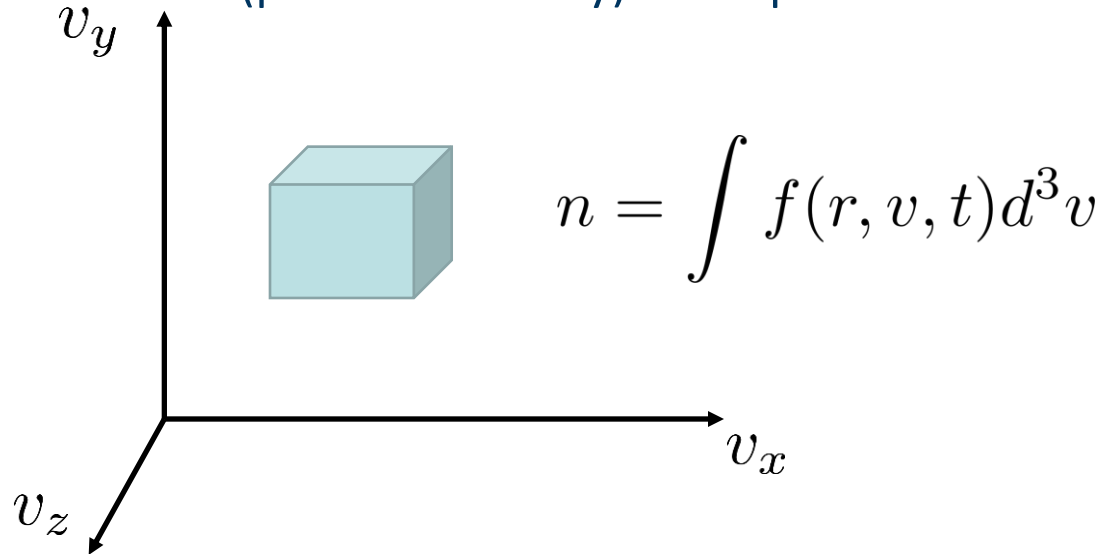
$$\vec{\nabla} \times \vec{H} = \vec{J} + \epsilon \frac{\partial \vec{E}}{\partial t}$$

- The collective behaviour and the huge number of particles make the solution impossible in such way.



# The distribution function

- The distribution function gives the number of particles per unit volume (particles density) with speed  $v$  as a function of time.



- The kinetic equation is an integro-differential equations in 7 parameters

$$\frac{Df}{Dt} = \frac{\partial f}{\partial t} + \vec{v} \cdot \vec{\nabla}_r f + \vec{a} \cdot \vec{\nabla}_v f = \text{collision terms}$$



# Macroscopic description

- Instead of known the physical parameters of each particle, one can calculate the average values for the whole plasma system.

- Average plasma density  $\bar{n} = \int f(r, v, t) d^3v$

- Average speed  $\bar{v} = \int v f(r, v, t) d^3v / \bar{n}$

- Kinetic energy  $\bar{E}_k = \int \frac{1}{2} m v^2 f(r, v, t) d^3v / \bar{n}$

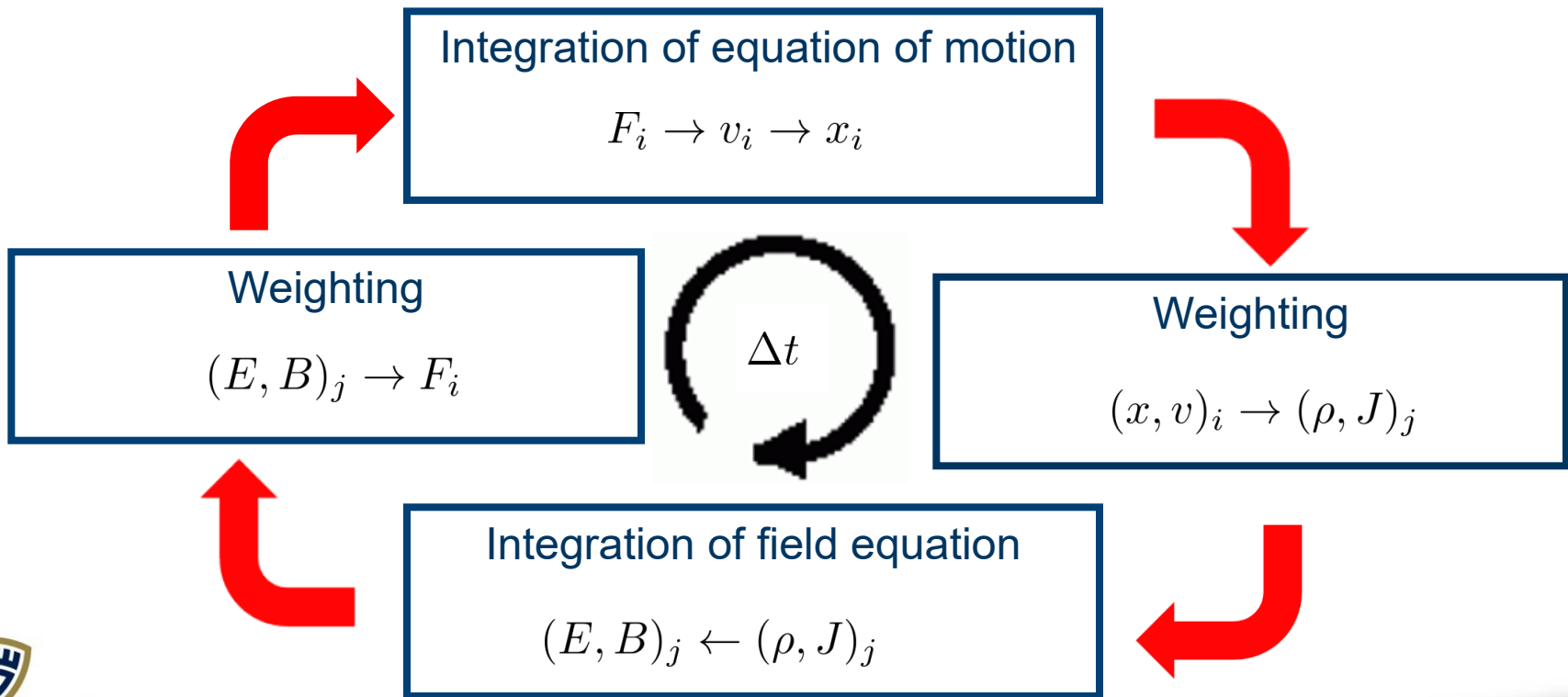
- Averages over Boltzmann equation

$$m v^q \left( \frac{\partial f}{\partial t} + \vec{v} \cdot \vec{\nabla}_r f + \vec{a} \cdot \vec{\nabla}_v f \right) = \text{collision terms}$$
$$q = 0, 1, 2, 3, \dots$$



# Particle in Cell Simulation

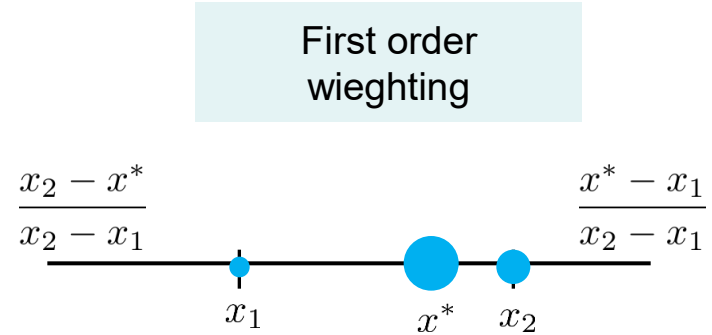
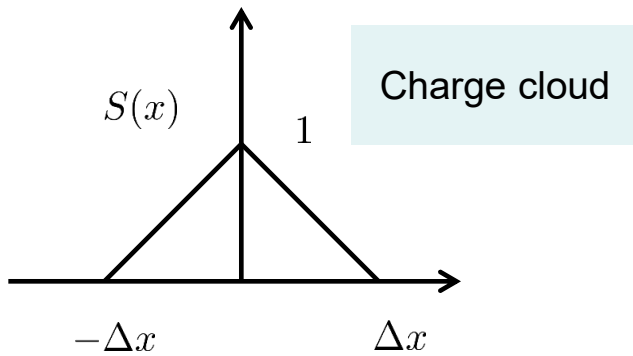
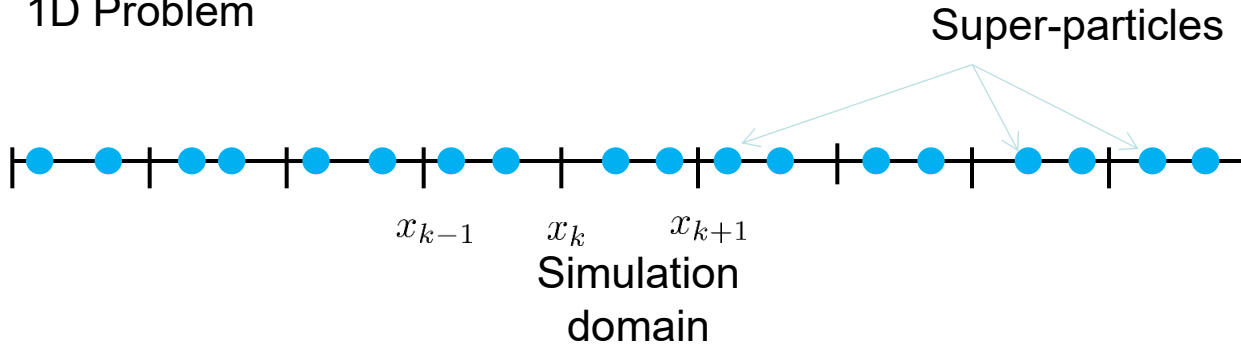
- Kinetic means „of or relating to motion“.
  - It is impractical to solve the equation of motion of all plasma particles.
  - Boltzman equation is an integro-differential equation.
- Particle-in-Cell : Super particle  $10^6 - 10^9$  real particles.





# Particles

1D Problem





# Fields

Poisson's eq.

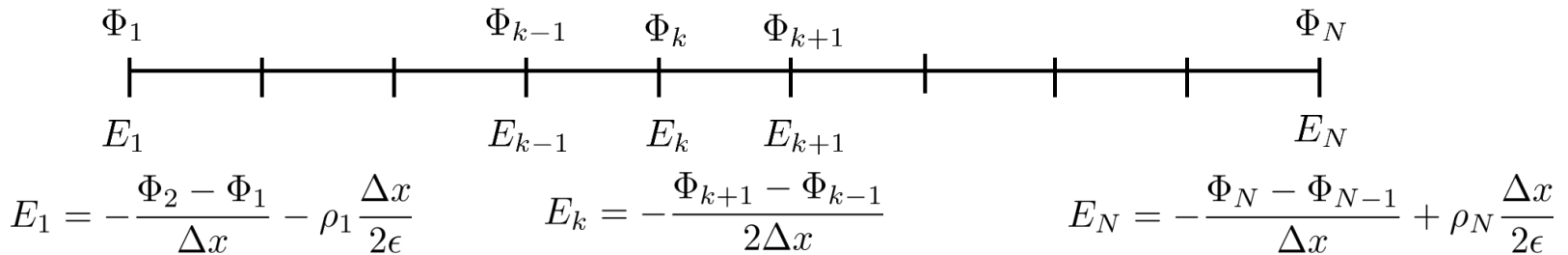
$$\nabla^2 \Phi = -\frac{\rho}{\epsilon}$$



$$\frac{\Phi_{k+1} - 2\Phi_k + \Phi_{k-1}}{\Delta x^2} = -\frac{\rho}{\epsilon}$$

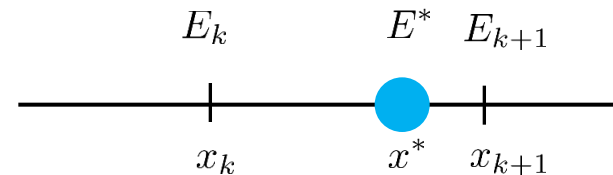
Boundary condition

Boundary condition



Interpolation of the fields to the particle positions

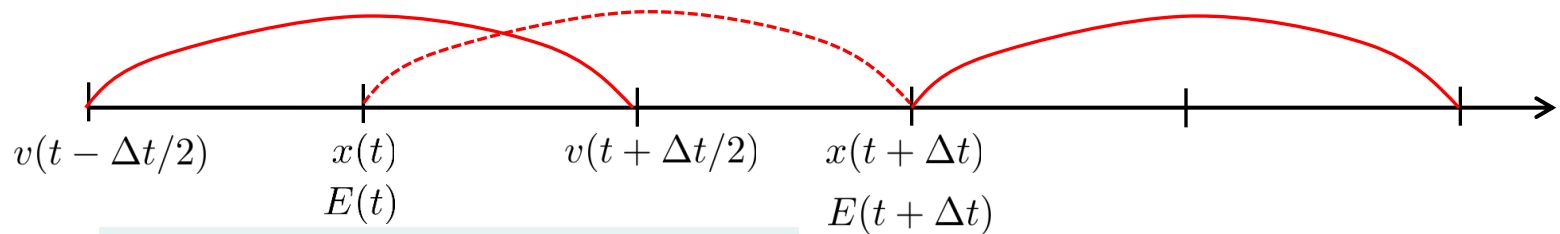
$$E^* = \frac{x^* - x_k}{\Delta x} E_{k+1} + \frac{x_{k+1} - x^*}{\Delta x} E_k$$





# Pushing particles

„Leapfrog“  
scheme



Descritization of equation of motions

$$\frac{v(t + \Delta t/2) - v(t - \Delta t/2)}{\Delta t} = \frac{q}{m} E(t)$$

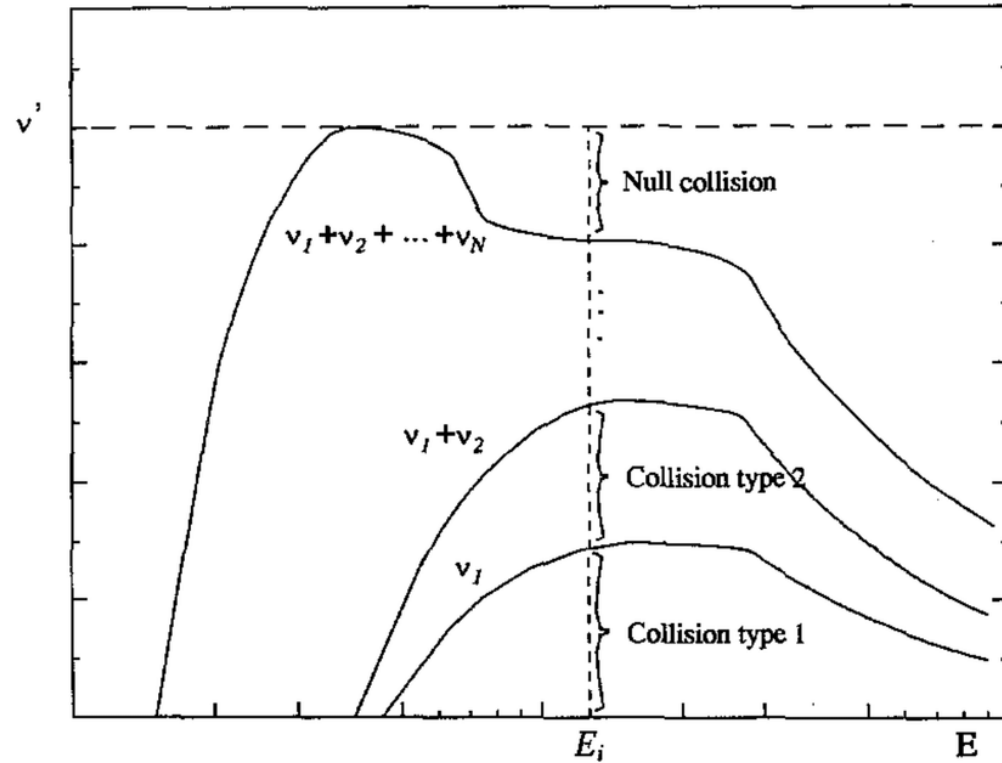
$$\frac{x(t + \Delta t) - x(t)}{\Delta t} = v(t + \Delta t/2)$$

Monte-Carlo Scheme is required for collisions



# Monte Carlo: null collision method

- Many collisions take place:  
impact ionization, charge exchange,  
hard-sphere, ...
- Let the probability of them  
 $P_1, P_2, P_3, P_4, \dots$
- Calculate the total probabilities  $P_T$
- Calculate relative probabilities  
 $P_1/P_T, P_2/P_T, P_3/P_T, P_4/P_T, \dots$



- Generate a random number between  $[0,1]$
- if  $P_1/P_T = < \text{The random number} < (P_1 + P_2)/P_T$
- Event 1 takes place
- If not

$(P_1 + P_2)/P_T = < \text{The random number} < (P_1 + P_2 + P_3)/P_T$





# Challenges of PIC simulation

- Numerical instabilities:
  - Accuracy criterion  $\omega_p \Delta t \leq 0.2$
  - Courant criterion  $v_{\max} \Delta t \leq \Delta x$
  - The computational grid has to resolve the Debye length  $\Delta x \leq \lambda_D$
- In order to have a good statistics, a reasonable high number of particles per Debye length must be used  $N_D \gg 1$
- Keep the probability for collisions small
$$P_{\text{coll}} = 1 - e^{-\nu t} \leq 0.1$$
- Alternatives:
  - Implicit schemes
  - Parallelization



# Fluid Models

- Continuity, momentum, and energy equations are closed with Poisson's equation



$$\frac{\partial n_{e,i,m}}{\partial t} + \vec{\nabla} \cdot \vec{\Gamma}_{e,i,m} = G_{e,i,m} - L_{e,i,m},$$

$$\vec{\Gamma}_{e,i,m} = \text{sign}(q_{e,i,m}) n_{e,i,m} \mu_{e,i,m} \vec{E} - D_{e,i,m} \vec{\nabla} n_{e,i,m},$$

$$\frac{\partial n_e T_e}{\partial t} = -\vec{\nabla} \cdot \left( \frac{5}{3} T_e \vec{\Gamma}_e - \frac{5}{3} n_e D_e \vec{\nabla} T_e \right) - e \vec{\Gamma}_e \cdot \vec{E} - n_e n_G k_{\text{loss}},$$

and

$$T_i = T_m = 0.026 \text{ eV}.$$



# Fluid Models

## Ar atomic processes considered in the simulation

Equation of Reaction	Rate of Reaction Coefficient	
$e + \text{Ar} \rightarrow \text{Ar}^+ + 2e$	impact-ionization	$K_{ei} = 1.253 \times 10^{-7} \exp(-18.618/T_e) \text{ cm}^3/\text{s}$
$e + \text{Ar} \rightarrow \text{Ar}^* + e$	collisional-excitation	$K_{ex} = 3.712 \times 10^{-8} \exp(-15.06/T_e) \text{ cm}^3/\text{s}$
$e + \text{Ar}^* \rightarrow \text{Ar}^+ + 2e$	impact-ionization	$K_{mi} = 2.05 \times 10^{-7} \exp(-4.95/T_e) \text{ cm}^3/\text{s}$
$e + \text{Ar}^* \rightarrow \text{Ar} + e$	collisional-deexcitation	$K_{em} = 1.818 \times 10^{-9} \exp(-2.14/T_e) \text{ cm}^3/\text{s}$
$e + \text{Ar}^* \rightarrow \text{Ar}^r + e$	radiative-deexcitation	$K_r = 2 \times 10^{-7} \text{ cm}^3/\text{s}$
$\text{Ar}^* + \text{Ar}^* \rightarrow \text{Ar}^+ + \text{Ar} + e$	collisional-ionization	$K_{mm} = 6.2 \times 10^{-10} \text{ cm}^3/\text{s}$
$\text{Ar}^* + \text{Ar} \rightarrow 2\text{Ar}$	collisional-deexcitation	$K_{2q} = 3.0 \times 10^{-15} \text{ cm}^3/\text{s}$
$\text{Ar}^* + 2\text{Ar} \rightarrow \text{Ar} + \text{Ar}_2$	attachment	$K_{3q} = 1.1 \times 10^{-31} \text{ cm}^6/\text{s}$





Main reactions and the corresponding rate coefficients in the Ar/CF<sub>4</sub> discharge plasma.

Reaction equation	Reaction rate coefficient
$\text{CF}_3^- + \text{Ar}^+ \rightarrow \text{CF}_3 + \text{Ar}$	$1 \times 10^{-7} \text{ cm}^3 \text{ s}^{-1}$
$\text{F}^- + \text{Ar}^+ \rightarrow \text{F} + \text{Ar}$	$1 \times 10^{-7} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4 + \text{Ar}^+ \rightarrow \text{CF}_3^+ + \text{F} + \text{Ar}$	$9.58 \times 10^{-10} \text{ cm}^3 \text{ s}^{-1}$
$\text{Ar} + \text{CF}_3^+ \rightarrow \text{CF}_3 + \text{Ar}^+$	$1 \times 10^{-9} \text{ cm}^3 \text{ s}^{-1}$

**Chengjie Bai et al 2018 *J. Phys. D: Appl. Phys.* 51 255201**



Reaction equation	Reaction rate coefficient
$\text{CF}_4 + e \rightarrow \text{CF}_4^+ + 2e$	Calculated by BOLSIG+
$\text{CF}_3 + e \rightarrow \text{CF}_3^+ + 2e$	$1.4 \times 10^{-11} (11605 \times T_e)^{0.6481} \exp(-9.8/T_e) \text{ cm}^3 \text{ s}^{-1}$
$\text{F} + e \rightarrow \text{F}^+ + 2e$	$7.489 \times 10^{-13} (11605 \times T_e)^{0.8595} \exp(-17.6/T_e) \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4 + e \rightarrow \text{CF}_4^*(12.5 \text{ eV}) + e$	Calculated by BOLSIG+
$\text{CF}_4 + e \rightarrow \text{CF}_4^*(8 \text{ eV}) + e$	Calculated by BOLSIG+
$\text{CF}_4 + e \rightarrow \text{CF}_4(\text{V13}) + e$	Calculated by BOLSIG+
$\text{CF}_4 + e \rightarrow \text{CF}_4(\text{V24}) + e$	Calculated by BOLSIG+
$\text{CF}_4 + e \rightarrow \text{CF}_3^+ + \text{F} + 2e$	$1.159 \times 10^{-11} (11605 \times T_e)^{0.7645} \exp(-17.2/T_e) \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4 + e \rightarrow \text{CF}_2^+ + \text{F}_2 + 2e$	$2.886 \times 10^{-11} (11605 \times T_e)^{0.5108} \exp(-22.8/T_e) \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4 + e \rightarrow \text{CF}^+ + \text{F}_2 + \text{F} + 2e$	$2.296 \times 10^{-14} (11605 \times T_e)^{1.09} \exp(-27.0/T_e) \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4 + e \rightarrow \text{CF}_3 + \text{F}^+ + 2e$	$1.482 \times 10^{-13} (11605 \times T_e)^{0.9375} \exp(-34.7/T_e) \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4 + e \rightarrow \text{CF}_3 + \text{F} + e$	$2 \times 10^{-9} \exp(-13/T_e) \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4 + e \rightarrow \text{CF}_2 + 2\text{F} + e$	$5 \times 10^{-9} \exp(-13/T_e) \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_3 + \text{F}^- \rightarrow \text{CF}_4 + e$	$5 \times 10^{-10} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_2 + \text{F}^- \rightarrow \text{CF}_3 + e$	$5 \times 10^{-10} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF} + \text{F}^- \rightarrow \text{CF}_2 + e$	$5 \times 10^{-10} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_3 + \text{F} \rightarrow \text{CF}_4$	$2 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_2 + \text{F} \rightarrow \text{CF}_3$	$1.3 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF} + \text{F} \rightarrow \text{CF}_2$	$5.2 \times 10^{-15} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_3^- + \text{CF}_3^+ \rightarrow 2\text{CF}_3$	$4 \times 10^{-7} \text{ cm}^3 \text{ s}^{-1}$
$\text{F}^- + \text{CF}_3^+ \rightarrow \text{F} + \text{CF}_3$	$4 \times 10^{-7} \text{ cm}^3 \text{ s}^{-1}$
$\text{F}^- + \text{CF}_2^+ \rightarrow \text{F} + \text{CF}_2$	$1 \times 10^{-7} T_g^{-0.5} \text{ cm}^3 \text{ s}^{-1}$
$\text{F}^- + \text{CF}^+ \rightarrow \text{F} + \text{CF}$	$1 \times 10^{-7} T_g^{-0.5} \text{ cm}^3 \text{ s}^{-1}$
$\text{F}^- + \text{F}^+ \rightarrow \text{F}_2$	$4 \times 10^{-7} T_g^{-0.5} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_2^+ + e \rightarrow \text{CF} + \text{F}$	$4 \times 10^{-8} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}^+ + e \rightarrow \text{C} + \text{F}$	$4 \times 10^{-8} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_3^+ + e \rightarrow \text{CF}_3$	$9.6 \times 10^{-7} \text{ cm}^3 \text{ s}^{-1}$
$\text{F}^+ + e \rightarrow \text{F}$	$4 \times 10^{-8} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4^+ \rightarrow \text{CF}_3^+ + \text{F}$	$3.3 \times 10^5 \text{ s}^{-1}$
$\text{CF}_4 + e \rightarrow \text{CF}_3 + \text{F}^-$	$4.8 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_4 + e \rightarrow \text{CF}_3^- + \text{F}$	$3.28 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_2 + \text{F}_2 \rightarrow \text{CF}_3 + \text{F}$	$4.56 \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_3 + \text{F}_2 \rightarrow \text{CF}_4 + \text{F}$	$1.88 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}$
$\text{CF}_3^- + \text{F} \rightarrow \text{CF}_3 + \text{F}^-$	$5 \times 10^{-8} \text{ cm}^3 \text{ s}^{-1}$
$2\text{CF}_4^*(12.5 \text{ eV}) \rightarrow 2\text{CF}_4$	$4.9 \times 10^{-4} \text{ cm}^3 \text{ s}^{-1}$
$2\text{CF}_4^*(8 \text{ eV}) \rightarrow 2\text{CF}_4$	$4.9 \times 10^{-4} \text{ cm}^3 \text{ s}^{-1}$
$2\text{CF}_4(\text{V13}) \rightarrow 2\text{CF}_4$	$4.9 \times 10^{-4} \text{ cm}^3 \text{ s}^{-1}$
$2\text{CF}_4(\text{V24}) \rightarrow 2\text{CF}_4$	$4.9 \times 10^{-4} \text{ cm}^3 \text{ s}^{-1}$





# Global model: Zero-dimensional model

$$\frac{\partial n_e}{\partial t} = n_e n_s k_i - n_e n_s k_r - \text{loss term}$$

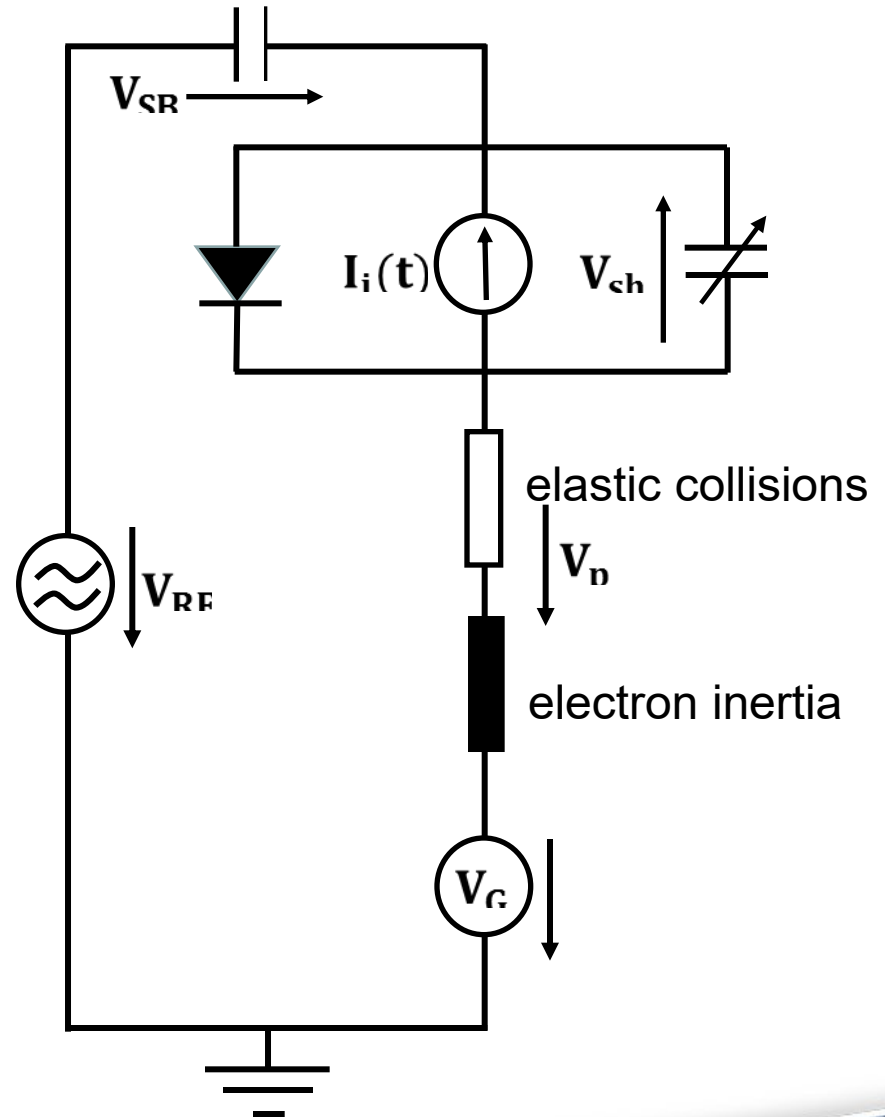
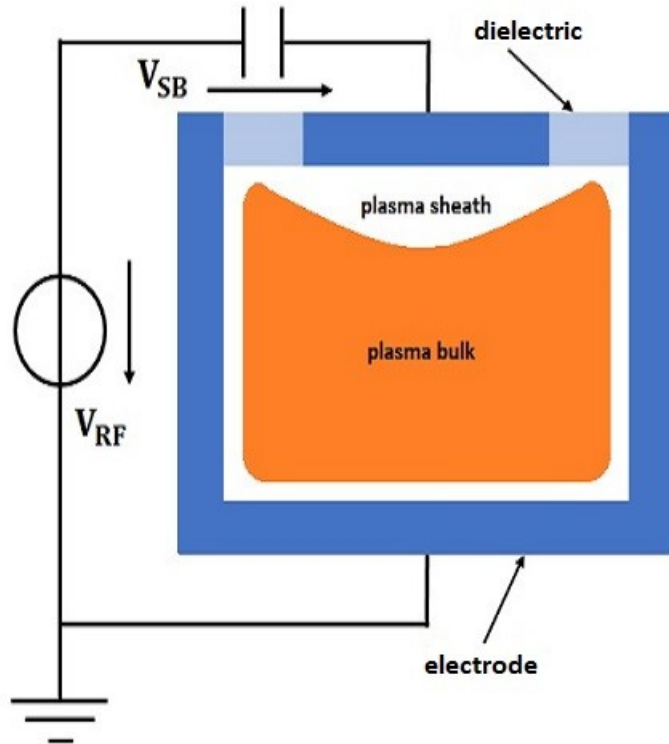
## Note

- If right hand side always positive = Simulation diverge with time
- If right hand side always negative= the plasma density vanishes with time
- We are looking for balance situation. Comparison with experiments is highly required.





# Global model: Electrical circuit



M. Shihab / Physics Letters A 382 (2018) 1609–1614



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# Experimental Side

Prof. Dr. Mohammed Shihab

Plasma Technology



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# Outline

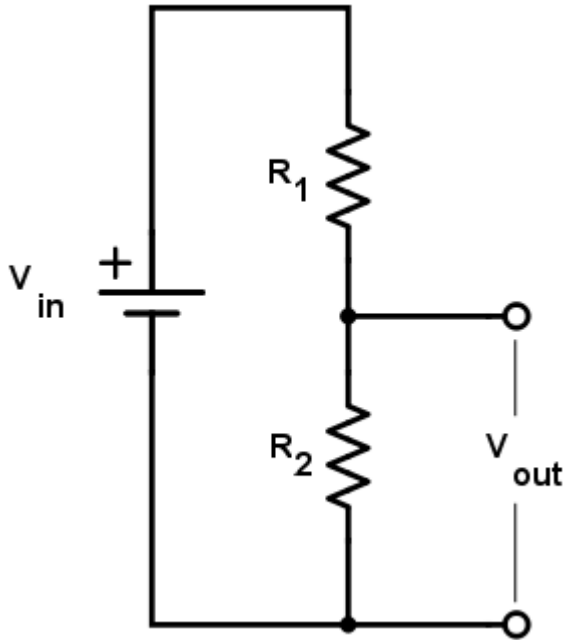
- Introduction.
  - Low temperature plasmas.
  
- Measurements:
  - Voltage
  - Current
  - Density
  - Temperature
  
- Conclusion.

# High Voltage Probe





# High Voltage Probe



$$V_{in} = I(R_1 + R_2)$$

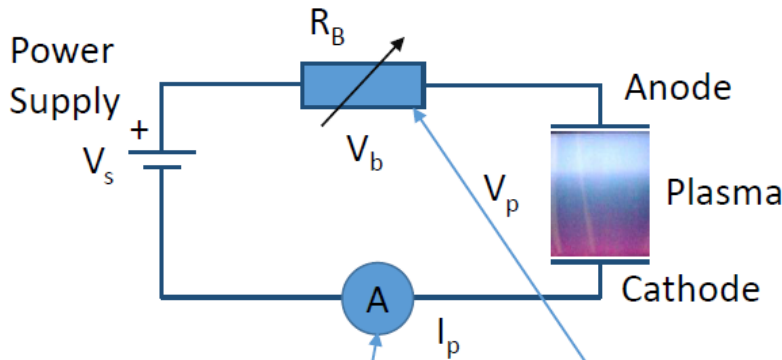
$$V_{out} = IR_2$$

$$\frac{V_{out}}{V_{in}} = \frac{R_2}{R_1 + R_2}$$

When  $R_2 \ll R_1$  Then  $V_{out} \ll V_{in}$

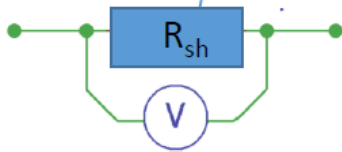


# DC Current Measurements



Ohm's Law

Power



$I_p$  can be also determined from a voltage drop on  $R_B$



Typical accuracy ~1%  
Range V: mV to kV  
Range A: mA to A



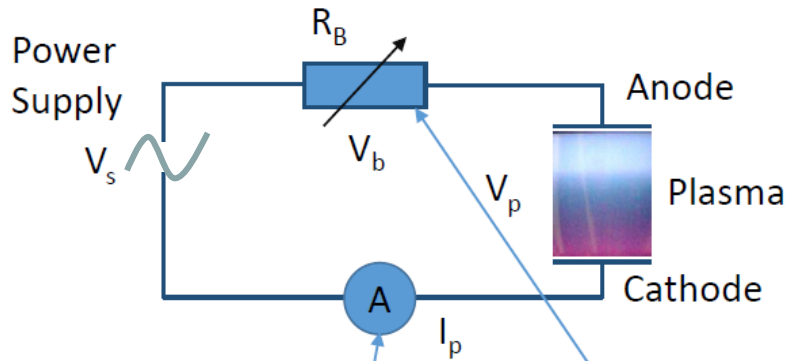
34465A

Typical accuracy ~0.01%  
Range V: mV to kV  
Range A: microA to A

Shunt resistor for DC:  $V=IR$

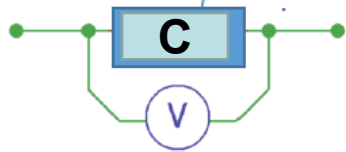


# AC Current



Ohm's Law

Power



$I_p$  can be also determined from a voltage drop on  $R_B$



Typical accuracy ~1%  
Range V: mV to kV  
Range A: mA to A



34465A

Typical accuracy ~0.01%  
Range V: mV to kV  
Range A: microA to A

For AC, replace the resistance with capacitor

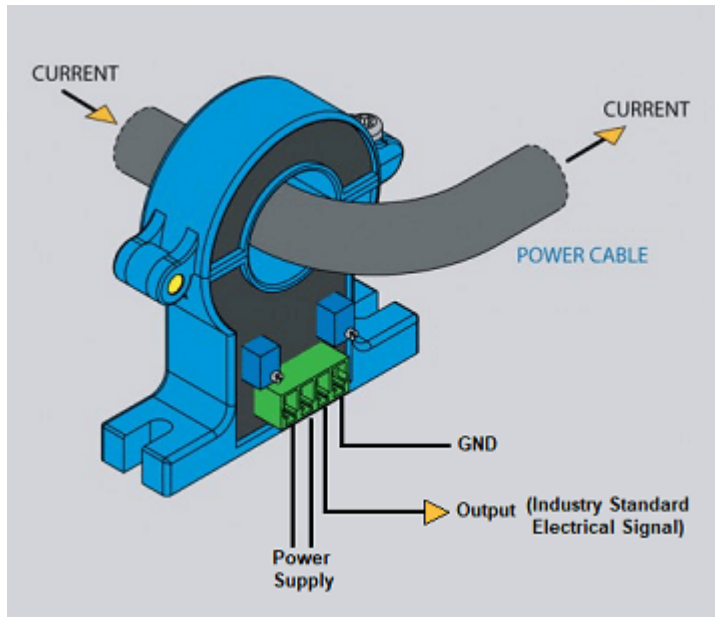
$$V = Q/C \quad I = C \frac{dV}{dt}$$



# Current Sensors

A current sensor is a device that detects and converts current to an easily measure output voltage

## Current transducer

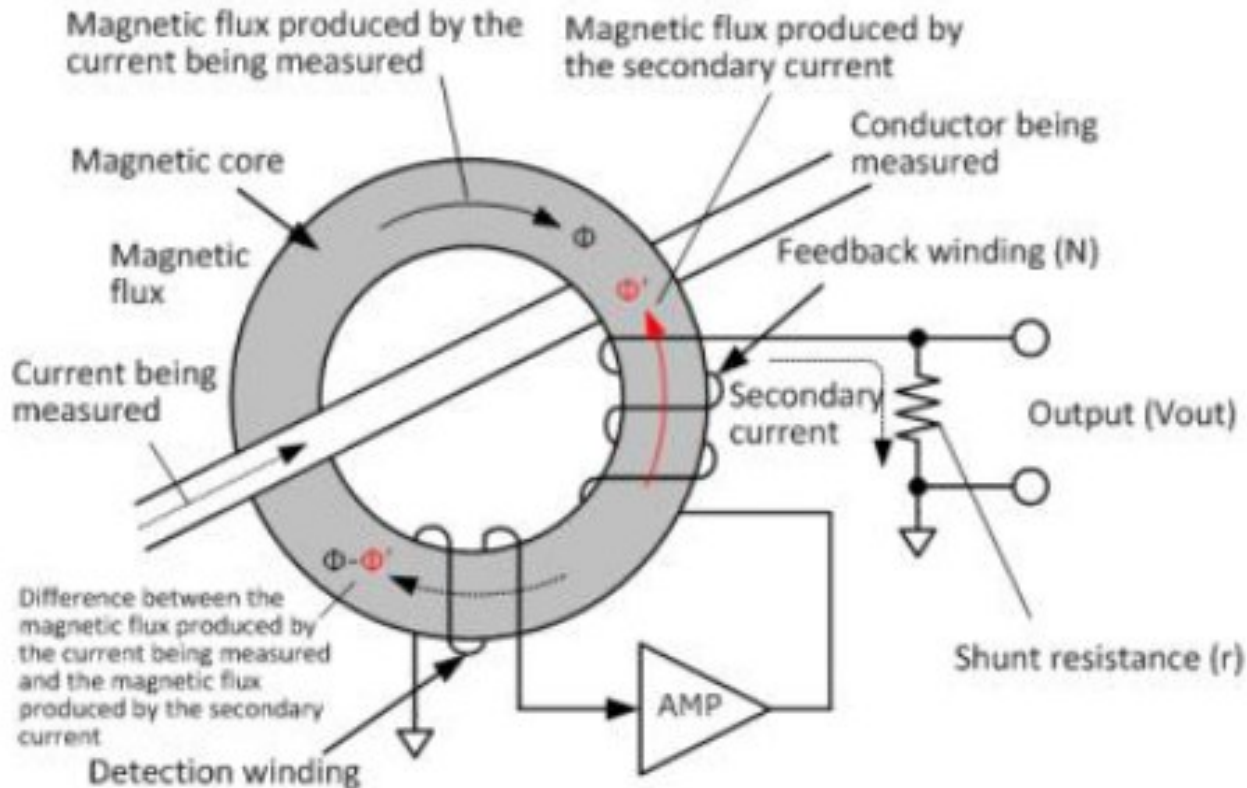




# Current Sensors

A current sensor is a device that detects and converts current to an easily measure output voltage

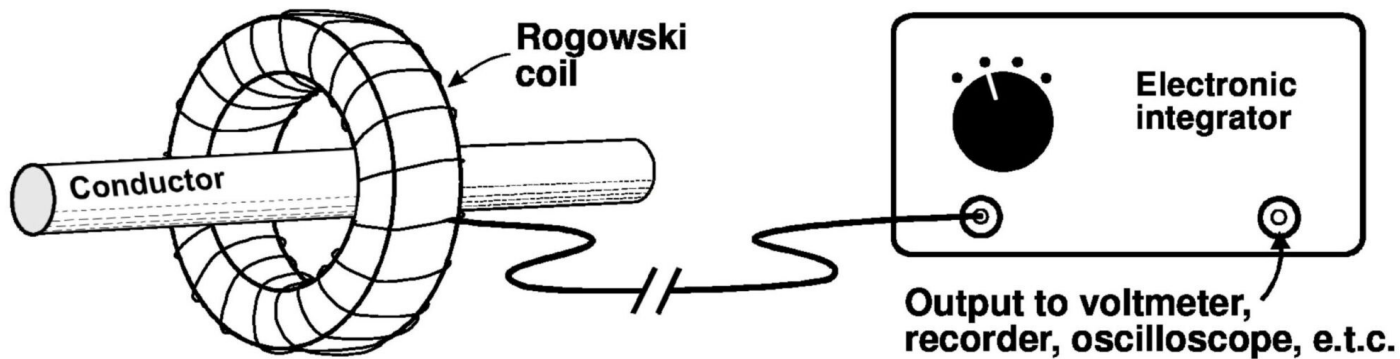
## Zero-flux type (AC)





# Current Sensors

A current sensor is a device that detects and converts current to an easily measure output voltage



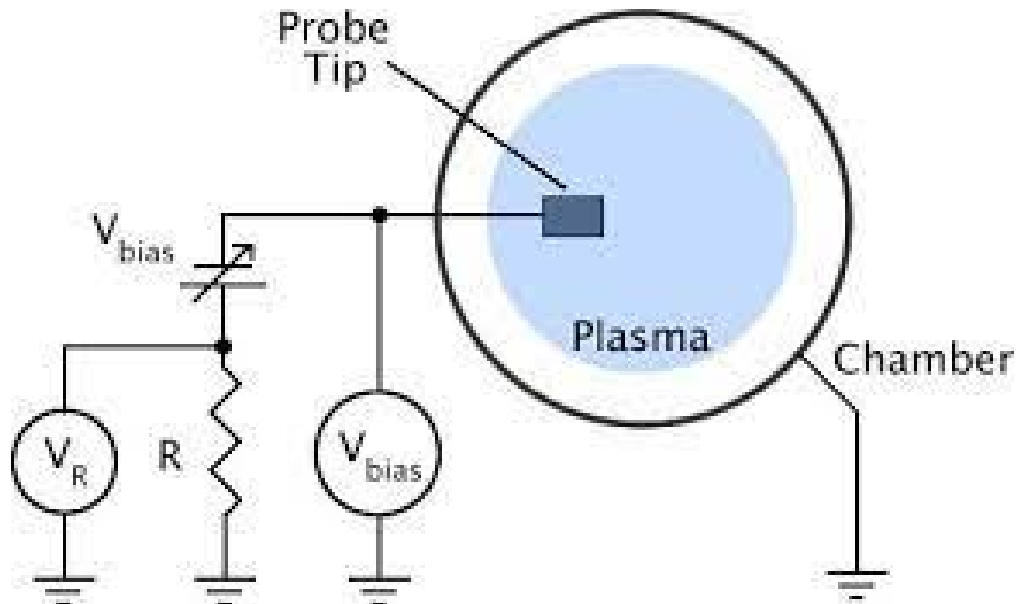
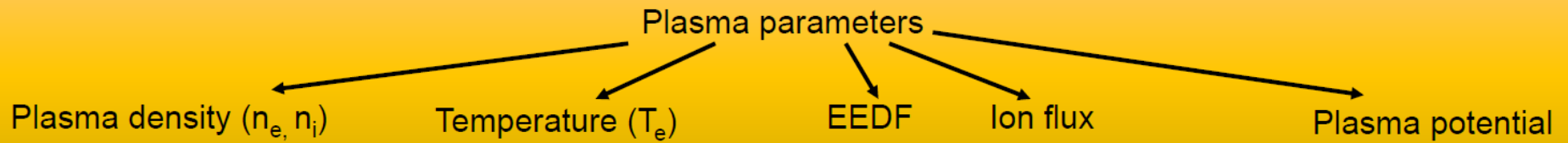
A Rogowski coil is an 'air-cored' toroidal coil placed round the conductor. The alternating magnetic field produced by the current induces a voltage in the coil which is proportional to the rate of change of current.

$$V = M \frac{dI}{dt}$$

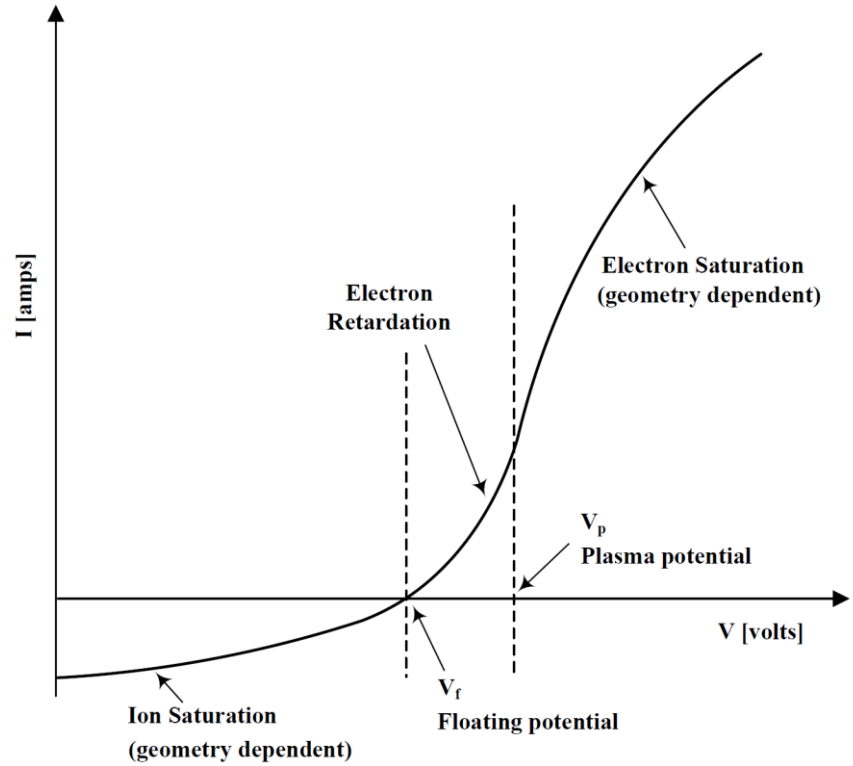
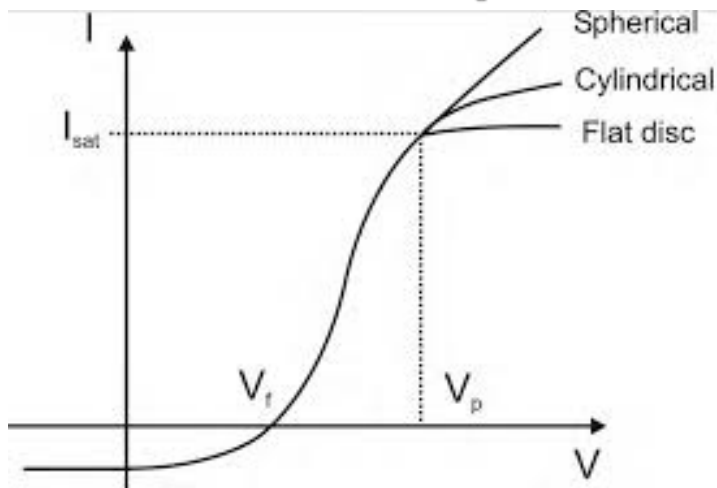
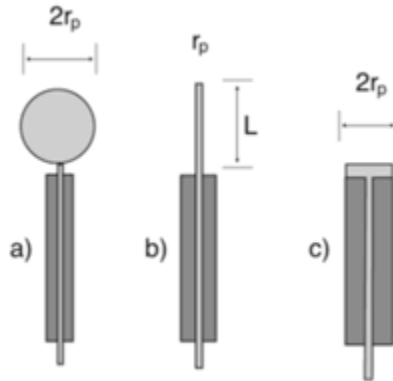


# Langmuir Probe

One of the most frequently employed methods for plasma diagnostics is Langmuir probes.



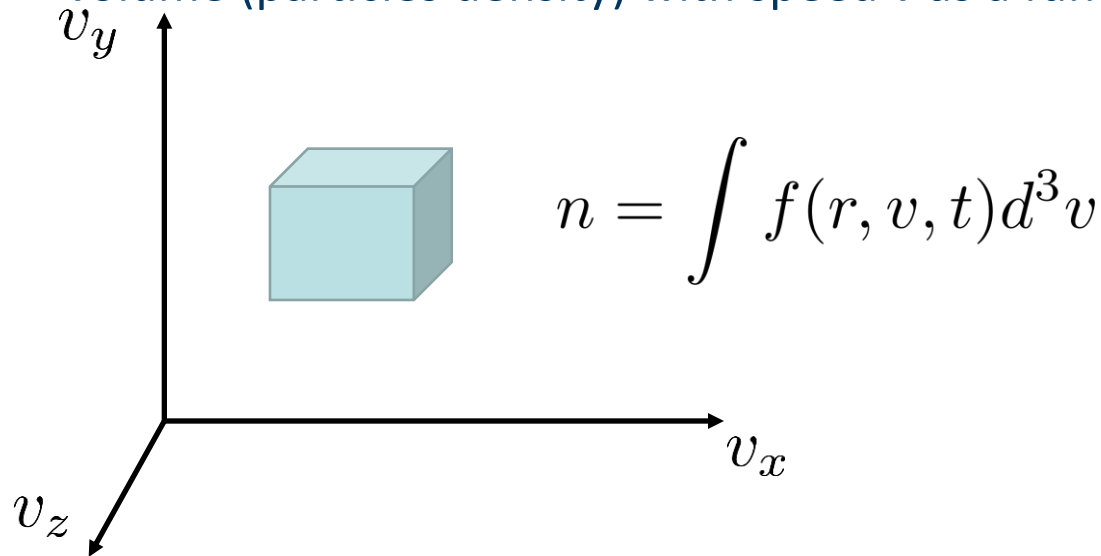
# Langmuir Probe





# The distribution function

- The distribution function gives the number of particles per unit volume (particles density) with speed  $v$  as a function of time.



- At equilibrium

$$f = f_0 \exp\left(\frac{-mv^2}{2k_B T_e}\right) \quad f = f_0 \exp\left(\frac{-E_k}{k_B T_e}\right)$$



# Sheath formation

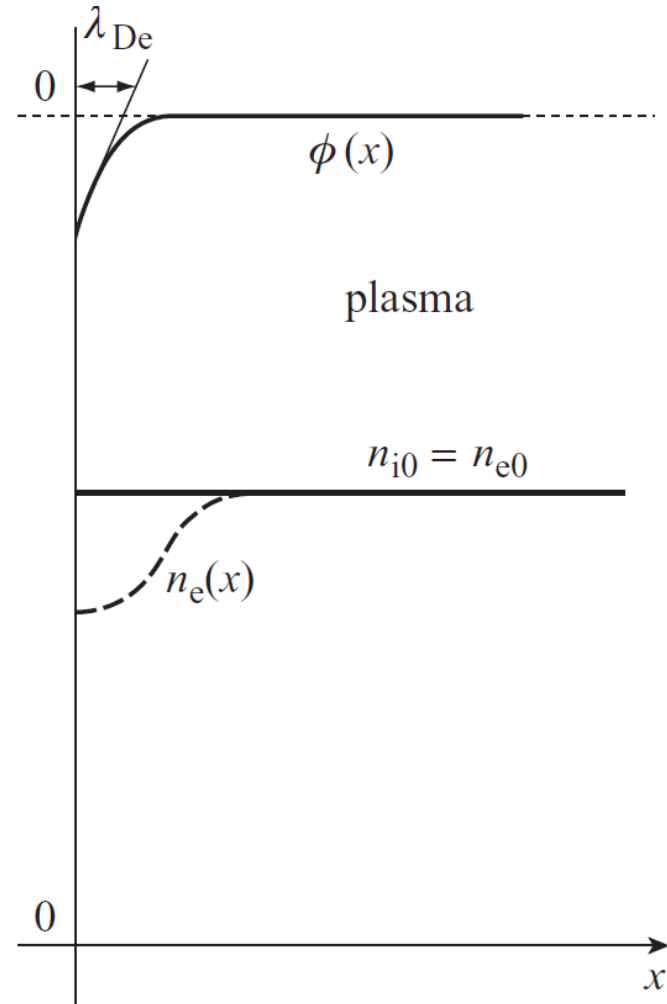
$$J_e = -e\Gamma_e = -\frac{1}{4}en_e\bar{v}_e = -en_e\sqrt{\frac{kT_e}{2\pi m}},$$

$$J_i = e\Gamma_i = \frac{1}{4}en_i\bar{v}_i = en_i\sqrt{\frac{kT_i}{2\pi M}}.$$

A steady state would be reached when the potential of the object is sufficiently negative for the electron flux to exactly balance that of the positive ions. Such a potential is called the *DC floating potential*. **At balance:**

$$n_e\sqrt{T_e/m} = n_i\sqrt{T_i/M}$$

$$n_i > n_e$$





# Floating Sheath

$$\frac{(n_i - n_e)e}{\epsilon_0} = \frac{dE}{dx} = -\frac{d^2\phi}{dx^2}.$$

$$e(n_i - n_e) = en_{e0} \left[ 1 - \exp\left(\frac{e\phi}{kT_e}\right) \right] \approx -\frac{e^2 n_{e0} \phi(x)}{kT_e},$$

$$\frac{d^2\phi}{dx^2} = \frac{e^2 n_{e0} \phi}{\epsilon_0 kT_e}. \quad \phi(x) = \phi_0 \exp\left(-\frac{x}{\lambda_{De}}\right),$$

$$\lambda_{De} = \sqrt{\frac{\epsilon_0 kT_e}{n_{e0} e^2}}$$

**Exercise 3.1: Debye length** Calculate the Debye length for a plasma in which the electron density is  $n_{e0} = 1.0 \times 10^{16} \text{ m}^{-3}$  and  $kT_e/e = 2.0 \text{ V}$ .





# Floating Potential

$$\Gamma_e = \frac{n_s \bar{v}_e}{4} \exp\left(-\frac{e\Delta\phi}{kT_e}\right). \quad \bar{v} = \left(\frac{8kT}{\pi m}\right)^{1/2}$$

The formation of the sheath retards electrons with a temperature  $T_e$ , Only electrons with energy greater than  $e\Delta\phi$  can reach the electrode.

$$\Gamma_e = \Gamma_i$$

$$\Delta\phi = -V_f$$

$$\frac{n_s \bar{v}_e}{4} \exp\left(\frac{eV_f}{kT_e}\right) = n_s u_B$$

Bohm Speed:

$$u_s = \left(\frac{kT_e}{M}\right)^{1/2}$$

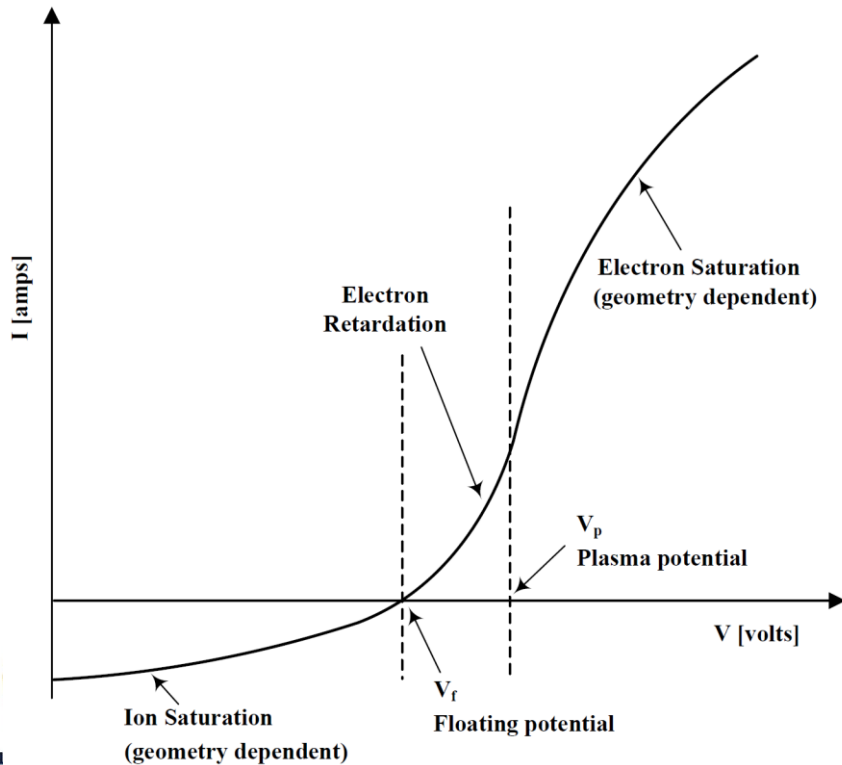
$$V_f = \frac{kT_e}{e} \frac{1}{2} \ln\left(\frac{2\pi m}{M}\right)$$



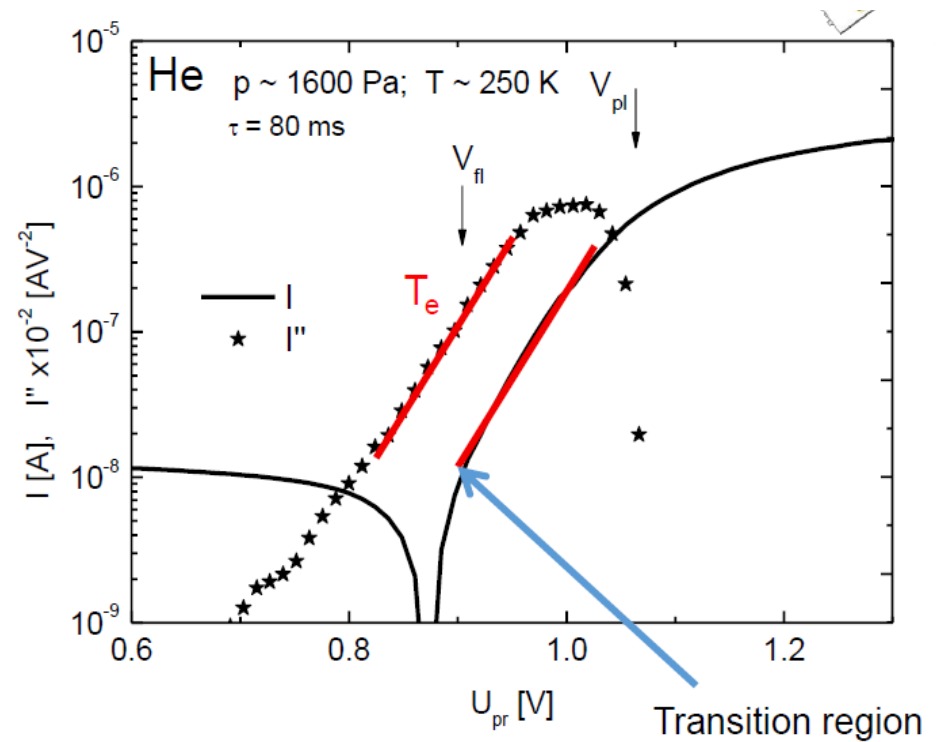
# Langmuir Probe

The electron temperature  $T_e$  for any plasma is well defined if the EEDF is Maxwellian

$$I_e(V) = I_{e0} \exp\left(-\frac{eV}{kT_e}\right)$$



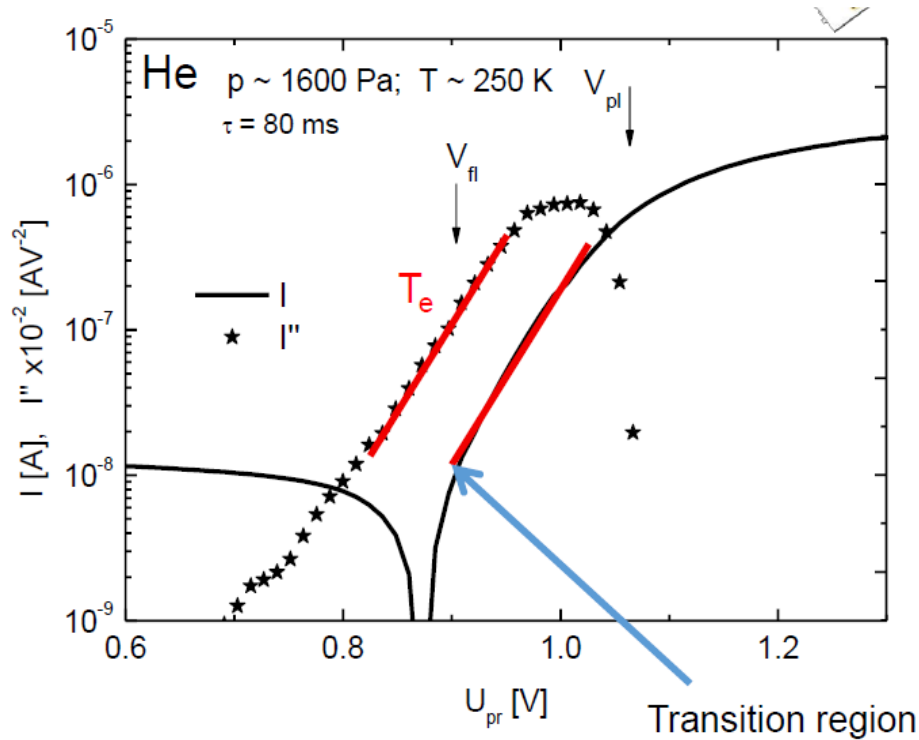
$$\ln[I_e(V)] = \ln[I_{e0}] - \frac{e}{kT_e} V$$



# Langmuir Probe:

Druyvesteyn method\*

The electron temperature  $T_e$  for any plasma is well defined if the EEDF is Maxwellian

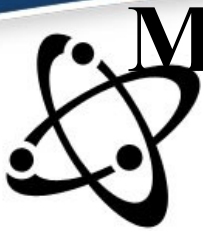


$$\frac{d^2 I}{d(V - V_p)^2} = \frac{1}{4} A q^2 \sqrt{\frac{2q}{m_e (V - V_p)}} [f(E)]$$

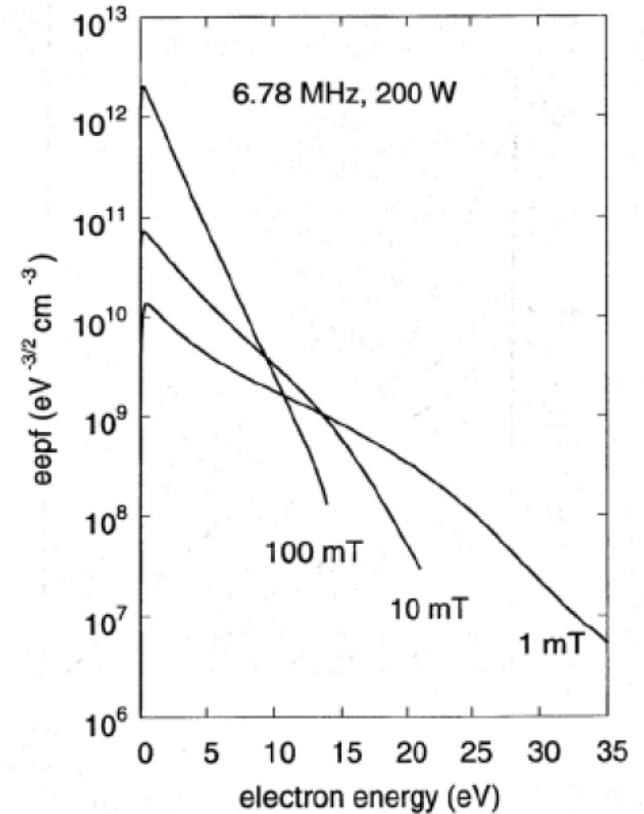
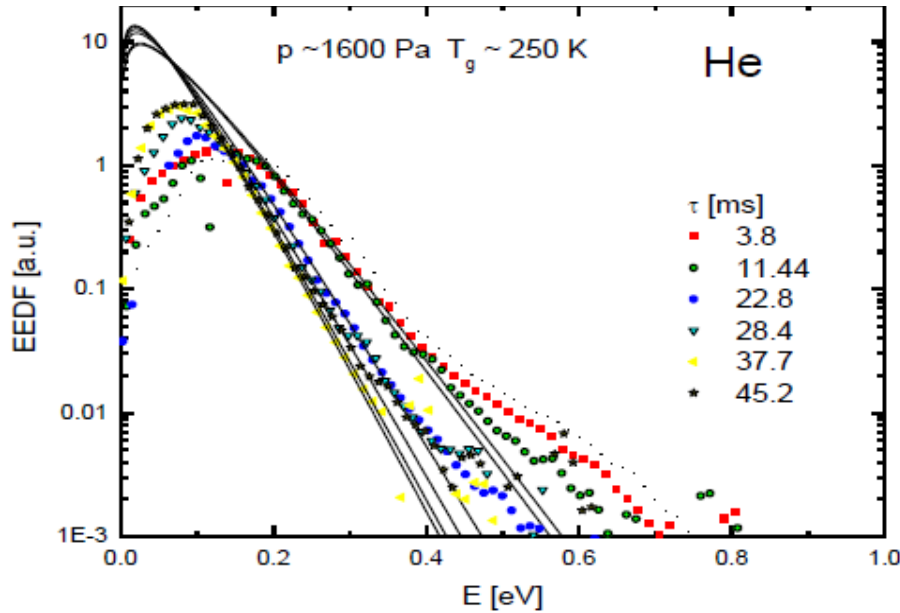
$$\frac{d^2 I}{d(V - V_p)^2} = \frac{1}{4} A q^3 \sqrt{2\pi m_e} (k_B T_e)^{-3/2} e^{-\frac{q(V - V_p)}{k_B T_e}}$$

Maxwellian EEDF

\*Druyvesteyn M.J., *Z. Physik* **64**(1930)781



# Maxwellian versus Bi-Maxwellian



\*V. I. Demidov and C. A. DeJoseph Jr. *Rev. Sci. Instrum.* 77, 116104 (2006)

F.F. Chen Langmuir probe diagnostics, IEEE-ICOPS meeting, Jeju, Korea, 2003

V. Godyak and R. Piejak, *Phys. Rev. Lett.* 65, 996 (1990)

# Electron Density

By EEDF integrating over all energies

$$n_e = \int_0^{\varepsilon_{\max}} f(\varepsilon) d\varepsilon \quad \longleftrightarrow \quad n_e = \int_0^{-\infty} f(U) dU$$

From  $I_e$

$$n_e = \frac{1}{S_{probe} q} \sqrt{\frac{2\pi m_e}{k T_e}} I_e (U_{pr} = V_{pl}) \quad V_{pl}! \quad T_e!$$

J. D. Swift and M. J. R. Schwar. *Electrical probes for plasma diagnostics*. London Iliffe books Ltd., 1970.

**I-squared** method

$$I^2 = \frac{2(Aqn_e)^2}{\pi^2 m_e} [k_B T_e + q(U_{pr} - V_{pl})] \quad n_e = \sqrt{\frac{\pi^2 m_e}{2A^2 q^3} S}$$

Slope of  $I^2(U)$

Španěl P.: *Int J. Mass Spectrom and Ion Proces.*, 149/150, 299, 1995

The concentration of electrons can be easily obtained without the need to determine accurate values of  $V_{pl}$  and  $T_e$

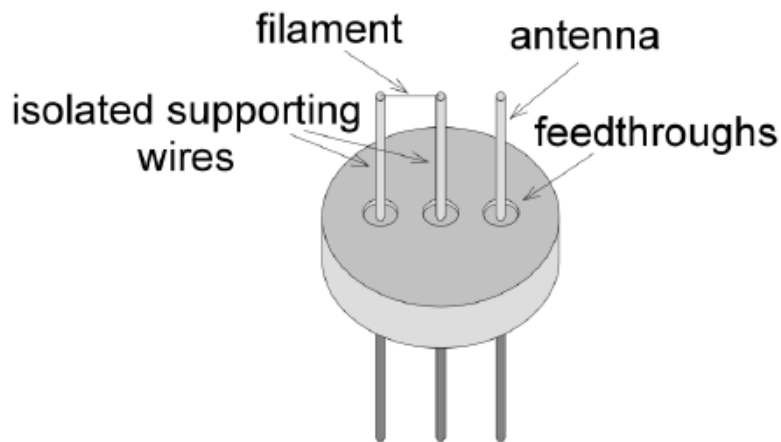
# Problems with Langmuir Probes

- Melting of the probe
- Contamination of the probe
- Interpretation of the results
- Need physics access to the plasma
- Langmuir probe failed in case of insulator deposition experiments

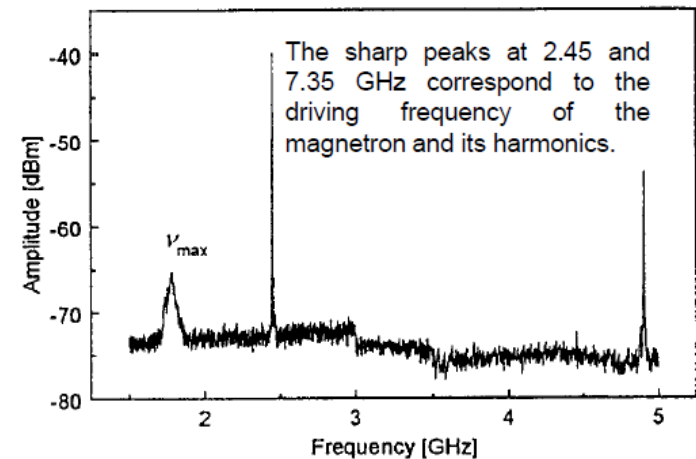


# Plasma Oscillation Probes

In the plasma oscillation method a weak electron beam injected into the plasma excites electrostatic electron waves oscillating at the electron plasma frequency, which is proportional to the square root of the electron density.



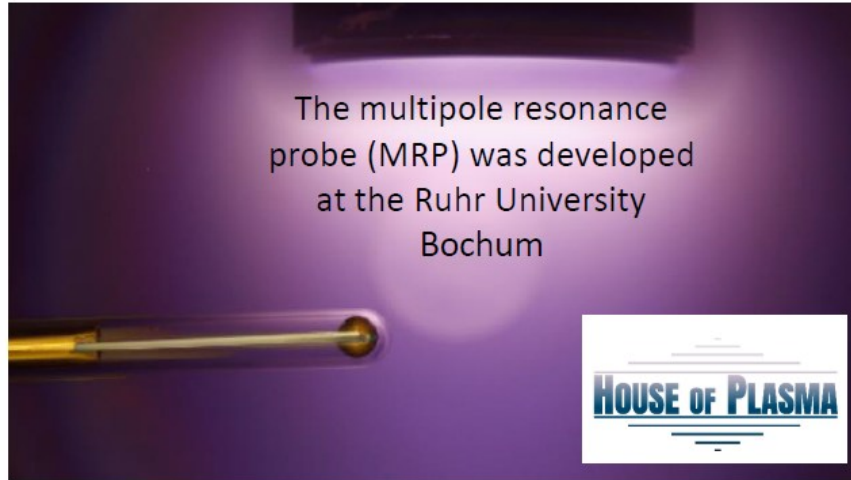
Frequency spectrum in Argon



$$\nu_{\max} \approx \omega_{pe} = \sqrt{\frac{q^2 n_e}{\epsilon_0 m_e}}$$



# Plasma Absorption Probes



$$f_{\text{res}} \sim \omega_{\text{pe}} \sim \sqrt{n_e}$$

The measuring principle is based on Active Plasma Resonance Spectroscopy (APRS). The probe is used to couple a high-frequency signal in the megahertz to gigahertz range via a dielectric into the plasma. At a frequency close to the electron plasma frequency, the plasma absorbs the energy of the signal and resonates. The response of the plasma-probe-system – the reflection value – is picked up by the probe and transmitted to an evaluation unit. Due to symmetry of the probe, its behavior can be analyzed mathematically transparent and a formulaic relationship between the resonance frequency and the electron density of the plasma can be specified.

# Retarding Field Analyzer

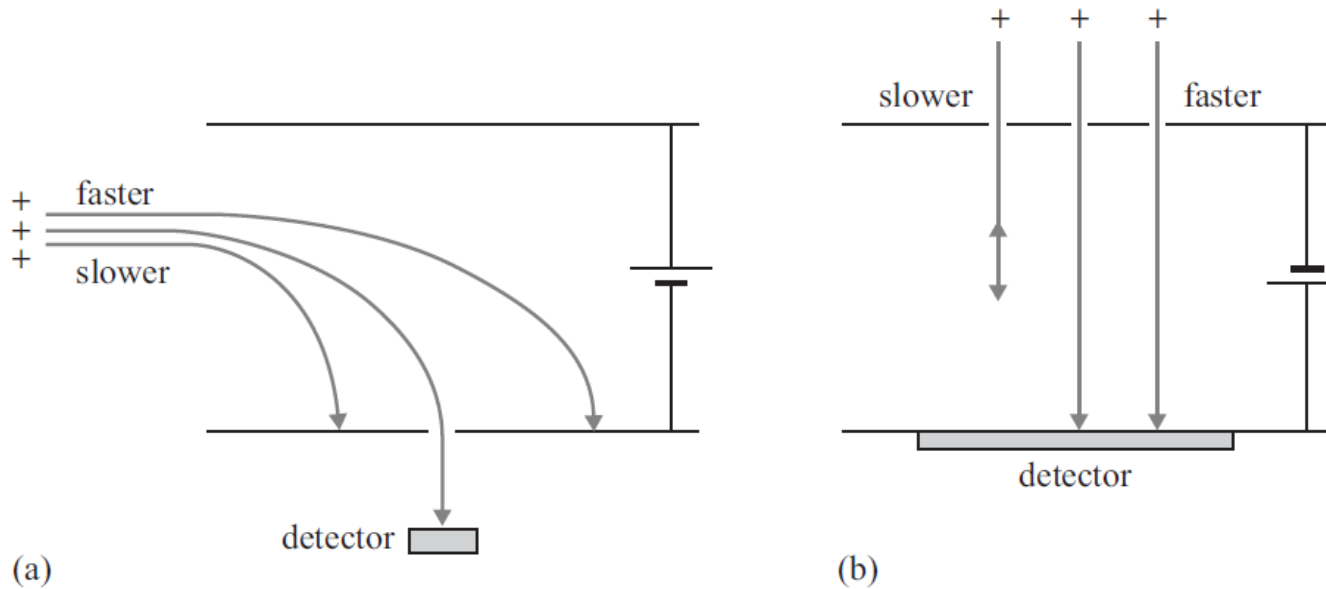
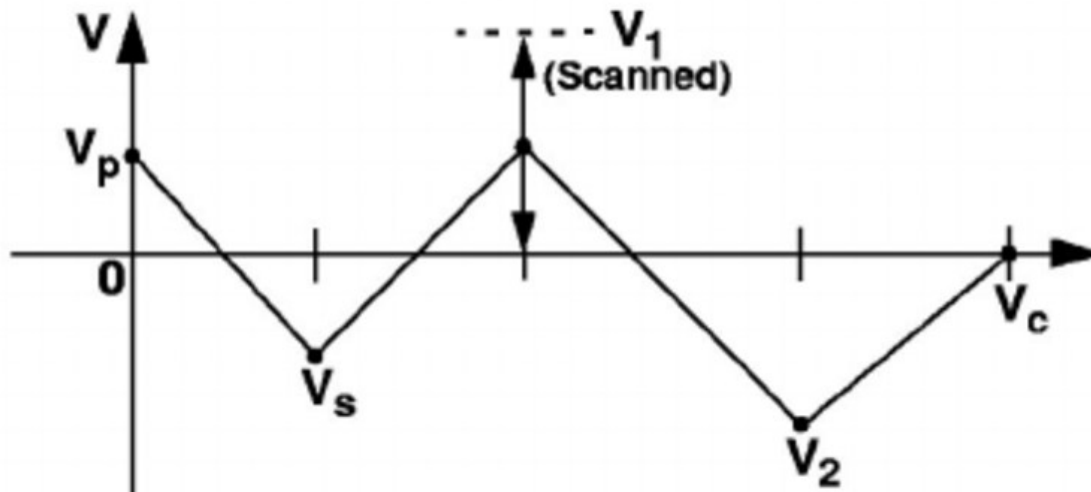
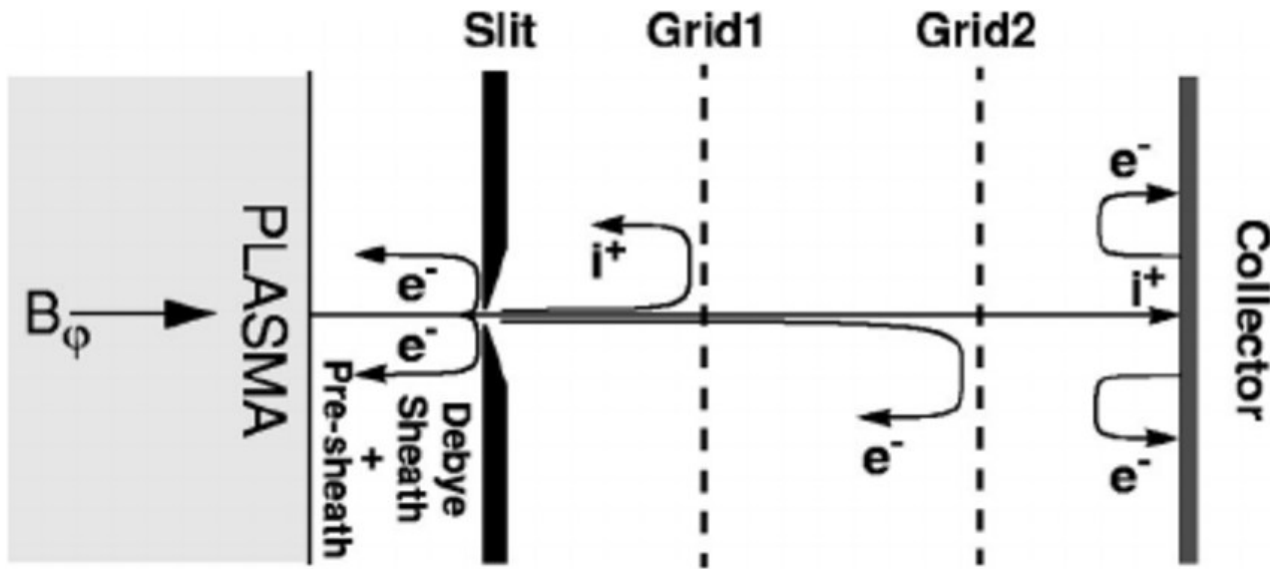


Figure 10.15 (a) A deflecting filter selects particles within a specific (narrow) range of energy; (b) a retarding filter passes particles with energy above a threshold level.



# Retarding Field Analyzer



# Retarding Field Analyzer

$$I = nevA$$

$$\frac{dI}{d\Phi} = eA \frac{d}{d\Phi} \int v f(v) dv$$

$$nv = \int v f(v) dv$$

$$\frac{dI}{d\Phi} = eA \frac{d}{dv} \frac{dv}{d\Phi} \int v f(v) dv$$

$$\frac{dI}{d\Phi} = eA \frac{dv}{d\Phi} \frac{d}{dv} \int v f(v) dv$$

$$\frac{dI}{d\Phi} = eA \frac{dv}{d\Phi} v f(v)$$

# Retarding Field Analyzer

$$\frac{dI}{d\Phi} = eA \frac{dv}{d\Phi} v f(v)$$

In collisionless plasma

$$e\Phi = \frac{1}{2}mv^2$$

$$ed\Phi = mv dv$$

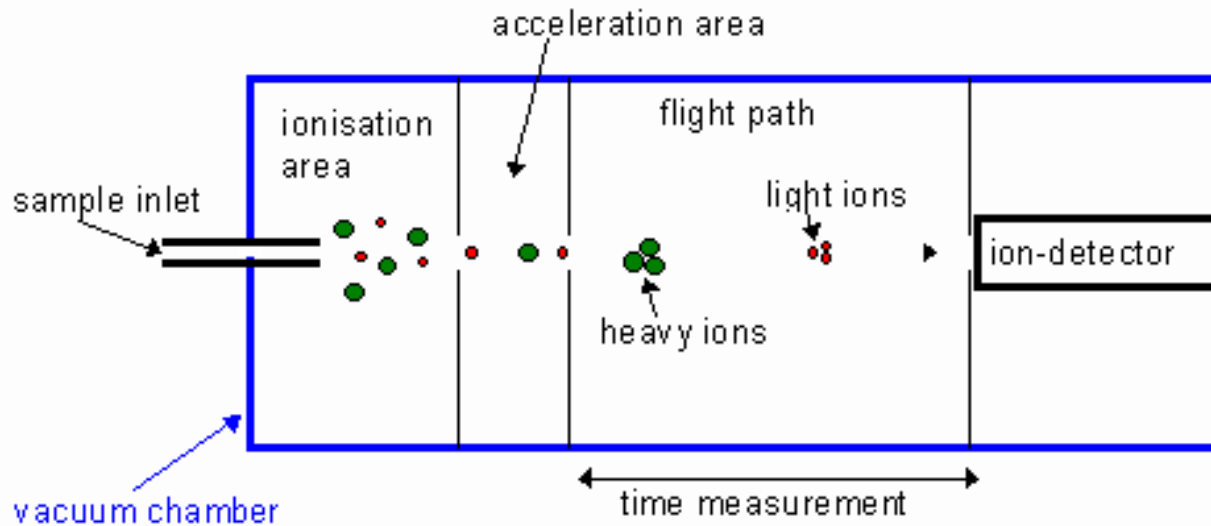
$$\frac{dv}{d\Phi} = \frac{e}{mv}$$

$$\frac{dI}{d\Phi} = eA \frac{dv}{d\Phi} v f(v)$$

$$\frac{dI}{d\Phi} = eA \frac{e}{mv} v f(v)$$

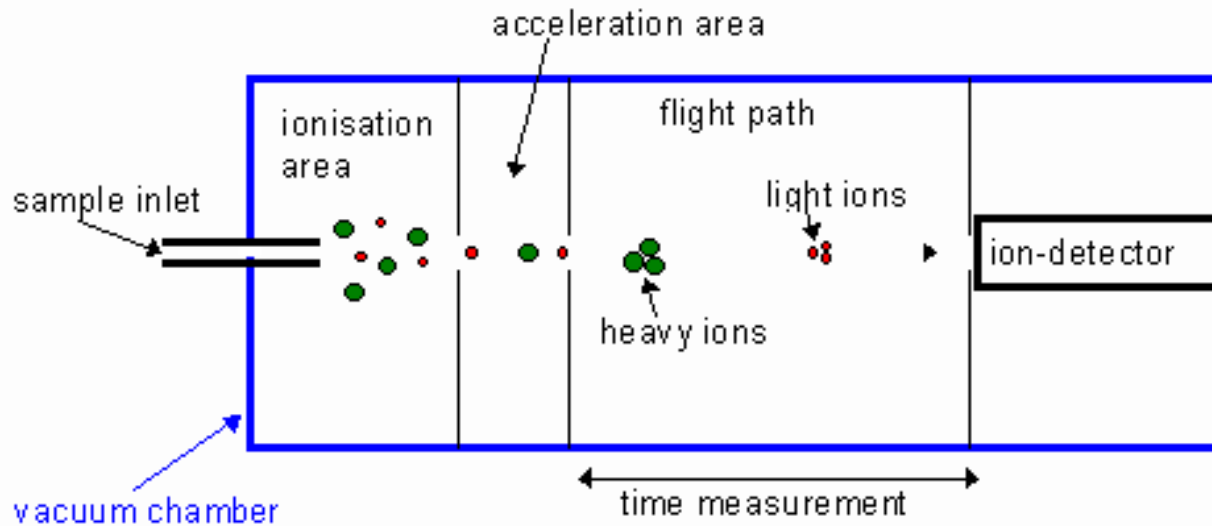
$$\frac{dI}{d\Phi} = A \frac{e^2}{m} f(v)$$

# Mass Spectrometer



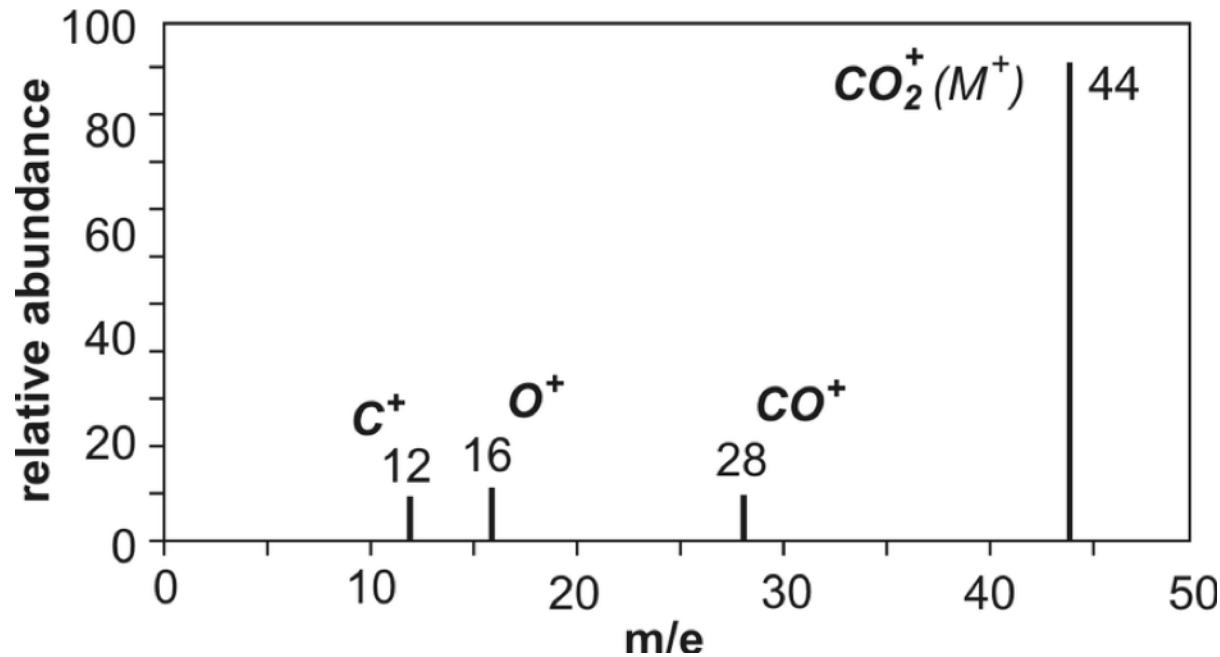
A **Time-of-Flight Mass Spectrometer** works by **accelerating** an **ionised** sample and calculating **mass per charge** based on how long each 'object' is in **flight** for. Since every 'object' receives equal force, according to Newton's Second Law, the acceleration of each 'object' will be inversely proportional to its mass.

# Mass Spectrometer



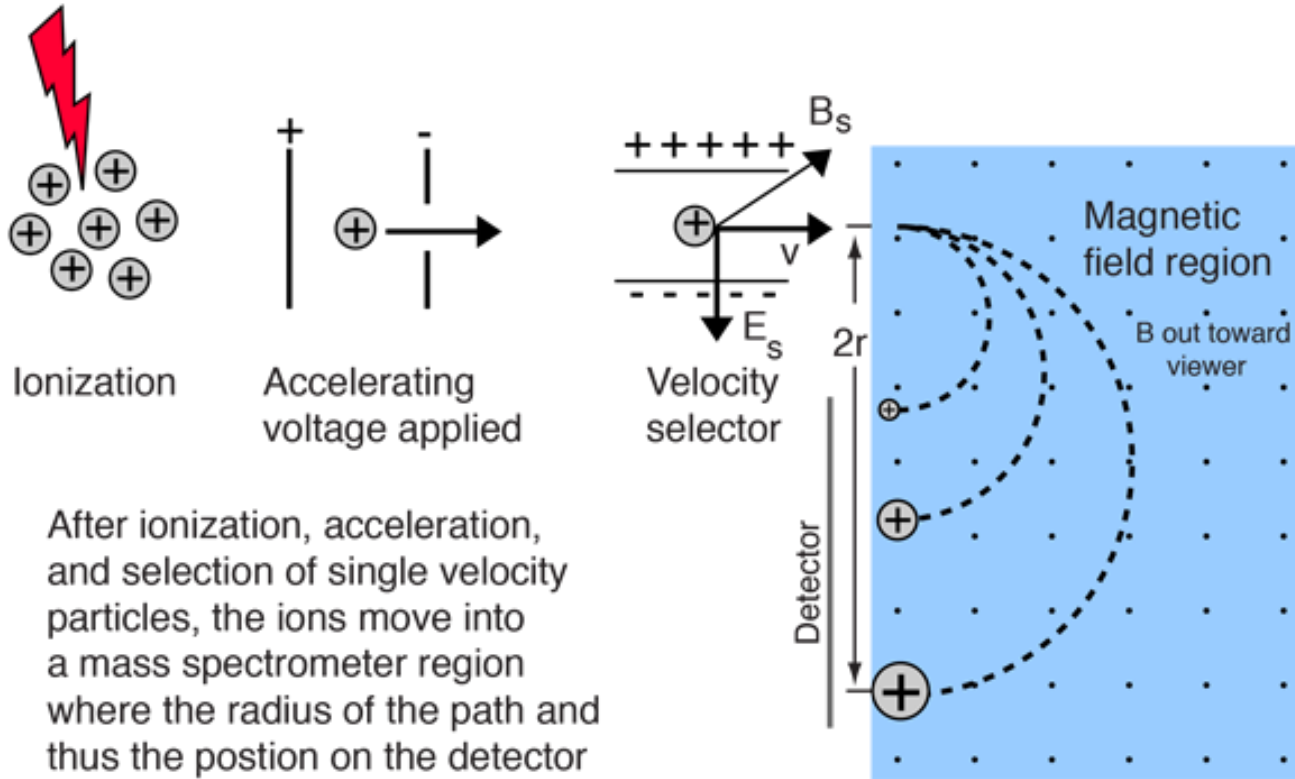
The sample is first **ionised** by **bombarding it with electrons**, which also causes **fragmentation** to form smaller groups of atoms. Ions tend to have **+1 charge**, since a bombarding electron will knock an electron out of an atom's shell, so 'mass per charge' can generally be taken as simply '**mass**'.

# Mass Spectrometer



The ions are then **accelerated** by **Electromagnetic Field** and travel through a **vacuum** area called the **Drift Region**, before being **detected** by the **Ion Detector**.

# Mass Spectrometer



Ionization

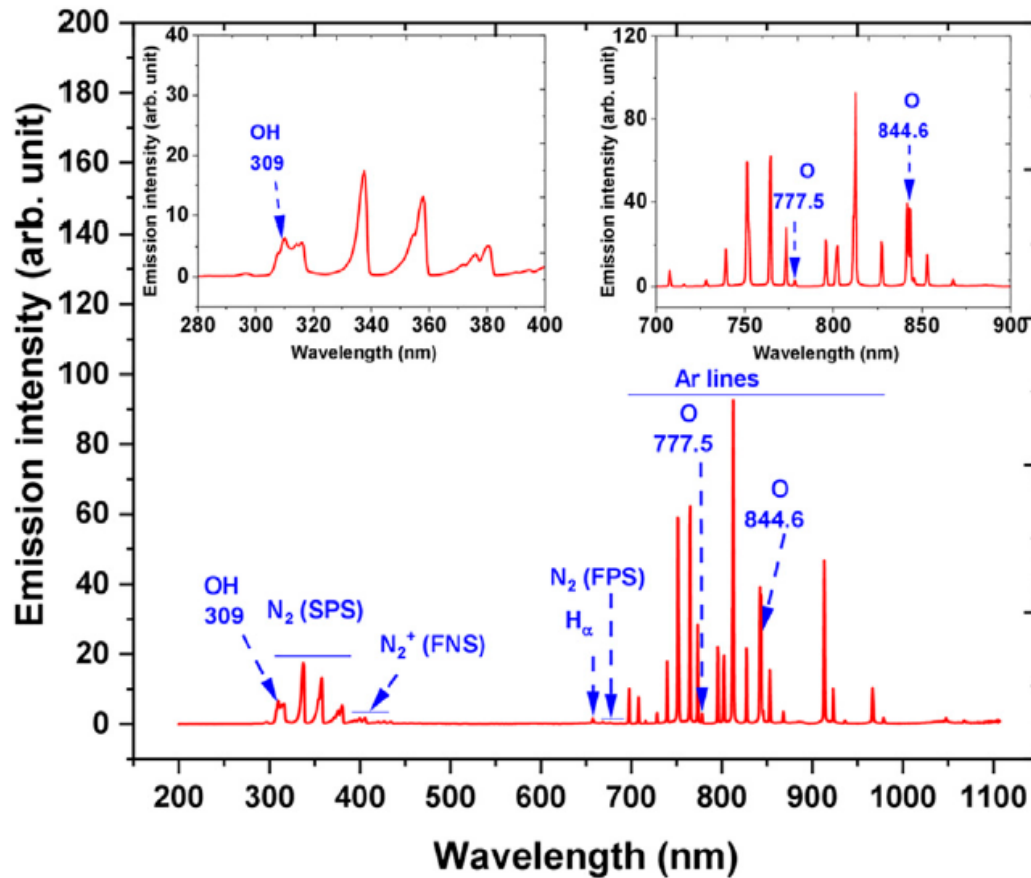
Accelerating voltage applied

Velocity selector

After ionization, acceleration, and selection of single velocity particles, the ions move into a mass spectrometer region where the radius of the path and thus the position on the detector is a function of the mass.

$$r = \frac{mv}{qB} = \frac{mE_s}{qBB_s}$$

# The emission Spectrum



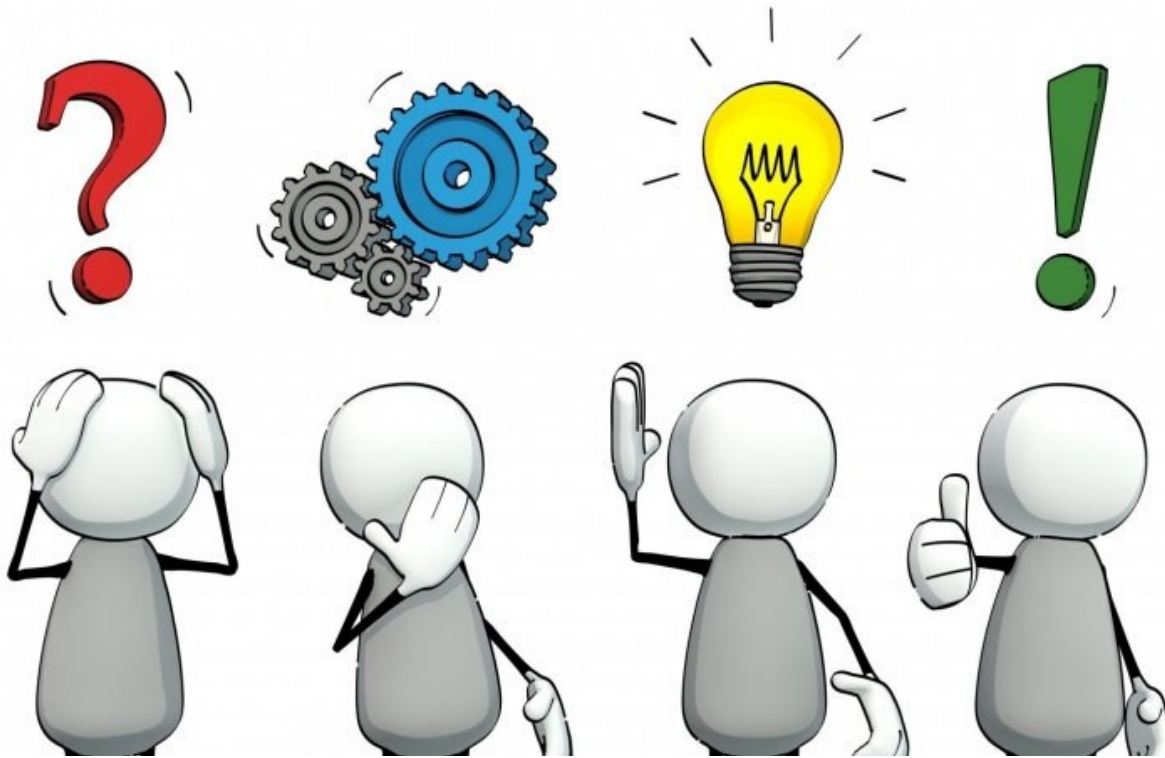
**FIGURE 6** | The emission spectrum of Ar—APPJ in contact with ambient air and over a liquid surface. During the diagnostics, AB25 was placed under APPJ,  $V_o = 5$  ml, Ar 1 slm,  $P_{\text{mean}}$  at the sample 11 W. Inset plots show parts of the spectrum zoomed.



# Good and fast Start

## ■ References:

- **PRINCIPLES OF PLASMA DISCHARGES AND MATERIALS PROCESSING, MICHAEL A. LIEBERMAN & ALLAN J. LICHTENBERG, John Wiley & Sons, Inc (2005).**
- **PHYSICS OF RADIO-FREQUENCY PLASMAS, PASCAL CHABERT & NICHOLAS BRAITHWAITE, Cambridge University Press (2011).**
- **Spacial issue „ Plasma and Nanotechnology“ : , J. Phys. D: Appl. Phys. 44 (2011)**



Thanks!